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A QUANTITATIVE ANALYSIS OF DISTORTIONS IN MANAGERIAL FORECASTS

by Yueran Ma^{*}, Tiziano Ropele[†], David Sraer[‡] and David Thesmar[§]

Abstract

This paper quantifies the economic costs of distortions in managerial forecasts. We match a business survey run by the Bank of Italy with administrative data on firms' balance sheets and income statements. The resulting dataset allows us to observe a long panel of managerial forecast errors for a representative sample of Italian firms with at least 20 employees. We show that managerial forecast errors are positively and significantly autocorrelated. This persistence of forecast errors is consistent with managerial underreaction to new information. To quantify the economic significance of this forecasting bias, we estimate a dynamic equilibrium model with heterogeneous firms and distorted expectations. The estimated model matches not only the persistence of forecast errors, but also the empirical link between investment and managerial forecasts. Compared with a counterfactual with rational expectations, we find that managers exhibit large forecasting biases, which lead to significant distortions in firm-level investment. These distortions, however, imply limited loss in firm value. In general equilibrium, the estimated model leads to negligible aggregate efficiency losses from distorted forecasts.

JEL Classification: D61; D84.

Keywords: Expectation Formation; Misallocation; Corporate Investment.

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1 Introduction ¹

This paper quantifies the effect of biases in managerial forecasts on corporate investment, firm value and aggregate efficiency. Several studies have convincingly documented the existence of systematic biases in managerial decision-making. In a large sample of newly-created French firms, [Landier and Thesmar \(2009\)](#) show that managerial optimism correlates with short-term leverage. [Malmendier and Tate \(2005\)](#) analyze a sample of publicly traded US firms and find a strong positive relation between the sensitivity of investment to cash flow and executive overconfidence. [Malmendier and Tate \(2008\)](#) establish that overconfident managers overpay for acquisitions. Similarly, [Hirshleifer et al. \(2012\)](#) document that overconfident managers invest more in innovation and achieve greater innovative success for given R&D expenditures. A nascent, related, literature emphasizes the importance of systematic errors in managerial forecasting. Using a survey of large public US firms, [Ben-David et al. \(2013\)](#) provide evidence that CEOs exhibit miscalibrated expectations of aggregate stock market returns, and that, in the cross-section of firms, CEO overconfidence correlates with investment and leverage. Using US CFO survey data, [Gennaioli et al. \(2016\)](#) document that managerial expectations tend to be extrapolative, and that expectations have strong explanatory power for firm investment. While these papers establish a *statistically significant* relationship between systematic forecast errors and managerial decisions, our paper asks whether such forecasting biases matter *quantitatively*. Do they create significant distortions in firm-level decisions? Do they significantly impair aggregate efficiency?

Our paper answers these questions in two steps. First, we use a high quality dataset to study managerial expectations. We rely on an annual business survey, the Survey of Industrial and Service Firms, run by the Bank of Italy. This survey collects managerial forecasts of future firm-level outcomes for a panel of about 4,000 firms per year. It samples firms in industrial and service sectors with at least 20 employees. We match this sample with administrative data on firms' balance sheets and income statements. The resulting dataset allows us to analyze the determinants of forecast errors and their connection with actual corporate behavior. Second, we combine reduced-form empirical evidence and a structural model to quantify the eco-

¹We thank seminar participants at ASSA, Princeton University, UIUC, UC Berkeley, Boston College, Brandeis, Chicago, Dartmouth, MIT, UCLA, SITE, 10th Ifo Conference on Macroeconomics and Survey Data, CefES2020 and 2020 Central Bank Macro Modelling Workshop for their insightful comments. The views expressed here should not be interpreted as representing the views of the Bank of Italy or any other institution with which the authors are affiliated.

conomic implications of distortions in managerial forecasts. Standard analyses in the literature usually provide reduced-form evidence showing that biases in managerial forecasts affect firm-level decisions, e.g., financing or investment. These analyses are, however, mostly silent on how much these distortions impair firm value or aggregate efficiency. In contrast, our structural approach builds on such reduced-form evidence and allows us to compare the economy we observe in the data – which potentially features distorted beliefs – with a counterfactual economy where agents hold rational expectations.

Our analysis starts with reduced-form evidence of systematic biases in managerial forecasts. Our approach is similar to recent contributions in the macroeconomics and finance literature that investigates the dynamics of beliefs using survey data.² In particular, we show that, in our panel of Italian firms, managerial forecast errors are highly persistent. The autocorrelation coefficient of log-sales forecast errors is .32 in our preferred specification and is strongly statistically significant. This persistence in forecast errors holds even when controlling for firm fixed-effects and is stable across firm size quintiles and across industries. This result is consistent with the hypothesis that managers underreact to news about their own sales. Intuitively, a positive shock about period t 's sales generates a positive forecast error in period t . If the manager underreacts to this news and sales are persistent, the $t + 1$ forecast will be too low on average, giving rise to another positive forecast error in period $t + 1$. Thus, underreaction to news leads to positive autocorrelation of forecast errors.

We then develop an economic framework to quantify the effect of forecasting biases. We start from a standard neoclassical model of investment with heterogeneous firms, similar to [David and Venkateswaran \(2019\)](#) with the addition that managers may not process information efficiently. Production takes place through a standard Cobb-Douglas technology that combines labor and capital. Firm-level productivity follows an AR(1) process. Every period, managers observe the realization of productivity and a private signal informative about next-period productivity. Firms face a one period time-to-build for capital investment, so that current capital expenditures decisions depend on managerial forecasts about future productivity. In contrast to the standard neoclassical model, these forecasts need not be rational. We extend the formulation of belief formation in [Bordalo et al. \(2018\)](#) to accommodate both over- and underreaction to news about firms' productivity. Managers can either exaggerate the news contained in the current innovation to productivity (the belief distortion empha-

²See, for instance, the recent works by [Coibion and Gorodnichenko \(2015\)](#), [Bordalo et al. \(2018\)](#), [Bordalo et al. \(2019\)](#), [Malmendier and Nagel \(2016\)](#), [Bouchaud et al. \(2019\)](#).

sized in [Bordalo et al. \(2018\)](#)), or instead fail to fully account for its news content.³ In addition to time-to-build, our model make two additional assumptions: (1) firms face quadratic adjustment costs to capital, and (2) forecasts may be observed with measurement error. We introduce these ingredients in the model to account for an important feature of the data. With a Cobb-Douglas production function and no adjustment costs, the elasticity of capital to sales forecast is equal to 1. In the data, this elasticity is about .4. Both adjustment costs and measurement error in forecast break the unit elasticity, and allow the model to match the empirical relationship between news and corporate actions.

We estimate the model using a simulated method of moments. Our estimation targets three key features of the data. The first set of moments relates to firm-level production. We match the productivity process observed in the production data, as well as the autocorrelation of investment to identify capital adjustment costs. The second set of moments characterizes managerial expectations. The estimation targets the persistence in sales forecast errors, which directly relates to the degree of underreaction in managerial forecasts. It also targets the variance of sales forecast errors to measure private information, a key driver of empirical managerial forecasts. The final moment we use is the elasticity of capital to sales forecasts, which pins down the “noise” in empirical forecasts. Consistent with the reduced-form evidence, our estimated structural model indicates the presence of large distortions in forecasts. When forecasting date $t+1$ productivity, we estimate that managers assign a weight on date t productivity shock that is less than half of that for a rational manager. Relative to the rational expectations benchmark, we find that the estimated underreaction leads to an increase in the variance of sales forecast errors of 14.63 %.

This underreaction to news about productivity leads to significant distortions in firm-level investment. For a productivity shock at the 75th percentile of the distribution, the average manager in the data under-invests by 10.01 % relative to the rational expectation counterfactual. Symmetrically, for a productivity shock at the 25th percentile, the inattentive manager over-invest by 16.72 % relative to the rational manager. These large distortions on investment lead, however, to limited reduction in firm value: in the counterfactual where managers hold rational expectations, firm value is only 0.65 % larger. This result emanates in part because, in our model, firms select their capital stock to optimize their value without any additional constraints.

³We emphasize a behavioral interpretation of the persistence in forecast errors. Another interpretation could rely on noisy information models (e.g., [Coibion and Gorodnichenko \(2015\)](#)). However, in our context, we know that managers observe their firm’s realized sales, making this interpretation less appealing.

As a result, at the optimum, first-order deviations in investment only have second-order effects on firm value.⁴ The effect of distorted forecasts is further dampened in general equilibrium, as equilibrium prices mediate the inefficiencies induced by belief distortions: in a rational equilibrium counterfactual, aggregate TFP is only 0.08 % higher than in the data. While statistically significant, and economically sizable when focusing on investment, the managerial underreaction we document in the data has almost negligible effects in terms of aggregate efficiency.

Through its focus on managers and its long panel dataset, our paper contributes to the recent literature that uses forecast data to test rationality. [Coibion and Gorodnichenko \(2015\)](#) show that past revisions positively predict forecast errors in consensus macroeconomic forecasts. They argue that this predictability arises from informational frictions. [Bouchaud et al. \(2019\)](#) document underreaction among stock analysts. Also looking at stock analysts, [Bordalo et al. \(2019\)](#) show that forecast errors on long-term EPS growth forecasts are positively correlated with past growth, suggesting overreaction. [Bordalo et al. \(2020b\)](#) find overreaction in macro and financial variables at the individual level among professional forecasters. [Tanaka et al. \(2019\)](#) analyze the link between firm performance and macro forecast accuracy. Using data on household expectations of inflation, [Malmendier and Nagel \(2016\)](#) find evidence consistent with “experience effects”: heavy discounting of pre-birth data combined with recency bias. We contribute to this literature by shifting the focus to managerial expectations of their own firm’s activity. This is a crucial step to understand the real effects of deviations from rationality coming from the supply side of the economy. Our data shows that managerial sales’ expectations clearly exhibit underreaction to news. On this aspect, our paper is related to independent work by [Barrero \(2020\)](#), who also studies managerial expectations but find evidence consistent with managerial overreaction. We believe that our large, long panel of firms allows us to better estimate distortions in expectation. [Barrero \(2020\)](#) follows about 300 firms over 5 years; in contrast, our sample covers about 4,000 firms per year, over 16 years. We are thus able to include firm fixed-effects and are less likely to suffer from small-sample bias, which typically biases estimates toward overreaction. We explore the differences between the two papers in more detail in our empirical Section.⁵

⁴This finding remains, of course, a quantitative result: larger distortions in forecasts than the ones we estimate in the data could definitely result in large distortions in firm value.

⁵An earlier work studying managerial expectations is ([Bordalo et al., 2018](#)). They use data collected by the Duke CFO survey and find that firms’ earnings forecasts tend to be too high when the level of recent earnings is high. The level of recent earnings, however, does not necessarily capture news. CFOs in this US sample may extrapolate past trends in earnings, and it is difficult to measure news

Through its aggregation approach, our paper also contributes to the literature that investigates the role of managerial information processing on long-term output in steady-state models. On the theory side, [Akerlov and Yellen \(1985\)](#) show that, in most equilibrium settings, near-rational behavior can have first-order aggregate consequences, even when it has second-order individual effects. [Hassan and Mertens \(2017\)](#) build on [Akerlov and Yellen \(1985\)](#) and show that near-rational errors lead to first-order distortions in household savings decisions. On the empirical side, [David et al. \(2016\)](#) develop a steady-state production model similar to ours, but use it to quantify aggregate efficiency improvements that result from a well-developed stock market. [David and Venkateswaran \(2019\)](#) employ a similar model to investigate the effect of information frictions – managers imperfectly observing future productivity – on aggregate efficiency. In contrast to our approach, these papers do not use forecast data and instead assume that managers hold rational expectations. Using detailed survey data, we find that, in addition to information frictions, expectations exhibit underreaction to news, which we incorporate into our structural model.

By relating survey forecasts to actual behavior, our paper also relates to [Giglio et al. \(2020\)](#). Using survey data, [Giglio et al. \(2020\)](#) document a positive and significant relationship between stock market returns forecasts and investors’ risky share. They show that, quantitatively, this empirical relationship is smaller than what a frictionless benchmark would predict. Similarly, we find a positive and significant relation between sales forecasts and corporate investment, but not as large as the one we would observe under a frictionless model.

The rest of the paper is organized as follow. Section 2 presents reduced-form evidence of persistence in managerial forecast errors. Section 3 builds a production framework with heterogeneous firms and distorted expectations, provides a structural estimation of the model, and quantifies a number of partial equilibrium counterfactuals. Section 4 provides aggregation results. Section 7 concludes.

2 Evidence on Managerial Biases

2.1 Data and Summary Statistics

Sample. Our main data comes from the Survey of Industrial and Service Firms (INVIND, henceforth), which is a large annual business survey conducted by the

in the Duke CFO survey.

Bank of Italy on a representative sample of firms. Since 2002, the reference universe in INVIND consists of firms with at least 20 employees operating in industrial sectors (manufacturing, energy, and extractive industries) and in non-financial private services, with administrative headquarters in Italy.⁶ The survey adopts a one-stage stratified sample design. The strata are combinations of branch of activity (according to an 11-sector classification), size class (in terms of number of employees classified in seven buckets), and region in which the firm’s head office is located. In recent years each wave has about 4,000 firms (3,000 industrial firms and 1,000 service firms).

The data is collected by the Bank of Italy’s local branches between February and April every year. Among other things, the survey asks firms to report their sales in three periods: the fiscal year that just ended (preliminary results), the previous fiscal year (final results), and the current fiscal year (forecasts). There are few missing observations: for sales forecast, the average rate of non-response in our sample period is only seven percent per year.⁷ The survey also has an important panel dimension. Firms in the survey tend to participate for many years. Among the firms that respond more than once to the survey, the average firm respond for 7 years; 25% of firms in the sample are present in the sample for at least 10 years. While we do not observe the identity of the survey respondent, we know that the group of control over strategic decisions in our sample is stable: since 2002, only 4% of firms every year report a transfer of control in the INVIND survey.

The extensive use of the Survey of Industrial and Service Firms in the literature is a testament to its reliability. INVIND has been used to study the effect of uncertainty on investment decision (Guiso and Parigi (1999), the role of credit supply shocks for investment decisions (Gaiotti (2013) and Cingano et al. (2016)) or how resource misallocation affects productivity growth in Italy (Calligaris et al. (2018)).

Throughout the paper, we define firm i ’s empirical log-sales forecast errors as the difference between the log of firm i ’s actual sales and the log of firm i ’s sales forecast:

$$\widehat{FE}_{it} = \log sales_{it} - \log F_{i,t-1} sales_{it}$$

where $sales_{it}$ is total sales of year t and $F_{i,t-1} sales_{it}$ is sales forecast reported in February to April of year t .

To compute the firm-specific log-sales forecast error, we measure actual sales ($sales_{it}$) using firm balance sheet data from Company Accounts Data System (CADS), which is

⁶A methodological note about the survey can be found at <https://tinyurl.com/v6unt8n>.

⁷For these missing observations, the Bank of Italy provides an imputed sales forecast. Our results are similar whether or not we use these imputed observations.

managed by the Cerved Group and covers all Italian limited liability companies. We do not use the self-reported sales data in INVIND to measure actual sales (i.e. final result for previous fiscal year) as this information might be subject to self-reporting biases.

We keep firms that report at least 5 sales forecasts.⁸ In all our regression analysis, we deal with outliers by trimming observations that fall beyond the median +/- 5 times the interquartile range. Our final sample runs from 2002 through 2017, and contains about 37,000 total firm-year observations.

Summary Statistics. Table 1 provides summary statistics for our working sample. Panel A focuses on firms for which forecast data are available. Panel B provides descriptive statistics for the universe in order to make a comparison. Log-sales forecast errors have a mean of -.01. That the mean log-sales forecast is negative is expected as a result of Jensen’s inequality. Log-sales forecast errors have a standard deviation of 18%. Figure 1 reports a histogram of log-sales forecast error. This figure shows that the log-sales forecast error is close to normally distributed.

2.2 Forecast accuracy

We first verify the accuracy of managerial sales forecasts in our data. One possible concern is that these reported forecasts are only weakly correlated with managers’ true forecasts, for instance because managers put little effort in answering the survey. In Table 2, we show that sales forecasts are highly informative about actual future sales. To this end, we estimate the following simple linear regression:

$$\log sales_{it} = \alpha + \beta \log F_{i,t-1} sales_{it} + controls_{it-1} + \epsilon_{it},$$

where $sales_{it}$ and $F_{i,t-1} sales_{it}$ represent respectively firm i ’s actual and forecasted sales as defined above. Standard errors are clustered by both firm and time. Table 2, column (1) shows that the coefficient estimate for β is .99 with a standard error of .001. The R^2 of this regression is 99% without firm fixed effects. Column (2) to (4) augment this regression by adding control variables. These specifications are consistent with the finding in Column (1) that managerial forecasts reported in the survey data strongly forecast future realized sales. In Column (5) to (8), we confirm these results using a slightly different specifications: we normalize both realized sales and

⁸In the initial dataset, firms that appears at most 4 years in the sample account for about 15 percent of the overall number of firm-year observations.

forecasted sales with to lagged assets and add a host of control variables. These regressions show that our data on managerial forecasts have useful empirical content. However, they do not prove that the reported sales forecasts are free of measurement error. As a result, we will include in our model measurement error in reported sales forecast. We will identify such measurement error through a combination of two moments: the variance of sales forecast errors and the relationship between sales forecasts and capital investment decisions.

2.3 Forecasts and Capital Investment

We now show that sales expectations are linked to firms' capital investment decisions at the time they are formed. To this end, we regress the log of firm i capital stock for fiscal year t on log-sales forecasts issued at the beginning of year t :

$$\log k_{it} = \alpha_i + \delta_t + \kappa_{\log(k)/\log(\mathbb{F})} \log F_{i,t-1} sales_{it} + \epsilon_{it},$$

where k_{it} is measured as the capital stock (net fixed tangible assets) at the end of year $t - 1$: when there is a one period time to build, this is the capital stock that is used in production in year t . $F_{i,t-1} sales_{it}$ is the forecast of sales in year t made at the beginning of the year and α_i and δ_t denote respectively firm and year fixed effects. Table 3 reports estimates of the coefficient $\kappa_{\log(k)/\log(\mathbb{F})}$ using manufacturing firms only (see Column (1)) and all firms in the sample (see Column (2)). In both cases, the estimated elasticity is statistically significant and about equal to .4: *within a firm*, a 10% increase in sales forecasts is associated with a 4% increase in the capital stock. As explained below, in a simple model with Cobb-Douglas production, noiseless forecasts and no capital friction, this elasticity turns out to be 1. Our Italian data suggest however a smaller response of investment to changes in sales forecasts than the benchmark frictionless model. This is why our model will feature both a real friction (adjustment cost in capital accumulation) and a measurement friction (noise in reported forecasts) to accommodate this empirical finding.

2.4 Persistence of Forecast Errors

Under rational expectations, managerial forecast errors should not be predictable using variables in the manager's information set, which presumably includes past sales and past forecasts. We document instead that managerial forecasts errors are persistent, and positively predictable by previous forecast errors. As hinted in the

Introduction, this feature is consistent with underreaction to new information.

Figure 2 provides a binned scatter plot of the relationship between past log-sales forecast errors (defined as \widehat{FE}_{it-1} above) and current log-sales forecast errors (\widehat{FE}_{it}). To construct this figure, we split the sample in vigintiles of lagged log-sales forecast error on the x-axis and represent the average current log-sales forecast error on the y-axis. As shown, the relationship between lagged and current log-sales forecast error is increasing and close to linear.

We confirm this finding by estimating the following model:

$$\widehat{FE}_{it} = \alpha + \delta_t + \kappa_{FE} \widehat{FE}_{i,t-1} + \epsilon_{it}, \quad (1)$$

where δ_t denotes year fixed effects and α is just a constant. Standard errors are clustered at the firm and year level.

Table 4 reports the estimates of coefficient κ_{FE} . Column (1) uses only manufacturing firms and finds an estimate of κ_{FE} of .29. Column (3) uses all firms in the sample and reports an estimated κ_{FE} of .32. In both cases, the estimated κ_{FE} is highly significant. Columns (2) and (4) add firm fixed effects to equation (1) for manufacturing and all firms respectively. These fixed effects allow firms to exhibit an average bias in their forecast over the sample period (either over-optimism or over-pessimism). It is obviously challenging to disentangle the persistence of forecast errors from a firm-specific constant since our panel dataset contains a finite time length (at most 16 years). In particular, this augmented model cannot be estimated consistently using OLS given the short time period in our sample (Nickell (1981)). As a result, we further restrict the sample to firms with at least nine forecasts and estimate the model using dynamic panel GMM (Arellano and Bover (1995)).⁹ This augmented model leads to an estimate of κ_{FE} of .17 for all firms (.159 for manufacturing), significant at the 1% level.

The results in Table 4 are consistent with the hypothesis that managers underreact to sales-related news. A positive news at date t about date t sales (e.g., a positive productivity shock) implies a positive forecast error at date t . If productivity is persistent, and the manager is slow to incorporate this news into her forecast for date $t + 1$ sales, then this manager is too pessimistic at date t about date $t + 1$ sales, which leads her to exhibit, on average, a positive forecast error at date $t + 1$. Hence, the positive autocorrelation of forecast errors is consistent with underreaction.

⁹In our original survey dataset, firms that report at least nine sales forecast account for about 60 percent of the overall firm-year observations.

A possible concern about the relevance of the finding in Table 4 is that the persistence in forecast error is mostly a phenomenon among smaller firms. We split the entire sample of firms into 5 size groups based on the firm’s number of employees. For each of these groups, we re-run regression (1) separately, both with and without firm fixed effects. We report results in Table 5. Across size groups, the point estimate for κ_{FE} is strongly significant and ranges from .28 to .42 without firm fixed effects and between .143 and .211 when including firm fixed effects. A similar pattern emerges for manufacturing firms as seen in column (3) and (4). If anything, the persistence in forecast errors seems to be slightly increasing with firm size, although given the confidence intervals, we cannot reject the null hypothesis that the estimated autoregressive coefficients are constant across size groups. As a result, we feel comfortable assuming that firms are homogeneous in terms of κ_{FE} in our quantitative exercise.

In parallel work, [Barrero \(2020\)](#) exploits a survey of US managers and document evidence consistent with *managerial overreaction*. [Barrero \(2020\)](#)’s specification is different from ours: he regresses sales growth forecast error on past sales growth and estimates a significant negative coefficient. To assess whether the different findings are driven by the different specifications, we estimate a regression similar to [Barrero \(2020\)](#) using our sample of Italian firms. Precisely, we regress date t+1 log-sales forecast error, which equals the forecast error in log-growth sales, on date t realized log-growth sales. Panel A, Table [IAII](#) in Appendix [A.2](#) shows the result controlling for various fixed-effects. In every specification, we find a positive and significant coefficient, consistent with managerial underreaction.

Another concern with interpreting our findings relates to external validity: while the managers of private companies in Italy may underreact to news, managers of large firms in the US may process information differently. We examine information processing by managers of large US public companies by using guidance data. Every year, a self-selected sample of publicly-traded firms in the US issues sales guidance, which communicates to the market firm’s expectation of sales growth in the coming year. To measure log-sales forecast errors, we match the universe of guidance from 2003 onwards with sales realization in Compustat. Appendix section [A](#) describes the sample in details. Table [IAI](#) provides descriptive statistics for this sample. We use this sample to estimate the persistence of log-sales forecast errors for US public firms. Panel B, Table [IAII](#) in Appendix [A.2](#) shows that, consistent with our main finding in Table 4, forecast errors in the guidance data are significantly auto-correlated over time. Quantitatively, managers in the guidance data exhibit less underreaction than managers in the Italian data: the estimated persistence is about .17, compared with

.32 in our baseline dataset (Table 4).¹⁰

Taken together, the results in Table 4 and Table 5 reject the null hypothesis that managers process information efficiently. However, we cannot directly interpret these point estimates from an economic standpoint. What do they imply for the firm’s investment policy and firm value? To answer this question one would need a structural model in order to “shut down” the forecasting biases that we observe in the data and construct appropriate counterfactuals. This is what we do in Section 3.

3 Structural Model

3.1 Model Setup

We start from a standard neoclassical model of investment augmented with two types of frictions: (1) real capital frictions (one-period time-to-build and quadratic adjustment costs), and (2) distorted beliefs.

3.1.1 Economy

Time is discrete. At date t , firm i combines capital (k_{it}) and labor (l_{it}) to generate sales ($p_{it}y_{it}$) with a Cobb-Douglas technology:

$$p_{it}y_{it} = Ae^{\nu_{it}} (k_{it}^{\alpha} l_{it}^{1-\alpha})^{\theta},$$

where ν_{it} is revenue-based log-productivity, α is the capital share, and θ captures decreasing returns to scale in revenues, which may arise from technology or market power. A is a positive constant. Input markets are competitive. w is the wage rate in the labor market and r is the safe rate of return in this economy.¹¹ At date t , firms hire l_{it} employees after observing ν_{it} . We assume an AR(1) process for ν_{it} :

$$\nu_{it} = (1 - \rho)\mathcal{V}_i + \rho\nu_{it-1} + \psi_{it} + \omega_{it} \quad \text{with} \quad (\omega_{it}, \psi_{it}) \sim \mathcal{N} \left[\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_{\omega}^2 & 0 \\ 0 & \sigma_{\psi}^2 \end{pmatrix} \right] \quad \& \quad \mathcal{V}_i \sim \mathcal{N}(0, \sigma_{\mathcal{V}}^2) \quad (2)$$

¹⁰In parallel work, [Bordalo et al. \(2020a\)](#) also use guidance data. They find that firms’ earnings forecasts correlate negatively with recent earnings. The level of recent earnings, however, does not necessarily capture news. In addition, with persistent earnings, this specification is exposed to small sample bias, which bias the estimates in the direction of overreaction.

¹¹We omit the time subscript for w and r , as we only consider steady-state economies.

where ν_i is the long-run mean of firm i 's productivity. Furthermore, ω_{it} is a shock realized at date t whereas ψ_{it} denotes a private signal observed by the manager at date $t - 1$ (but not by the econometrician). Our model thus allows for managerial private information about future productivity, as in [David and Venkateswaran \(2019\)](#).

At date t , the firm chooses labor demand l_{it} , given current productivity ν_{it} and installed capital k_{it} , to maximize operating profits:

$$\max_{l_{it}} \left\{ A e^{\nu_{it}} k_{it}^{\alpha\theta} l_{it}^{(1-\alpha)\theta} - w l_{it} \right\} = \Omega e^{\frac{\Phi}{\alpha\theta} \nu_{it}} k_{it}^{\Phi} \quad (3)$$

where $\Phi \equiv \frac{\alpha\theta}{1-(1-\alpha)\theta}$ and $\Omega \equiv (1 - (1 - \alpha)\theta) \left(\frac{(1-\alpha)\theta}{w} \right)^{\frac{1-\alpha}{\alpha} \Phi} A^{\frac{\Phi}{\alpha\theta}}$.

We assume a one-period time-to-build in capital: firms invest in the capital stock k_{it} before ν_{it} is realized. As a result, before investing managers need to form expectations about next-period productivity. The next section describes our model of belief formation.

3.1.2 Distorted Expectations

Managers may exhibit distorted expectations about future productivity. In the spirit of [Bordalo et al. \(2018\)](#), we assume that managers use the following conditional density:

$$h_{t-1}^s(\nu_{it} | \nu_{it-1}, \psi_{it}) = h(\nu_{it} | \nu_{it-1}, \psi_{it}) \left[\frac{h(\nu_{it} | \nu_{it-1}, \psi_{it})}{h(\nu_{it} | \widehat{\nu}_{it-1} = \rho\nu_{it-2} + \psi_{it-1}, \psi_{it})} \right]^{\gamma} \frac{1}{Z} \quad (4)$$

where Z is a normalization coefficient. The subjective density h^s depends on two terms. The first term, h , is the objective conditional distribution of ν_{it} , conditional on the information available at the beginning of date t , ν_{it-1} and ψ_{it} . The second term corresponds to the over- or underreaction to the surprise realization ω_{it-1} . The “diagnosticity” is large when the past realization of productivity is high compared to its rational expectation. Those states are overweighted when $\gamma > 0$ (representativeness bias in [Bordalo et al. \(2018\)](#)). They are underweighted when $\gamma < 0$. A negative γ can be rationalized as a lack of attention: large surprises are less representative of potential realization and therefore more likely to be overlooked. From a psychological standpoint, such a bias can be related to the “conservatism” bias emphasized in [Edwards \(1968\)](#).

Given our parametric assumptions on the distribution of ω and ψ , it is straightforward to show that the formulation of beliefs in Equation (4) leads the manager to believe in the following conditional distribution for ν_{it} :

$$\nu_{it} \sim \mathcal{N} \left((1 - \rho)\mathcal{V}_i + \rho\nu_{it-1} + \psi_{it} + \underbrace{\gamma\rho\omega_{it-1}}_{\text{over/underreaction}}, \sigma_\omega^2 \right) \quad (5)$$

Note that when $\gamma = 0$, this formulation boils down to the rational expectation. When $\gamma > 0$ (resp. < 0), managers overreact (resp. underreact) to the date $t - 1$ innovation in productivity ω_{it-1} . This formulation is similar to [Bordalo et al. \(2018\)](#), but extends it to underreaction by allowing γ to be negative, which will turn out to be the case in our estimation.

The final feature of reported managerial forecasts in our model is that they may contain noise. Such noise can help explaining the low elasticity of capital to managerial forecast we document in [Table 3](#), and is a reasonable assumption when dealing with survey data ([Giglio et al., 2020](#)). More precisely, we assume that reported log-sales forecasts are described by:

$$\log \left(\widehat{\mathbb{F}}_{i,t-1}[p_{it}y_{it}] \right) = \log \left(\mathbb{F}_{i,t-1}[p_{it}y_{it}] \right) + \zeta_{it}, \quad \text{where: } \zeta_{it} \sim \mathcal{N} \left(0, \sigma_\zeta^2 \right) \quad (6)$$

where $\log \left(\widehat{\mathbb{F}}_{i,t-1}[p_{it}y_{it}] \right)$ is the observed sales forecast and $\log \left(\mathbb{F}_{i,t-1}[p_{it}y_{it}] \right)$ is the true forecast on which the manager bases her investment decisions.

Sales forecasts are not structural objects but depend on endogenous employment decisions by managers. We assume that there is a one-period time to build in capital so that sales forecasts take the capital decision as given. But labor is expected to be ex-post chosen optimally. With the formulation of forecasts in [Equation \(5\)](#), the empirical log-sales forecast error (\widehat{FE}_{it}) then admits a simple expression:

$$\begin{aligned} \widehat{FE}_{it} &= \log(p_{it}y_{it}) - \log(\mathbb{F}_{t-1}[p_{it}y_{it}]) - \zeta_{it} \\ &= \underbrace{-\frac{\Phi}{\alpha\theta}\gamma\rho\omega_{it-1}}_{\text{Belief distortions}} + \underbrace{\frac{\Phi}{\alpha\theta}\omega_{it} - \frac{1}{2}\left(\frac{\Phi}{\alpha\theta}\right)^2\sigma_\omega^2}_{\text{Rational expectation error}} - \underbrace{\zeta_{it}}_{\text{Noise}} \end{aligned} \quad (7)$$

Log-sales forecast errors are first driven by the bias parameter γ . Past positive productivity shocks will lead to larger future forecast errors if $\gamma < 0$. This will induce persistence in forecast errors, as we find in the data. The rational expectation error is negative on average, due to Jensen's inequality. Forecast errors also include the expectation noise ζ_{it} . However, private information is *not* part of forecast errors, as should be expected. This will help identification as we discuss below.

3.1.3 Investment

Capital k_{it} is selected at $t - 1$ and depreciates at the constant rate δ . When investing, we assume that the firm faces quadratic adjustment cost to capital (Hayashi, 1982). Specifically, starting from capital k_{it-1} , installing capital k_{it} costs the firm $c_k \frac{(k_{it} - (1 - \delta)k_{it-1})^2}{k_{it-1}}$, in addition to the actual capital expenditures. As discussed above, in addition to the measurement error on sales forecast, this feature of the model is useful to rationalize the low elasticity of capital to sales forecast observed in the data (Table 3).

These adjustment costs imply that the firm's manager faces a dynamic optimization problem. This problem can be represented by a Bellman equation with four state variables. The endogenous state variable is the capital stock installed in the previous period, k . The three exogenous state variables are (1) the current level of productivity ν , (2) the private information about next period productivity ψ , and (3) the current shock ω . In particular, ω is a state variable because the manager bases her forecast on the subjective distribution described in Equation (5), so that she does not process the news about ω efficiently.¹²

Since we consider a steady-state economy with no aggregate risk, the firm discounts future profits at the safe rate of return. As a result, for a firm with long term productivity ν_i , the dynamic optimization problem admits the following Bellman representation:

$$V^i(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1})) = \max_{k_{it+1}} \left\{ \Omega e^{\frac{\Phi}{\alpha\delta} \nu_{it}} k_{it}^\phi - (k_{it+1} - (1 - \delta)k_{it}) - c_k \frac{(k_{it+1} - (1 - \delta)k_{it})^2}{k_{it}} + \frac{1}{1 + r} \mathbb{E}_{it} [V^i(k_{it+1}; \nu_{it+1}, \omega_{it+1}, \psi_{it+2}) | (\nu_{it}, \omega_{it}, \psi_{it+1})] \right\}$$

with:

$$\begin{pmatrix} \nu_{it+1} \\ \omega_{it+1} \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N} \left(\begin{pmatrix} (1 - \rho)\nu_i + \rho\nu_{it} + \gamma\rho\omega_{it} + \psi_{it+1} \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix} \right) \text{ and } \psi_{it+2} \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

As shown formally in Appendix B.1, we can simplify the previous problem by expressing its solution as a function of another Bellman equation that does not depend

¹²For a rational manager, at date t , ν_{it} and ψ_{it+1} are sufficient to make an efficient forecast about ν_{it+1} .

on long-term productivity. Consider the following Bellman equation:

$$(8) \quad V(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1})) = \max_{k_{it+1}} \left\{ \Omega e^{\frac{\Phi}{\alpha\theta} \nu_{it}} k_{it}^\phi - (k_{it+1} - (1 - \delta)k_{it}) - c_k \frac{(k_{it+1} - (1 - \delta)k_{it})^2}{k_{it}} + \frac{1}{1 + r} \mathbb{E}_{it} [V(k_{it+1}; \nu_{it+1}, \omega_{it+1}, \psi_{it+2}) | (\nu_{it}, \omega_{it}, \psi_{it+1})] \right\}$$

with:

$$\begin{pmatrix} \nu_{it+1} \\ \omega_{it+1} \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N} \left(\begin{pmatrix} \rho\nu_{it} + \gamma\rho\omega_{it} + \psi_{it+1} \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix} \right) \quad \text{and} \quad \psi_{it+2} \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

Then, let $k^*(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ be the optimal policy function of this Bellman problem and let $V(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ be its optimal value. It is straightforward to show that the optimal policy function $k^{i,*}(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ and the value function $V^i(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ of a firm with long-term productivity \mathcal{V}_i can be expressed as:

$$\begin{cases} k^{i,*}(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1})) = e^{\frac{\mathcal{V}_i}{1-\theta}} \times k^*\left(\frac{k_{it}}{e^{\frac{\mathcal{V}_i}{1-\theta}}}; (\nu_{it} - \mathcal{V}_i, \omega_{it}, \psi_{it+1})\right) \\ V^i(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1})) = e^{\frac{\mathcal{V}_i}{1-\theta}} \times V\left(\frac{k_{it}}{e^{\frac{\mathcal{V}_i}{1-\theta}}}; (k_{it}; (\nu_{it} - \mathcal{V}_i, \omega_{it}, \psi_{it+1}))\right) \end{cases} \quad (9)$$

We can therefore solve the problem of a firm with long-term productivity \mathcal{V}_i by simply solving the Bellman problem (8) and then applying Equation (9) to its value and policy function.

3.2 Model Identification

In our baseline estimation, we calibrate four parameters: α , the capital share, is calibrated to be .33; θ , the decreasing returns to scale in revenue, is .8; δ , the depreciation rate of capital is set to 10%; finally, the risk-free rate, r , is calibrated to 5%. In Section 6 below, we show that our main findings are robust to alternative calibration of α and θ .

We estimate the key parameters of the model via a Simulated Method of Moments (SMM). We look for the set of parameters $\Theta = (\rho, \sigma_\omega, \sigma_\psi, \gamma, \sigma_\zeta, c_k, \sigma_\nu)$ such that model-generated moments $m(\Theta)$ on simulated data fit a predetermined set of data moments m . We use indirect inference because we cannot solve the model analytically (but we solve a particular case analytically below in order to build intuition). Our SMM estimation is done in two steps:

1. For a given set of parameters, we solve the Bellman equation (8) numerically and obtain the optimal policy function $k^{i,*}$. We use policy function iteration on a discrete grid for the state space $(k; (\nu, \omega, \psi))$
2. Our parameter estimates minimize the distance from simulated to data moments,

$$\hat{\Theta} = \operatorname{argmin}_{\Theta} ((\mathbf{m} - m(\Theta))' \Sigma (\mathbf{m} - m(\Theta)))$$

where the weighting matrix Σ is the inverse of the variance-covariance matrix of empirical moments. Standard errors are obtained by bootstrapping on the estimation sample using a block bootstrap at the firm-level.

We now describe the set of moments we use in our estimation. We follow [David et al. \(2016\)](#) and construct revenue-based productivity using our calibration for α and θ . For firm i at date t , we compute its productivity as $\hat{\nu}_{it} = \frac{\alpha\theta}{\Phi} (\log(VA_{it}) - \Phi \log(k_{it}))$, where VA_{it} denotes firm i 's value added for fiscal year t ¹³ and k_{it} is the stock of net fixed tangible assets at the end of year $t - 1$.¹⁴ Both variables are taken from CADs.

We then estimate three moments that capture the dynamic process followed by firms' productivity as posited in Equation (2). The first moment is $\hat{\chi} = \frac{\operatorname{Var}(\hat{\nu}_{it} - \hat{\nu}_{it-2})}{\operatorname{Var}(\hat{\nu}_{it} - \hat{\nu}_{it-1})} - 1$. If $\hat{\nu}_{it}$ follows an AR(1) process with a persistent component, then $\hat{\chi}$ is an unbiased estimate of ρ in the model, even in small sample ([Lo and MacKinlay \(1988\)](#)). We then compute $\mathbb{V}_i = \frac{1}{T} \sum_{t=1}^T \frac{\hat{\nu}_{it} - \hat{\chi}\hat{\nu}_{it-1}}{1 - \hat{\chi}}$ and then estimate its cross-sectional variance: $\sigma_V^2 = \operatorname{Var}_i(\mathbb{V}_i)$. In the model, \mathbb{V}_i depends on the long-term productivity of firm i , \mathcal{V}_i and the within-firm average of TFP innovations: $\mathbb{V}_i = (\mathcal{V}_i + \frac{1}{T} \sum_{t=1}^T \frac{(\omega_{it} + \psi_{it})}{1 - \rho})$. Finally, we estimate the variance of TFP residuals $\hat{\sigma}_\tau^2 = \operatorname{Var}(\hat{\nu}_{it} - \hat{\chi}\hat{\nu}_{it-1} - (1 - \hat{\chi})\mathbb{V}_i)$, which provides an estimate of the variance of innovations to the productivity process ($\sigma_\psi^2 + \sigma_\omega^2$ in the model).

More specifically, our estimation targets the following seven empirical moments, which include the three moments pertaining to firms' productivity process just described as well as four additional moments relating to managerial forecasts and investment:

¹³Note that our model does not have intermediary inputs, so that value added is equal to total sales. The model can be extended to include intermediary inputs by assuming a Cobb-Douglas production function in inputs, labor and capital. Value added is then simply a constant share of total sales and all our analysis carries through.

¹⁴In the model, k_{it} is determined at date $t - 1$ but can only be used for production in period t . PPE observed in year $t - 1$ includes the capital expenditures made in year $t - 1$ and thus corresponds to our definition of k_{it} in the model.

1. Variance of the estimated productivity innovations $\widehat{\sigma}_\tau^2$. This estimate has a direct counterpart in the model: $\widehat{\sigma}_\tau^2 = \sigma_\omega^2 + \sigma_\psi^2$, a combination of the true innovation in the TFP process and the information about TFP innovations privately known by the manager a period in advance.
2. Estimated persistence of productivity process $\widehat{\chi}$. In the model, this estimate corresponds directly to the persistence parameter ρ in Equation (2).
3. The cross-sectional variance of \mathbb{V}_i : as explained above, \mathbb{V}_i corresponds in the model to the persistent component in TFP \mathcal{V}_i , plus the within-firm average of TFP innovations $\frac{1}{T} \sum_{t=1}^T \frac{(\omega_{it} + \psi_{it})}{1-\rho}$. We target the cross-sectional variance of \mathbb{V}_i : $\sigma_V^2 = \text{Var}_i(\mathbb{V}_i)$.
4. Persistence of sales forecast errors. Given the closed-form expression for log-sales forecast error in Equation (7), it is possible to show that (see Appendix B.2):

$$\kappa_{FE} = -\frac{\left(\frac{\Phi}{\alpha\theta}\right)^2 \gamma \rho \sigma_\omega^2}{\sigma_{FE}^2},$$

where σ_{FE}^2 is the variance of log-sales forecast errors.

As discussed in the empirical Section, Table 4 presents the empirical estimates for κ_{FE} . We use Columns (1) and (3). These specifications do not include firm fixed-effects, since our model does not allow for systematic optimism/pessimism bias. Intuitively, this moment helps identify the structural parameter γ , which governs the degree of over- or underreaction. Under rational expectations ($\gamma = 0$), forecast errors should be i.i.d. over time and κ_{FE} should be 0. As explained in Section 2.4, persistent forecast errors ($\kappa_{FE} > 0$) are consistent with underreaction ($\gamma < 0$).

5. Variance of log-sales forecast errors (net of year fixed effects) ($\widehat{\sigma}_{FE}^2$). In Appendix B.2, we show that this variance can be derived from Equation (7):

$$\sigma_{FE}^2 = \sigma_\zeta^2 + \left(\frac{\Phi}{\alpha\theta}\right)^2 (1 + \gamma^2 \rho^2) \sigma_\omega^2$$

The variance of forecast errors contains the rational forecast error, $\left(\frac{\Phi}{\alpha\theta}\right)^2 \sigma_\omega^2$, and two extra terms: the expectation noise σ_ζ^2 and the additional effect of forecasting biases $\left(\frac{\Phi}{\alpha\theta}\right)^2 \gamma^2 \rho^2 \sigma_\omega^2$. As usual in expectations studies, expectations biases increase the variance of forecast errors whether biases consist of over- or underreaction, since the rational expectation is the minimum MSE estimate.

6. Autocorrelation of firm investment rate, $\widehat{\kappa_{capex}}$. In the data we estimate this coefficient through a simple linear model (with time fixed-effects):

$$\frac{k_{it+1} - (1 - \delta)k_{it}}{k_{it}} = \alpha + \kappa_{capex} \frac{k_{it} - (1 - \delta)k_{it-1}}{k_{it-1}} + \epsilon_{it} \quad (10)$$

Intuitively, κ_{capex} captures the extent of quadratic adjustment costs c_k , and is a moment classically used to pin down capital adjustment cost (e.g. [Cooper and Haltiwanger \(2006\)](#)).

7. Elasticity of the capital stock to sales forecast. As explained above, in a frictionless model with Cobb-Douglas production function, this elasticity should be one, whether expectations are rational or not. Intuitively, this elasticity will be lower than one in the presence of capital adjustment costs (c_k) and the variance of noise in the sales forecast (σ_ζ^2). We do not have a closed form solution for this moment to match with the estimates reported in [Table 3](#), but we build intuition with a model without adjustment costs in the next Section.

To illustrate how the model is identified, [Figure 3](#) shows numerical comparative statics for the estimated model. To construct this figure, we start from the set of parameters estimated in [Section 3.4](#) below. We then vary one of the parameters around its estimated value and re-compute the simulated moments with this alternative set of parameters. [Figure 3](#) reports the parameter/moment pairs for which a variation in the parameter leads to a significant variation in the simulated moment. [Figure 3](#) highlights a number of intuitive relationships in the data. Adjustment costs c_k increase the persistence of investment and decrease the elasticity of capital to forecast. The noise in managerial forecasts, σ_ζ , increases the variance of forecast errors, but decrease the persistence of forecast errors and the elasticity of capital to forecast (attenuation bias). A more persistent TFP process (ρ) leads to a higher estimated persistence of TFP residuals $\hat{\chi}$, but also to a larger variance of forecast errors, a larger persistence of forecast errors, a larger persistence of investment and a larger elasticity of capital to forecast. An increase in inattention, i.e., a lower γ , mostly leads to an increase in the variance of forecast errors, and an increase in the persistence of forecast errors. An increase in the dispersion of the true TFP innovations, σ_ω , leads to an increase in the variance of forecast errors, an increase in the persistence of forecast errors, an increase in the variance of total TFP innovations (σ_τ^2), an increase in the cross-sectional variance of \mathbb{V}_i , and an increase in both the persistence of investment and the elasticity of capital to forecasts. Symmetrically, an increase in the private

information component of TFP innovations, σ_ψ , leads to a decrease in both the persistence of investment and the elasticity of capital to forecasts. Identification in our model is obtained through the combination of these relationships between simulated moments and structural parameters. In the next section, we build further intuitions by considering a simplified version of our model.

3.3 Building Intuition

In this section, we build a number of intuitions for the estimation by exploring a simpler version of the model that features no adjustment costs to capital ($c_k = 0$) and no measurement error in reported sales forecast ($\sigma_\zeta = 0$).

In this simplified version of the model, the optimal capital stock admits a closed-form solution. In the absence of adjustment costs, the user cost of capital is $R = r + \delta$, and the firm selects its optimal capital stock at date $t - 1$ to maximize date t profits, that is:

$$\max_{k_{it}} \left\{ \Omega \mathbb{F}_{it-1} \left[e^{\frac{\Phi}{\alpha\theta} \nu_{it}} \right] k_{it}^\Phi - R k_{it} \right\}$$

which then yields

$$k_{it} = \left(\frac{\Phi}{R} \right)^{\frac{1}{1-\Phi}} \Omega^{\frac{1}{1-\Phi}} \left(\mathbb{F}_{it-1} \left[e^{\frac{\Phi}{\alpha\theta} \nu_{it}} \right] \right)^{\frac{1}{1-\Phi}}.$$

Using our formula for distorted expectations, it is straightforward to show that the optimal log-capital stock is:

$$\log(k_{it}) = \frac{1}{1-\Phi} \left(\log \left(\frac{\Phi \Omega}{R} \right) + \frac{\Phi}{\alpha\theta} ((1-\rho)\mathcal{V}_i + \rho(\nu_{it-1} + \gamma\omega_{it-1}) + (1+\lambda)\psi_{it}) + \frac{1}{2} \left(\frac{\Phi}{\alpha\theta} \right)^2 \sigma_\omega^2 \right)$$

In particular, in this simple model, the first-order condition in capital implies a unit elasticity of capital to forecast:

$$\log(k_{it}) = \log \left(\frac{\Phi \Omega}{R} \right) + \log(\mathbb{F}_{t-1} [p_{it} y_{it}])$$

This model is obviously unable to account for the finding in Table 3: in the data, this elasticity is around .4. The data thus calls for an additional ingredient to break this unit elasticity. The first ingredient we consider is measurement error in the reported forecast: $\log(\widehat{\mathbb{F}_{i,t-1}[p_{it} y_{it}]}) = \log(\mathbb{F}_{i,t-1}[p_{it} y_{it}]) + \zeta_{it}$, where $\zeta_{it} \sim \mathcal{N}(0, \sigma_\zeta^2)$. The noise term ζ serves as classical measurement error for the log-sales forecast and therefore biases downwards the coefficient of a regression of $\log(k_{it})$ on $\log(\mathbb{F}_{t-1} [p_{it} y_{it}])$.

However, having measurement error only is unlikely to fully account for the low elasticity in Table 3. In the data, the variance of $\log(\mathbb{F}_{t-1}[p_{it}y_{it}])$ net of firm and year fixed-effects¹⁵ is about .083. As a result, measurement error as specified above would induce a downward bias of about $\frac{\sigma_{\zeta}^2}{.083}$. On the other hand, we also know that measurement errors are bounded by the variance of forecast errors, which is .03. Therefore, even if managers had perfect foresight and forecast errors only came from noise, the resulting downward bias would lead to an elasticity of $\approx 1 - \frac{.03}{.083} \approx .64$, which is still much larger than the elasticity in the data. This result explains why we also introduce quadratic adjustment costs to capital as another mechanism to lower the response of capital to sales forecasts.

3.4 Model Estimation

Table 6 reports the results of our structural estimation. Panel A shows the estimation results using only firms in manufacturing. Panel B shows the estimation results using all firms in the sample. Each panel reports the parameter estimates, as well as the empirical moments and their model counterparts.

We first discuss the parameter estimates. Since the results across the two samples are similar, we focus our discussion on Panel B, which uses all firms in the sample. We estimate γ at -.56. This coefficient estimate implies significant underreaction to the realization of productivity innovation ω_{it} when forecasting date $t + 1$ productivity. A rational manager's date t forecast for date $t + 1$ productivity is: $(1 - \rho)\nu_i + \rho\nu_{it} + \psi_{it-1}$. In the model, the manager instead forecasts $(1 - \rho)\nu_i + \rho(\nu_{it} + \gamma\omega_{it}) + \psi_{it-1}$. A γ of -.56 implies a weight of ω_{it} in date t forecast of about half that of a rational manager.

We also find that ω and ψ have approximately the same volatility (respectively 7.4% and 8.7%). In other words, about half of the variance of observed productivity innovations is driven by managerial private information (ψ). The remaining half comes from the true innovation ω . Overall, however, both shocks are relatively small: this is because the variance of TFP innovations in the data is itself limited ($\sigma_{\tau}^2 = .013$). This low volatility of ω limits the potential of mistakes due to forecasting biases. In the data, the variance of log-sales forecast errors is .03. The variance of log-sales forecast errors due to underreaction is $(\frac{\Phi}{\alpha\theta})^2 \gamma^2 \rho^2 \sigma_{\omega}^2 \approx .0036$ and therefore only accounts for about 12% of the total variance of log-sales forecast errors. Our estimation also reveals limited noise in the managerial sales forecast: in our estimation, σ_{ζ} accounts

¹⁵For obvious identification reasons, we include firm and year fixed-effects in the regressions in Table 3

only for 3% of the overall variance of log-sales forecast error. Overall, the variance of the rational forecast error represents about 85% of the total variance of log-sales forecast error.

Finally, the estimation uncovers significant adjustment costs to capital: $c_k \approx .35$. Relative to [Cooper and Haltiwanger \(2006\)](#), our estimate is larger: in their specification with only quadratic adjustment costs, they estimate a c_k of about .22 (see Table 4 in [Cooper and Haltiwanger \(2006\)](#), where their γ parameter corresponds to $2 \times c_k$). However, [Cooper and Haltiwanger \(2006\)](#) work with plant-level data, which typically exhibit a lower persistence of investment (in their dataset, the autocorrelation of investment at the plant-level is .058 relative to .483 in our sample). This is because investment at the plant level is lumpier.

Table 6 also compares the empirical moments targeted in the estimation with their model counterparts. The model manages to match all moments accurately except for the persistence of the productivity process: in the data, the persistence is estimated at .81 while the model needs a lower persistence of .68 to match all the other moments well. Apart from this persistence, the model can closely replicate three key moments of the data: (1) the persistence of log-sales forecast errors, which characterizes the degree of underreaction γ , (2) the variance of log-sales forecast errors, and (3) the relationship between changes in the capital stock and changes in sales forecast, which characterizes the link between observed forecasts in the data and real decisions by the firm. The model also matches closely the persistence in investment rates.

3.5 Partial equilibrium counterfactual

In this section, we use our structural estimates to quantitatively compare average corporate behavior for firms with rational managers (i.e. assuming $\gamma = 0$) relative to firms with managers that use distorted forecasts (i.e. assuming $\gamma = -.56$). To begin with, we do this in partial equilibrium, i.e. without clearing product and labor markets.

Investment conditional on TFP shocks

In Figure 4, we first consider the case of capital expenditures. We start by simulating a large dataset from the estimation obtained in Panel B of Table 6 (which uses the entire set of firms in the sample). We then simulate a second dataset with the same history of productivity shocks, but where managers are rational ($\gamma = 0$) instead of exhibiting underreaction. We then split each simulated sample into 20 vingitiles

of productivity innovations (ω_{it}) and report, for each of these bins, the average investment ratio $\left(\frac{k_{it+1}-(1-\delta)k_{it}}{k_{it}}\right)$ for firms with rational managers (grey stars) and firms with non-rational managers (dark circles). The role of underreaction is evident in Figure 4: managers with distorted forecasts clearly underinvest when the productivity innovation ω_{it} is large and overinvest when it is low. Quantitatively, this effect is sizeable. For a productivity shock at the 75th percentile of the distribution, the average manager in the data underinvests by 10.01 % relative to a rational expectation counterfactual. Symmetrically, for a productivity shock at the 25th percentile, the inattentive manager overinvests by 16.72 % relative to a rational manager.

Firm value conditional on TFP shocks

While the distortions on investment policy observed in Figure 4 appear economically significant, we find smaller effect on firm value. Figure 5 repeats the exercise in Figure 4, but computes average firm value instead of average investment ratios. As expected, for a given productivity innovation ω_{it} , the value of a firm with rational forecasts is strictly larger than the value of a firm whose manager exhibits distorted forecasts. However, this difference is quantitatively limited: on average, the value of the rational firm is only 0.65 % larger than the value of the firm with distorted forecasts. This finding remains similar whether or not we condition on the realized TFP innovation (ω_{it}).

A natural interpretation is that, in our setting, firms select their capital stock to optimize their value without any additional constraints. As a result, at the optimum, first-order deviations in investment only have second-order effects on firm value. This finding remains, of course, a quantitative result: larger distortions in forecasts (i.e. a smaller γ) or more volatile productivity innovations (a larger σ_ω) could well have resulted in large implications for firm value. However, given the estimated parameters, the effect is modest.

4 Aggregation

We nest the firm-level investment model of Section 3 into a general equilibrium framework. This allows us to explore the aggregate cost induced by managers' distorted forecasts.

4.1 Aggregation Setup

We consider a simple market structure following [Dixit and Stiglitz \(1977\)](#). There is a continuum of intermediate input producers: at date t , firm i is a monopolist and produces quantity y_{it} of an intermediary input at price p_{it} . These inputs are used in the production of a final good. The final good market is perfectly competitive, and aggregates intermediate inputs with a CES technology:

$$Y_t = \left(\int_i y_{it}^\theta di \right)^{\frac{1}{\theta}}. \quad (11)$$

The price of the final good is normalized to 1. Profit maximization in the final good market implies that the demand for product i is given by: $p_{it} = \left(\frac{Y_t}{y_{it}} \right)^{1-\theta}$, where Y_t represents the aggregate level of output. There is a single labor market from which all firms hire workers at the wage rate w_t , which firms take as given. Households have GHH preferences over leisure and consumption: $u(c_t, l_t) = \left(c_t - \frac{w_0}{L_0^\frac{1}{\epsilon}} \frac{l_t^{1+\frac{1}{\epsilon}}}{1+\frac{1}{\epsilon}} \right)$. As a result, labor supply is $L_0 \left(\frac{w_t}{w_0} \right)^\epsilon$ where ϵ is the constant labor supply elasticity.

The firm-level model of investment of [Section 3](#) can be nested into this framework. Assume firm i production combines labor and capital with a Cobb-Douglas technology: $y_{it} = B e^{z_{it}} k_{it}^\alpha l_{it}^{1-\alpha}$. Log-productivity z_{it} is stochastic and follows an AR(1) process:

$$z_{it} = \rho z_{it-1} + \epsilon_{it} + \eta_{it} \quad \text{with:} \quad (\epsilon_{it}, \eta_{it}) \sim \mathcal{N} \left[\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\epsilon^2 & 0 \\ 0 & \sigma_\eta^2 \end{pmatrix} \right],$$

where η_{it} is privately observed by the manager in period $t - 1$. In particular, we assume no aggregate uncertainty so that aggregate output is constant $Y_t = Y$ and the equilibrium wage on the labor market is also constant $w_t = w$. Given that input producers are monopolists, profit maximization with respect to pricing decisions (p_{it}) implies that firms' revenue exhibit decreasing returns to scale:

$$p_{it} y_{it} = \underbrace{Y^{1-\theta}}_{=A} \underbrace{e^{\theta z_{it}}}_{=e^{\nu_{it}}} (k_{it}^\alpha l_{it}^{1-\alpha})^\theta.$$

Therefore, this model is equivalent to the baseline firm-level model discussed in [Section 3](#): $A = Y^{1-\theta} B^\theta$, $\nu_{it} = \theta z_{it}$, $\omega_{it} = \theta \epsilon_{it}$ and $\psi_{it} = \theta \eta_{it}$.

Definition 1. An equilibrium in this economy is defined by a pair (w, Y) such that:

1. The labor market is in equilibrium: $L^s = L_0 \left(\frac{w}{w_0} \right)^\epsilon = \int_i l_{it} di = L^d$.

2. Total output is the sum of firm-level output: $Y = \int_i p_{it} y_{it} di$.

Given a general equilibrium, aggregate TFP in this economy admits a simple expression:

$$TFP = \frac{Y}{K^\alpha L^{1-\alpha}}.$$

4.2 Building Intuitions

Consider first the simplified setting of Section 3.3. There are no adjustment costs ($c_k = 0$) and no measurement error in sales forecast ($\sigma_\zeta = 0$). With these assumptions, it is straightforward to show that aggregate TFP depends solely on the variance of forecast errors:

$$\log(TFP) = -\frac{\alpha}{2} \left(1 + \frac{\alpha\theta}{1-\theta} \right) \text{Var}[FE_{it}] \quad (12)$$

Proof. See Appendix B.3. □

This formula for aggregate TFP is reminiscent of [Hsieh and Klenow \(2009\)](#). In this setting without adjustment costs, forecast errors made when investing are formally equivalent to a wedge between the user cost of capital and the marginal productivity of capital $\alpha\theta \frac{p_{it} y_{it}}{k_{it}}$. When the log-sales forecast error turns out to be positive, the firm's capital stock is too large relative to a completely frictionless benchmark where there is no information friction, i.e. one where the firm is rational and observes productivity when investing.

The productivity loss has two sources: the information friction (time to build) and the deviation from rationality. It follows directly from Equation (12) that, in this simple framework without adjustment costs, aggregate TFP losses due to distorted forecasts depend solely on the increase in the variance of the log-sales forecast errors due to the forecasting bias:

$$\log(TFP^{\text{rational}}) - \log(TFP^{\text{actual}}) = \frac{\alpha}{2} \left(1 + \frac{\alpha\theta}{1-\theta} \right) (\text{Var}[FE_{it}^{\text{actual}}] - \text{Var}[FE_{it}^{\text{rational}}]) \quad (13)$$

which is positive as the forecast error with bias has a bigger variance than the rational forecast error. This comes from the fact that rational forecasts have the lowest MSE.

In particular, this last expression provides a natural bound for TFP losses due to

distorted forecasts:

$$\begin{aligned} \log(TFP^{\text{rational}}) - \log(TFP^{\text{actual}}) &< \log(TFP^{\text{perfect foresight}}) - \log(TFP^{\text{actual}}) \\ &\leq \frac{\alpha}{2} \left(1 + \frac{\alpha\theta}{1-\theta}\right) \text{Var}[FE_{it}^{\text{actual}}] \end{aligned}$$

This bound is useful since it does not require the structural estimates in Table 6. Given a variance of log-sales forecast error of .03, and our calibration for α and θ , we see that, in this frictionless benchmark, TFP losses due to distorted forecasts can be at most $.38 \times .03 \approx 1.15\%$. Given the relatively low variance of log-sales forecast errors in the data, this frictionless benchmark already informs us about the limited scope that distorted forecasts may exert on aggregate efficiency. The structural estimation allows us to obtain a precise estimate.

4.3 TFP losses due to distorted forecasts

As we explained in Section 3.3, results in Table 3 reject the null hypothesis of no adjustment costs. As a result, aggregate efficiency losses due to the forecasting bias observed in the data need to be inferred from the model that includes quadratic adjustment costs to capital. Since this model does not admit closed-form solutions, we proceed numerically. In Appendix B.4, we show a simple methodology to compute the difference in aggregate log-TFP between the actual economy and the counterfactual economy with rational expectations. In a first step, we can calculate the average capital stock (K^*) and the average sales Y^* in an economy where $w = Y = 1$ and firms long-term productivity is 0 (for all i , $\nu_i = 0$): this is easily done by simulating the solution to the Bellman problem in Equation 8. In a second step, we can calculate the same quantities for an economy where again, $w = Y = 1$ and $\nu_i = 0$ for all firms, but where managers hold rational expectations: denote these quantities by (K_0^*, Y_0^*) . As we show in Appendix B.4, aggregate TFP losses due to distorted forecasts are then given by:

$$\log(TFP_0) - \log(TFP) = \alpha(\log(K^*) - \log(K_0^*)) + \frac{1 - (1 - \alpha)\theta}{\theta} (\log(Y_0^*) - \log(Y^*)) \quad (14)$$

Quantitatively, we find that TFP losses due to biases in managerial forecasts are:

$$\log(TFP^{\text{rational}}) - \log(TFP^{\text{actual}}) = 0.10\%$$

These TFP losses are an order of magnitude smaller than the partial equilibrium loss in value discussed in Section 3.5. Unsurprisingly, general equilibrium forces dampen the effect of forecasting biases observed in partial equilibrium. Quantitatively, these general equilibrium effects are large and lead us to conclude that the significant distortion on forecasting estimated in Table 6 have negligible implications for aggregate efficiency.

5 Alternative calibration for α and θ

In this section, we explore the robustness of our findings to alternative specification of α , the capital share in production, and θ , the price elasticity of demand. In our baseline estimation, α is set to .33 and θ is set to .8. We consider two sensitivity analyses. First, we set θ to .8, but let α vary from .2 to .5. Second, we set α to .33, but let θ vary from .6 to .9. For each alternative calibration, we re-estimate our model. Note that a different calibration for α and θ changes the model, but also the empirical moments related to TFP: an alternative calibration leads to a different set of TFP residuals, and therefore different estimates for $\hat{\chi}$, σ_τ and σ_V . Once the model are re-estimated, we compute the partial equilibrium value loss from distorted forecasts, in a similar fashion to what we did in Section 3.5. We also compute the general equilibrium TFP losses from distorted forecasts, as we did in Section 4.3.

We present the results graphically in Figure 6. The upper panel shows the partial equilibrium value losses for alternative calibration of α and θ . As expected, these value losses increase with α , the share in production of the distorted inputs, and θ , the decreasing returns to scale in revenues. However, we also see that the magnitudes of the estimated losses remain quantitatively similar to our baseline estimate. In our baseline estimate, we estimated value losses of 0.54 % and TFP losses of 0.08 %. When α is calibrated at .5 (large capital share), value losses are about 1% and TFP losses about .15%. When θ is calibrated at .9 (high degree of substitution across inputs in final good production), value losses are about 2% and TFP losses about .12%.

6 Optimism, Pessimism and Underreaction

Column (1) and (3) of Table 4 documents strong persistence in log-sales forecast errors. Our interpretation of this finding so far is that managers underreact to news about future TFP. However, this persistence could originate from a constant bias in

beliefs. Some managers may be over-optimistic, while others may be over-pessimistic (e.g., [Malmendier and Tate \(2005\)](#), [Landier and Thesmar \(2009\)](#) or [Ben-David et al. \(2013\)](#)). We entertain this possibility in Column (2) and (4) of Table 4. In these specifications, we control for firm fixed-effect. To avoid well-known biases in the estimation of persistence in the presence of individual fixed-effects and small T ([Nickell \(1981\)](#)), we restrict the sample to firms for which we observe at least 9 forecast errors and use dynamic panel GMM (e.g. [Arellano and Bover \(1995\)](#)). The estimated AR(1) coefficient for log-sales forecast error remains statistically significant, but its magnitude drop from about .3 to about .15. The estimation implies a volatility of fixed-effects in managerial forecast errors of 7.6%.

To estimate the economic magnitude of these findings, we augment the model introduced in Section 3 to allow for a pessimism / optimism bias. Precisely, we assume that firm i 's manager perceives her long-term productivity to be b_i , with $b_i \sim \mathcal{N}(0, \sigma_b^2)$ and b_i and \mathcal{V}_i are assumed to be independent. The manager therefore perceives the dynamics of ν to be:

$$\nu_{it} \stackrel{\mathbb{F}}{\sim} \mathcal{N} \left((1 - \rho) (\mathcal{V}_i + b_i) + \rho \nu_{it-1} + \psi_{it} + \underbrace{\gamma \rho \omega_{it-1}}_{\text{over/underreaction}}, \sigma_\omega^2 \right) \quad (15)$$

Introducing optimism / pessimism b_i is formally equivalent to increasing the firm's (perceived) long-term productivity by b_i . As a result, the value and optimal investment policy of a manager with a fixed bias b_i and long-term productivity \mathcal{V}_i derives directly from the value and investment policy of a firm with no bias ($b_i = 0$) and a long-term productivity of 0 ($\mathcal{V}_i = 0$). Let $k^*(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ be the optimal policy function in this case and $V(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ its optimal value. The optimal policy function $k^{i,*}(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1}))$ of a firm with long-term productivity \mathcal{V}_i and optimism / pessimism b_i can be expressed as:

$$k^{i,*}(k_{it}; (\nu_{it}, \omega_{it}, \psi_{it+1})) = e^{\frac{\mathcal{V}_i + b_i}{1-\theta}} \times k^* \left(\frac{k_{it}}{e^{\frac{\mathcal{V}_i + b_i}{1-\theta}}}; (\nu_{it} - (\mathcal{V}_i + b_i), \omega_{it}, \psi_{it+1}) \right) \quad (16)$$

We use this equation to simulate data from a model where firms may have long-term productivity $\mathcal{V}_i \sim \mathcal{N}(0, \sigma_{\mathcal{V}}^2)$ and fixed pessimism / optimism bias $b_i \sim \mathcal{N}(0, \sigma_b^2)$. Appendix B.5 shows precisely how to solve the model in this case.

We take the extended model to the data. Our estimation procedure is similar to the estimation described in Section 3.2, with two modifications. First, we use $\chi_{FE} = \frac{\text{Var}(FE_{it} - FE_{it-2})}{\text{Var}(FE_{it} - FE_{it-1})}$ to identify the persistence of log-sales forecast errors in the

presence of fixed belief biases. Second, we calculate \mathbb{V}_{FE} the variance of $\frac{FE_{it} - \widehat{\chi_{\text{FE}}} FE_{it-1}}{1 - \widehat{\chi_{\text{FE}}}}$ to identify the variance of the belief fixed-effects b_i . We match these two moments, as well the other six moments described in Section 3.2. Given the estimated parameters, Appendix B.5 also shows how to compute aggregate TFP in this economy. Aggregate TFP losses from distorted forecasts are then simply calculated by comparing aggregate TFP in this economy with aggregate TFP in an economy with $\gamma = \sigma_b = 0$.

Table 7 presents the results. The estimated structural parameters are mostly similar to the ones estimated in Table 6, with one exception: the estimated γ is now -.29 as opposed to -.56 in Panel B of Table 6. This result is not surprising: the estimated persistence in forecast errors is smaller when we allow for firm fixed-effects (Table 4) so that the model naturally finds less under-reaction. However, the smaller estimated value for γ implies a large and significant dispersion for the variance of b_i , the pessimism/optimism bias that managers exhibit: the estimate for σ_b is .049, which implies that about 10% of the variance in forecast errors can be attributed to fixed optimism/pessimism bias.

The last line in Table 7 reports the TFP losses due to distortions in forecast in this economy. We find that, relative to a rational expectation counterfactual ($\sigma_b = 0 = \gamma$), TFP in the actual economy is lower by .14%. This aggregate efficiency loss is close to what we report in Table 6, Panel B (0.10 %): on the one hand, in this economy with optimism/pessimism bias, managers exhibit under-react less to news about TFP, which reduces the potential efficiency gains of rational expectations; on the other hand, the existence of fixed biases in beliefs increase the distortions generated by non-rational expectations. Overall, the potential aggregate TFP gains in this economy have the same order of magnitude than in the economy where all the belief distortions emanate from under-reaction.

7 Conclusion

This paper leverages unique survey data on managerial forecasts to explore the real consequences of biases in managerial beliefs. We make three contributions. First, we document pervasive and significant persistence in managerial forecast errors, consistent with managerial inattention. Second, we estimate a quantitative model of firm dynamics that accounts jointly for: (1) the dynamics of beliefs, and in particular, the variance and persistence of forecast errors (2) the dynamics of productivity (3) the link between investment and beliefs. The estimated model implies large deviations from rational expectations and significant distortions in firm-level investment. How-

ever, the effect on firm value is limited. Finally, we nest this model in a standard general equilibrium framework to assess the contribution of distortions in managerial forecasts to aggregate inefficiency. Our quantitative analysis implies negligible aggregate losses, despite significant distortions in firm-level forecasts.

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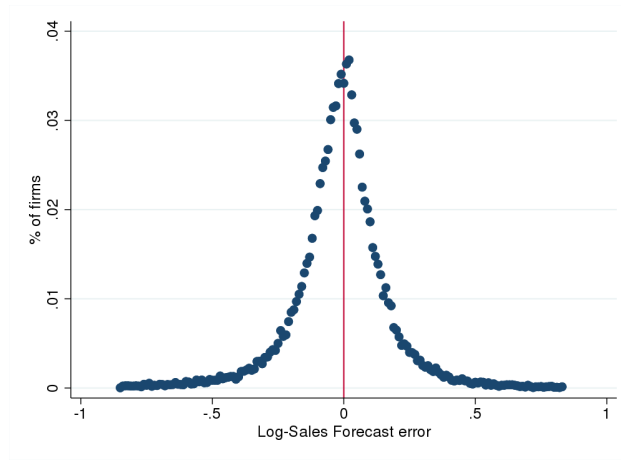
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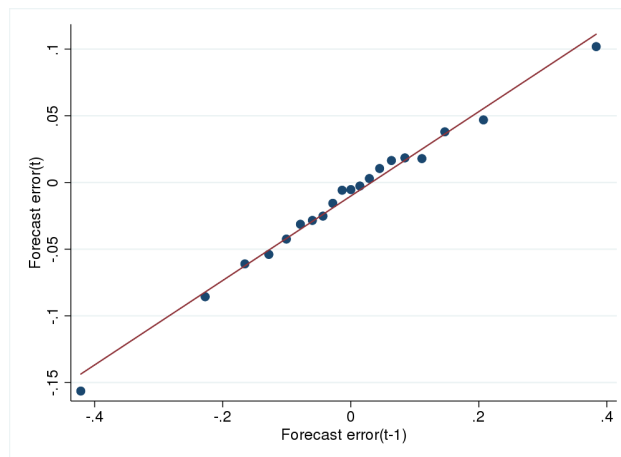
FIGURES

Figure 1: Forecast Errors: Histogram



Note: This figure plots the distribution of log-sales forecast errors. The log-sales forecast error is computed as the difference between realized sales in fiscal year t and sales forecast for year t issued at the beginning of year t .

Figure 2: Forecast Error Persistence: Binned Scatter Plot



Note: This figure is a binscatter plot of year t log-sales forecast error on year $t - 1$ log-sales forecast error.

Figure 3: Numerical Comparative statics

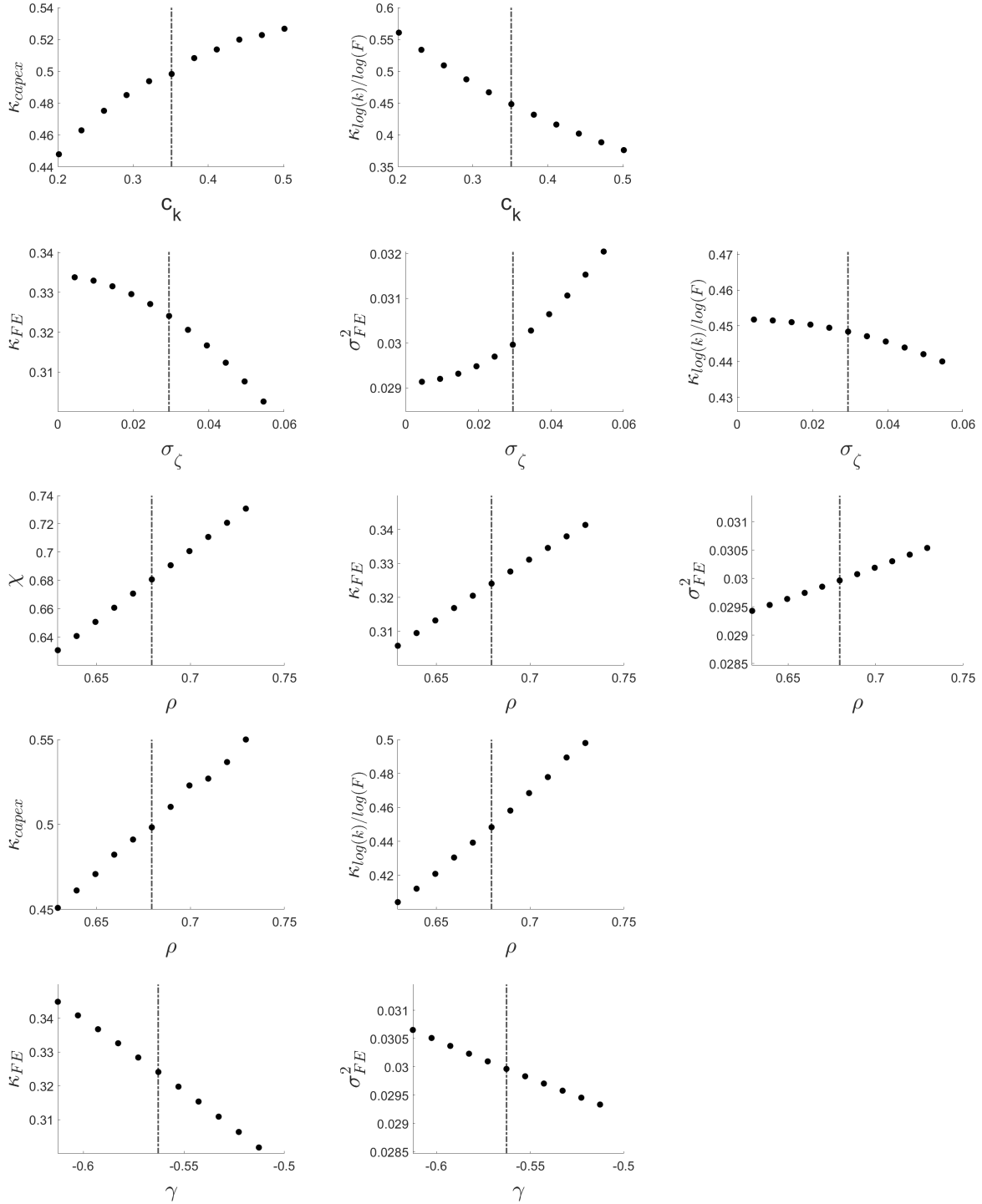
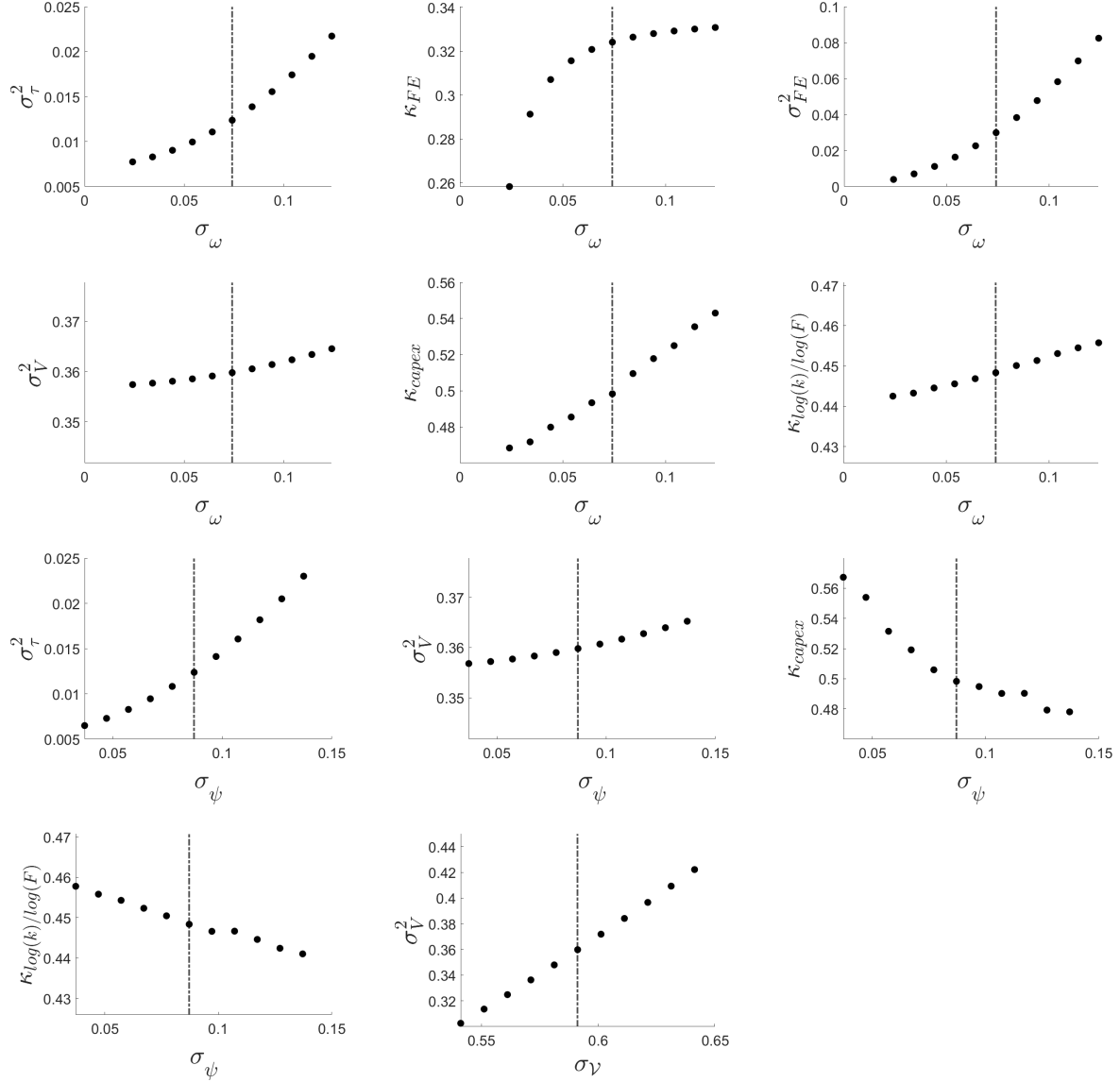
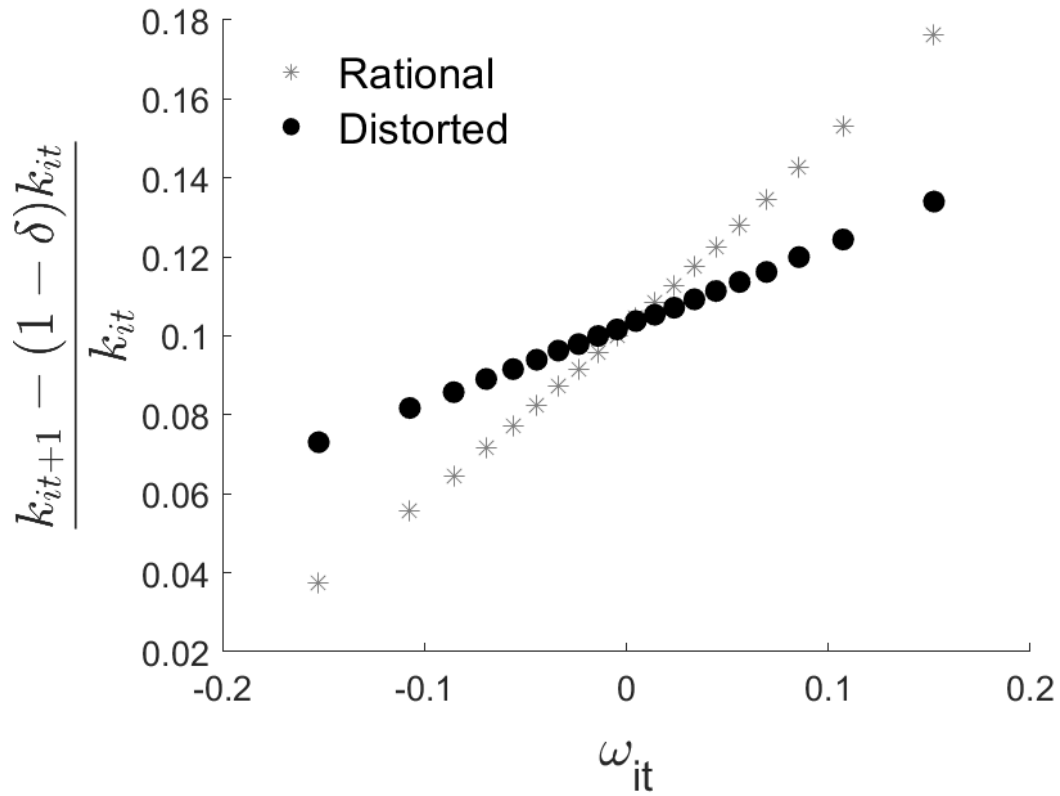


Figure 3: Numerical Comparative statics (continued)



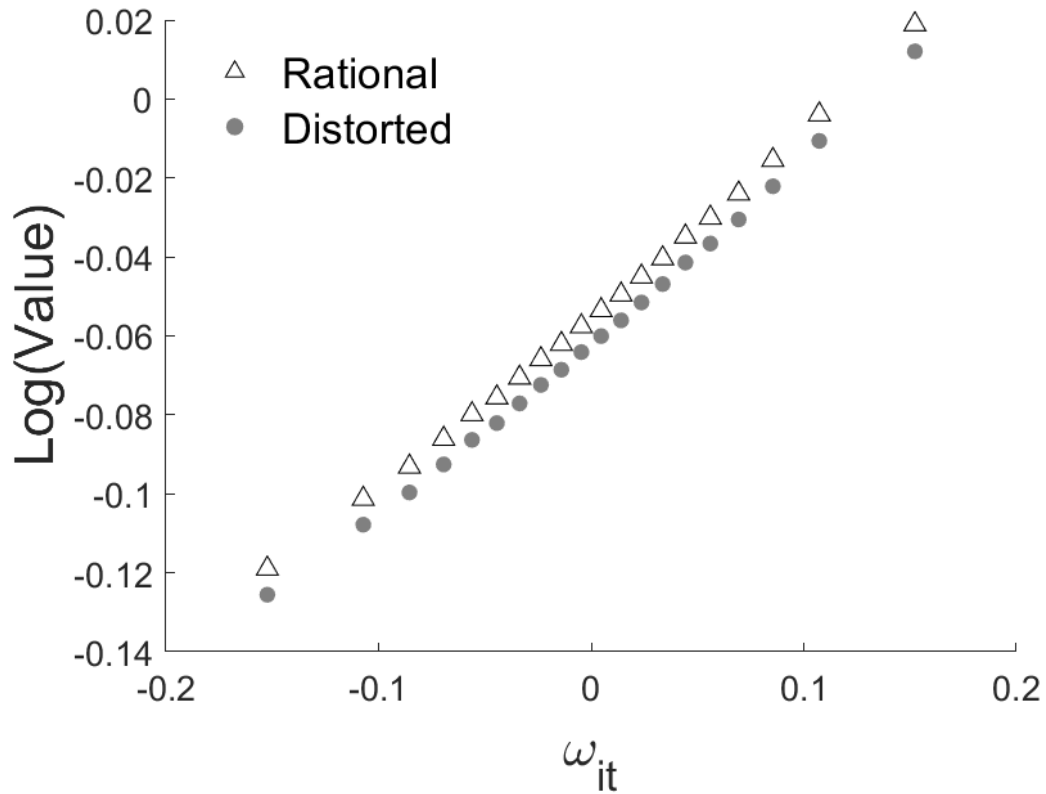
Note: This table provides numerical comparative statics for our simulated model. For each of the seven estimated parameters ($c_k, \sigma_\zeta, \rho, \gamma, \sigma_\omega, \sigma_\psi, \sigma_\gamma^2$), we compute the seven simulated moments ($\chi, \sigma_T^2, \kappa_{FFE}, \sigma_{FFE}^2, \sigma_V^2, \kappa_{capex}, \kappa_{\log(k)/\log(\mathbb{F})}$) for values of the parameters in the neighborhood of their estimated values (vertical dashed line). We report only the parameter-moment pair for which variations in the parameter lead to non-zero variations in simulated moments.

Figure 4: Firm Investment with Rational vs. Distorted Forecasts



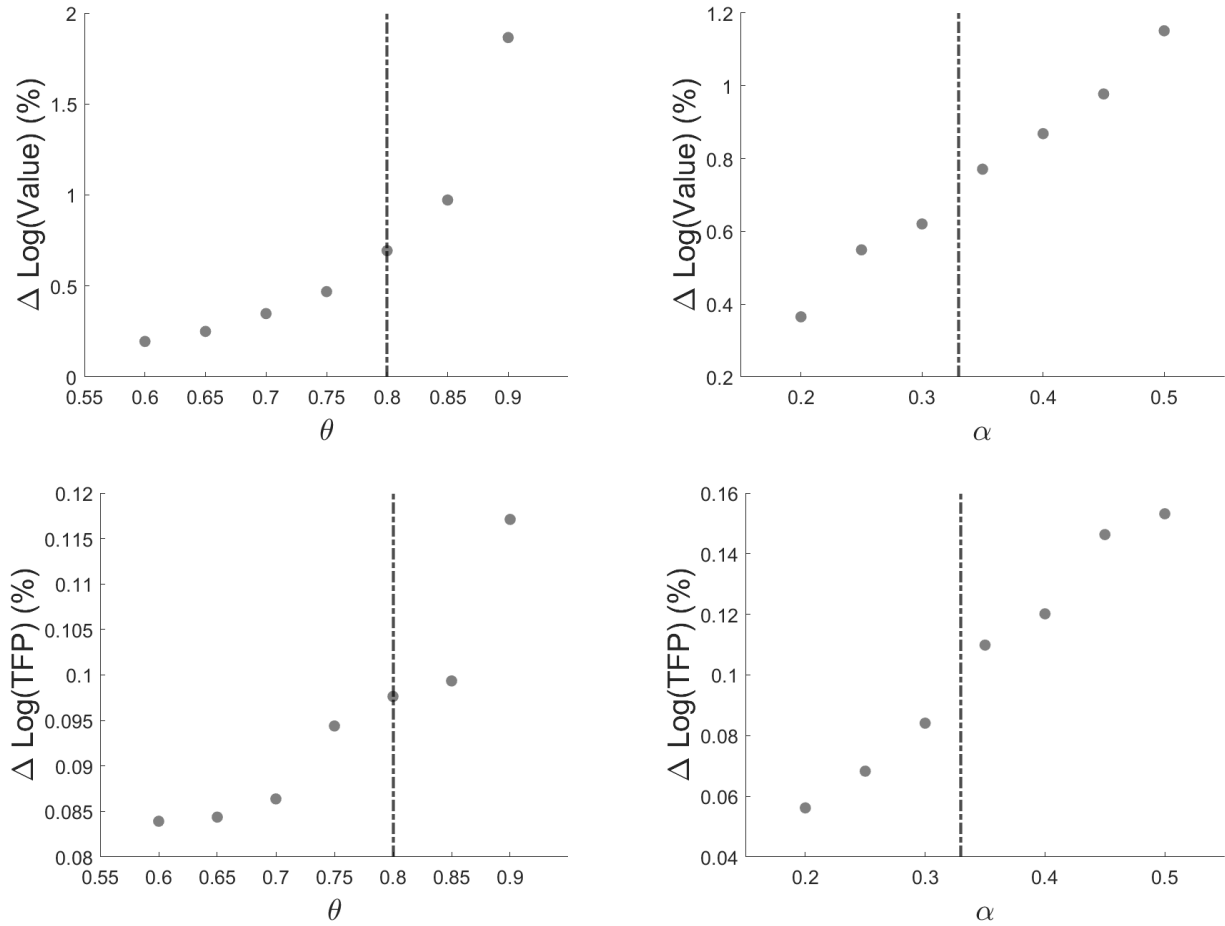
Note: This figure uses the estimation of Table 6 to simulate investment for managers using rational forecast (grey stars) or distorted forecasts (dark circles). We construct 20 vingtiles of date t TFP innovations (ω_{it}) and compute, for each of these bins, the average investment ratio for both managers with rational forecasts ($\gamma = 0$) and managers with distorted forecasts (γ set at its estimated value).

Figure 5: Firm Value with Rational vs. Distorted forecasts



Note: This figure uses the estimation of Table 6 to simulate firm value for managers using distorted forecasts (γ at its estimated value) relative to managers using rational forecasts ($\gamma = 0$). We construct 20 vingtiles of date t TFP innovations (ω_{it}) and compute, for each of these bins, the average firm value of rational managers (white triangles) and managers with distorted forecasts (grey circles).

Figure 6: TFP losses and Value Losses with alternative calibration



Note: the top panel computes value losses from distorted managerial forecasts for alternative calibration of α and θ . The methodology to compute these losses is described in Section 3.5. The bottom panel computes aggregate TFP losses from distorted managerial forecasts for alternative calibration of α and θ . The methodology to compute these losses is described in Section 4.3.

TABLES

Table 1: Summary Statistics

Variable	mean	p25	p50	p75	sd	<i>N</i>
Panel A. Italian merged survey and accounts						
Firm forecast error (log actual sales(<i>t</i>) - log forecast(<i>t</i> — <i>t</i> -1))	-0.01	-0.09	-0.01	0.07	0.18	39,721
Log sales	10.07	8.95	9.88	11.04	1.57	39,721
Log assets	10.12	9.02	9.91	11.06	1.58	39,721
Sales/l.assets	1.14	0.71	1.02	1.42	0.66	39,285
Capex/l.assets	0.03	0.01	0.02	0.04	0.04	38,640
Cash flow/l.assets	0.07	0.03	0.06	0.10	0.07	38,791
Panel B. Italian accounting data						
Log sales	6.16	5.00	6.20	7.36	1.90	7,350,380
Log assets	6.09	4.93	6.10	7.28	1.86	8,261,704
Sales/l.assets	1.24	0.34	1.00	1.73	1.21	8,164,493
Capex/l.assets	0.02	0.00	0.01	0.03	0.03	7,650,925
Cash flow/l.assets	0.05	0.00	0.04	0.10	0.12	7,953,679

Note: Summary statistics. Panel A focuses on Italian firms for which sales forecasts were available from the Bank of Italy. Panel B produces the same descriptive statistics for the universe of Italian firms present in the Company Accounts Data System. Firm forecast error is the log difference between actual sales of fiscal year *t* and sales forecast at the beginning of year *t*. All variables are winsorized at the median +/- 5 times the interquartile range.

Table 2: Predicting Actual Sales

	log($Sales_{it}$)				$Sales_{it}/Assets_{i,t-1}$			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
log($F_{i,t-1}(Sales_{it})$)	0.999*** (0.001)	0.839*** (0.015)	0.558*** (0.039)	0.534*** (0.030)				
log($Sales_{it-1}$)			0.443*** (0.040)	0.467*** (0.030)				
$F_{i,t-1} \left[\frac{Sales_{it}}{Assets_{i,t-1}} \right]$					0.972*** (0.007)	0.801*** (0.014)	0.826*** (0.016)	0.821*** (0.016)
log($Sales_{it-1}$)							0.170*** (0.017)	0.176*** (0.017)
log($Assets_{it-1}$)							-0.168*** (0.017)	-0.174*** (0.016)
Fixed effects	Year	Year & Firm	Year & Industry	Year×Industry	Year	Year & Firm	Year & Industry	Year×Industry
Observations	39,721	39,667	39,466	39,320	39,208	39,152	39,206	39,058
Adj R ²	0.99	0.99	0.99	0.99	0.90	0.92	0.91	0.91

Note: This table presents the estimation results of regressions $\log(Sales_{it}) = \alpha + \log(F_{i,t-1}Sales_{it}) + controls_{i,t-1} + \epsilon_{it}$ and $Sales_{it}/Assets_{i,t-1} = \alpha + F_{i,t-1} [Sales_{it}/Assets_{i,t-1}] + controls_{i,t-1} + \epsilon_{it}$, where $Sales_{it}$ is sales of firm i in fiscal year t , $F_{i,t-1}Sales_{it}$ is beginning-of-year forecast of fiscal year t sales and $Assets_{i,t-1}$ is beginning-of-year of fiscal year t assets. Industry dummies are 2-digit industry dummies in Italian data. Standard errors are double-clustered by firm and year. ***, ** and * means statistically significant at the 1%, 5% and 10% confidence level.

Table 3: Sales Forecasts and Capital Investment

	Log k_{it}	
	Manufacturing Only (1)	All Firms (2)
$\log(F_{t-1}(Sales_{it}))$	0.366*** (0.034)	0.410*** (0.034)
Fixed effects	Firm & Year	Firm & Year
Observations	24,891	36,996
Adj R ²	0.92	0.93

Note: This table presents estimates of the following linear model: $\log k_{it} = \alpha_i + \delta_t + \kappa_{\log(k)/\log(\mathbb{F})} \log F_{i,t-1} sales_{it} + \epsilon_{it}$. The dependent variable $\log k_{it}$ is the log of capital (net tangible fixed assets) at the end of year $t-1$ while $\log F_{i,t-1} sales_{it}$ is the log of beginning-of-year forecast of fiscal year t sales. Column (1) estimates $\kappa_{\log(k)/\log(\mathbb{F})}$ on the sample of manufacturing firms. Column (2) estimates $\kappa_{\log(k)/\log(\mathbb{F})}$ for all firms in the sample. Standard errors are double-clustered by firm and year. ***, ** and * means statistically significant at the 1%, 5% and 10% confidence level.

Table 4: Persistence of Forecast Errors

	Log-sales forecast error (\widehat{FE}_{it})			
	Manufacturing (1)	(2)	All firms (3)	(4)
\widehat{FE}_{it-1}	0.289*** (0.021)	0.159*** (0.015)	0.321*** (0.017)	0.176*** (0.014)
Year FE	Yes	Yes	Yes	Yes
Firm FE	No	Yes	No	Yes
Observations	23,458	14,255	34,001	19,744
Adj R ²	0.11		0.12	

Note: This table presents estimation results for the following linear regression model: $\widehat{FE}_{it} = \delta_t + \kappa_{FE}\widehat{FE}_{it-1} + \epsilon_{it}$, where \widehat{FE}_{it} is the log-sales forecast error (log actual sales minus log sales forecast made in first quarter of fiscal year t). Columns (1) and (3) only includes year fixed-effects. Columns (2) and (4) add firm fixed-effects, and are estimated using dynamic panel GMM (Arellano and Bover (1995)) on the sample of firms with at least 9 sales forecasts. Standard errors are double clustered by firm and year. ***, ** and * means statistically significant at the 1%, 5% and 10% confidence level.

Table 5: Persistence of Forecast Errors: by Firm Size

	Forecast error			
	Manufacturing (1)	(2)	All firms (3)	(4)
Panel A: Firms with 20-49 employees				
Forecast error(t-1)	0.265*** (0.031)	0.133*** (0.026)	0.284*** (0.025)	0.142*** (0.022)
Observations	7,526	3,973	11,030	5,718
Adj R ²	0.09		0.09	
Panel B: Firms with 50-99 employees				
Forecast error(t-1)	0.296*** (0.029)	0.136*** (0.026)	0.308*** (0.025)	0.162*** (0.027)
Observations	5,320	3,270	7,397	4,339
Adj R ²	0.11		0.12	
Panel C: Firms with 100-199 employees				
Forecast error(t-1)	0.312*** (0.024)	0.199*** (0.035)	0.336*** (0.024)	0.207*** (0.034)
Observations	4,440	2,953	6,071	3,738
Adj R ²	0.14		0.14	
Panel D: Firms with 200-500 employees				
Forecast error(t-1)	0.303*** (0.029)	0.176*** (0.040)	0.356*** (0.028)	0.200*** (0.034)
Observations	3,605	2,265	5,227	3,179
Adj R ²	0.14		0.16	
Panel E: Firms with 501- employees				
Forecast error(t-1)	0.312*** (0.069)	0.121*** (0.036)	0.407*** (0.047)	0.187*** (0.043)
Observations	2,567	1,794	4,276	2,770
Adj R ²	0.15		0.19	
Firm FE	No	Yes	No	Yes
Year FE	Yes	Yes	Yes	Yes

Note: This table presents estimation results for the following linear regression model: $\widehat{FE}_{it} = \delta_t + \gamma \widehat{FE}_{it-1} + \epsilon_{it}$. Columns (1), (3) only includes year fixed-effects. Columns (2), (4) add firm fixed-effects, and are estimated using dynamic panel GMM (Arellano and Bover (1995)) on the sample of firms with at least 9 sales forecasts. Standard errors are double clustered by firm and year. Panel A (resp. B, C, D, and E) estimates the model using only firms with 20-49 employees (resp. 50-99, 100-199, 200-500, and more than 500). ***, ** and * means statistically significant at the 1%, 5% and 10% confidence levels.

Table 6: Structural Estimation: baseline estimate

Panel A: Manufacturing firms							
<u>Estimates:</u>							
	c_k	σ_ζ	ρ	γ	σ_ω	σ_ψ	σ_ν
	0.387	0.031	0.649	-0.509	0.077	0.091	0.515
	(0.037)	(0.110)	(0.025)	(0.149)	(0.012)	(0.010)	(0.020)
<u>Moments:</u>							
	χ	σ_τ^2	κ_{FE}	σ_{FE}^2	σ_V^2	κ_{capex}	$\kappa_{\log(k)/\log(\mathbb{F})}$
Data	0.762	0.013	0.289	0.031	0.275	0.461	0.366
Model	0.650	0.013	0.289	0.031	0.284	0.476	0.400
Difference	0.112	-0.000	-0.000	0.000	-0.009	-0.015	-0.034
<u>Implied TFP loss:</u>	0.08 %						
Panel B: All firms							
<u>Estimates:</u>							
	c_k	σ_ζ	ρ	γ	σ_ω	σ_ψ	σ_ν
	0.351	0.029	0.679	-0.563	0.074	0.087	0.591
	(0.025)	(0.062)	(0.021)	(0.096)	(0.007)	(0.006)	(0.027)
<u>Moments:</u>							
	χ	σ_τ^2	κ_{FE}	σ_{FE}^2	σ_V^2	κ_{capex}	$\kappa_{\log(k)/\log(\mathbb{F})}$
Data	0.812	0.012	0.321	0.030	0.358	0.483	0.410
Model	0.681	0.012	0.324	0.030	0.372	0.498	0.448
Difference	0.131	-0.000	-0.003	0.000	-0.014	-0.016	-0.038
<u>Implied TFP loss:</u>	0.10 %						

Note: Panel A focuses on firms in the manufacturing sector; Panel B uses all firms in the sample. χ is defined as $\frac{\text{Var}(\hat{\nu}_{it} - \hat{\nu}_{it-2})}{\text{Var}(\hat{\nu}_{it} - \hat{\nu}_{it-1})} - 1$, where $\hat{\nu}_{it}$ is the TFP residual for firm i in year t . σ_V^2 is defined as $\text{Var}_i(\mathbb{V}_i)$, where $\mathbb{V}_i = \frac{1}{T} \sum_{t=1}^T \frac{\hat{\nu}_{it} - \hat{\chi}\hat{\nu}_{it-1}}{1 - \hat{\chi}}$. σ_τ^2 is defined as $\text{Var}(\hat{\nu}_{it} - \hat{\chi}\hat{\nu}_{it-1} - (1 - \hat{\chi})\mathbb{V}_i)$. κ_{FE} is the persistence in log-sales forecast error estimated in Column (1) and (3) of Table 4. σ_{FE}^2 corresponds to the variance of log-sales forecast errors net of year fixed-effects. κ_{capex} corresponds to the autocorrelation coefficient of investment ratios and is estimated using Equation (10). $\kappa_{\log(k)/\log(\mathbb{F})}$ corresponds to the elasticity of capital to sales forecast with firm fixed-effects and is estimated in Table 3. Standard errors are computed with the delta method, where we use the inverse of the covariance matrix of empirical moments, clustered at the firm-level, as a weighting matrix.

Table 7: Structural Estimation: including optimism/pessimism bias

<u>Estimates:</u>								
	c_k	σ_ζ	ρ	γ	σ_ω	σ_ψ	σ_ν	σ_b
	0.366	0.030	0.697	-0.293	0.060	0.097	0.582	0.049
	(0.025)	(0.124)	(0.022)	(0.141)	(0.015)	(0.010)	(0.026)	(0.001)
<u>Moments:</u>								
	χ	σ_τ^2	χ_{FE}	σ_{FE}^2	σ_V^2	κ_{capex}	$\kappa_{\log(k)/\log(\mathbb{F})}$	\mathbb{V}_{FE}
Data	0.812	0.012	0.230	0.030	0.358	0.483	0.410	0.013
Model	0.697	0.012	0.229	0.035	0.359	0.496	0.450	0.018
Difference	0.115	-0.000	0.001	-0.005	-0.001	-0.014	-0.040	-0.005
<u>Implied TFP loss:</u>	0.14 %							

Note: The estimation uses all firms in the sample. χ is defined as $\frac{\text{Var}(\hat{\nu}_{it}-\hat{\nu}_{it-2})}{\text{Var}(\hat{\nu}_{it}-\hat{\nu}_{it-1})} - 1$, where $\hat{\nu}_{it}$ is the TFP residual for firm i in year t . σ_V^2 is defined as $\text{Var}_i(\mathbb{V}_i)$, where $\mathbb{V}_i = \frac{1}{T} \sum_{t=1}^T \frac{\hat{\nu}_{it}-\hat{\chi}\hat{\nu}_{it-1}}{1-\hat{\chi}}$. σ_τ^2 is defined as $\text{Var}(\hat{\nu}_{it}-\hat{\chi}\hat{\nu}_{it-1} - (1-\hat{\chi})\mathbb{V}_i)$. χ_{FE} is defined as $\frac{\text{Var}(FE_{it}-FE_{it-2})}{\text{Var}(FE_{it}-FE_{it-1})}$, where FE_{it} is the log-sales forecast error of firm i in year t . \mathbb{V}_{FE} is the empirical variance of $\frac{FE_{it}-\hat{\chi}_{FE}FE_{it-1}}{1-\hat{\chi}_{FE}}$. $\sigma_F E^2$ corresponds to the variance of log-sales forecast errors net of year fixed-effects. κ_{capex} corresponds to the autocorrelation coefficient of investment ratios and is estimated using Equation (10). $\kappa_{\log(k)/\log(\mathbb{F})}$ corresponds to the elasticity of capital to sales forecast with firm fixed-effects and is estimated in Table 3. Standard error are computed with the delta method, where we use the inverse of the covariance matrix of empirical moments, clustered at the firm-level, as a weighting matrix.

APPENDIX: FOR ONLINE PUBLICATION

A Additional Results

A.1 Description of the Guidance dataset

To investigate forecast error in US data, we exploit data on firms' expectations from the IBES Guidance dataset, a feed that offers quantitative (numeric) company expectations from press releases and transcripts of corporate events. We focus on forecasts of fiscal year total sales, which is one of the most common forecast. The forecast horizon ranges 1 quarter out (current quarter corresponds to the fiscal year end quarter) to about 30 quarters out; forecast horizon longer than 12 quarters is rare. For consistency, we restrict the sample to forecasts made in the first fiscal quarter about total sales of that fiscal year. Comprehensive data coverage starts from 2003 onward. Since we are interested in the persistence of forecast errors, we also restrict the sample to firms that issue at least 5 guidance over the sample period.

We focus on US non-financial firms (SIC outside of 6000 to 6999). The final sample – which we will refer to as the guidance sample – contains 5,222 firm-year observations, corresponding to about 440 firms per year. All variables are trimmed at the median +/- 5 times the interquartile range.¹⁶ To compare these forecast with realizations, we merge this sample with Compustat.

Appendix Table 1 Panel A provides basic summary statistics for firms in the guidance sample. Panel B reports statistics for firms in the contemporaneous full Compustat sample. The average firm in the guidance sample is larger and more profitable than the average firm in the Compustat sample. Panel A also contains summary statistics on the forecast errors from guidance. We compute log-sales forecast errors as the logarithm of actual sales minus the logarithm of forecast sales provided in the guidance. Average log-sales forecast errors in the guidance are .3% and have a 9% standard deviation (Panel A, Table 1).

¹⁶If we only trim at the 1% level, some observations still have log-sales forecast errors greater than 50% in absolute value. These observations mostly correspond to firms experiencing a significant corporate event, such as a merger. These large forecast errors should therefore not be attributed to managerial forecasting bias.

A.2 Additional Table

Table IAI: Summary Statistics

Variable	mean	p25	p50	p75	sd	<i>N</i>
Panel A. Guidance Sample						
Firm forecast error (log actual sales - log forecast)	0.00	-0.03	0.00	0.05	0.09	6,597
Log sales	7.16	5.99	7.11	8.28	1.68	6,597
Log assets	7.27	6.03	7.21	8.38	1.65	6,597
Q	2.18	1.34	1.81	2.61	1.21	6,490
Panel B. Compustat Sample						
Log sales	4.86	3.12	5.25	7.05	3.06	56,287
Log assets	4.86	3.07	5.10	7.08	3.12	61,714
Q	1.90	1.13	1.49	2.24	1.21	38,438

Note: Summary statistics of the guidance sample and the contemporaneous full Compustat sample. Sample period: 2004-2015. Both sample are restricted to firms outside the finance industry. The guidance sample is restricted to firms that have at least 5 guidance issued over the sample period. Firm forecast data are from IBES Guidance dataset. The forecasts are restricted to those made at the beginning of the first fiscal quarter, and the outcome is total sales of fiscal year. Firm forecast error is the logarithm of actual sales for the fiscal year minus the log of the guidance issued in the first quarter for the coming fiscal year. Q is the ratio of market value to total assets. All variables are trimmed at the median +/- 5 times the interquartile range.

Table IAI: Additional Evidence on Managerial Underreaction

	Dependent Variable: $\log(\text{Sales}_{i,t+1}) - \log(\mathbb{F}_{i,t}\text{Sales}_{it+1})$				
	(1)	(2)	(3)	(4)	(5)
Panel A: Barrero (2020)'s specification					
$\log(\text{Sales}_{i,t}) - \log(\text{Sales}_{it-1})$	0.104*** (0.031)	0.122*** (0.020)	0.099*** (0.033)	0.120*** (0.015)	0.087*** (0.025)
Fixed effects	None	Year	Industry	Industry & Year	Firm & Year
Observations	31,224	31,224	31,223	31,090	31,142
Adj. R ²	0.01	0.04	0.02	0.07	
Panel B: US Guidance Data					
$\log(\text{Sales}_{it}) - \log(\mathbb{F}_{t-1}(\text{Sales}_{it}))$	0.176*** (0.041)	0.186*** (0.032)	0.161*** (0.039)	0.170*** (0.030)	0.093*** (0.029)
Observations	5,331	5,331	5,331	5,331	2,929
Adj R ²	0.03	0.08	0.04	0.09	

Note: Panel A uses our main sample of Italian firms from the INVIND survey (Table 4). The dependent variable is the date t+1 log-sales forecast error ($\log(\text{Sales}_{i,t+1}) - \log(\mathbb{F}_{i,t}\text{Sales}_{it+1})$), which is equal to the forecast error for log-growth sales. The explanatory variable is realized log-growth sales in t ($\log(\text{Sales}_{i,t}) - \log(\text{Sales}_{it-1})$). Column (1) has no fixed effect. Column (2) includes year fixed-effects, column (3) industry fixed-effects, column (4) industry and year fixed effects and column (5) firm and year fixed-effects. Column (5) is estimated using dynamic panel GMM (Arellano and Bover (1995)) on the sample of firms with at least 9 sales forecasts. Standard errors are double clustered by firm and year.

Panel B uses the sample of managerial guidance for US public firms. The sample is described in Appendix A.1. The dependent variable is the date t+1 log-sales forecast error ($\log(\text{Sales}_{i,t+1}) - \log(\mathbb{F}_{i,t}\text{Sales}_{it+1})$). The explanatory variable is the date t log-sales forecast error. The fixed-effects are similar to Panel A. Column (5) is estimated using dynamic panel GMM (Arellano and Bover (1995)) on the sample of firms with at least 9 sales forecasts. Standard errors are double clustered by firm and year. ***, ** and * means statistically significant at the 1%, 5% and 10% confidence level.

B Proofs

B.1 Proof for optimal investment decision

To simplify notations, we drop the (i,t) subscripts and simply use prime superscript for next period variables. The Bellman problem of a firm with a long term productivity of 0 admits the following representation:

$$(17) \quad V(k; \nu, \omega, \psi') = \max_{k'} \left\{ \Omega e^{\frac{\phi}{\alpha\theta}} \nu k^\phi - (k' - (1 - \delta)k) - c_k \frac{(k' - (1 - \delta)k)^2}{k} + \frac{1}{1 + r} \mathbb{E} [V(k'; \nu', \omega', \psi'') | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N} \left(\begin{pmatrix} \rho\nu + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix} \right) \quad \text{and:} \quad \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

Let $k^*(k; \nu, \omega, \psi')$ be the optimal policy and $V_*(k; \nu, \omega, \psi')$ the resulting value.

Consider now the Bellman problem for a firm with a persistent component \mathcal{V}_i in productivity:

$$z' = (1 - \rho)\mathcal{V}_i + \rho z + \omega' + \psi'$$

Let V^i be the bellman value for this firm. This value admits the following representation:

$$(18) \quad V^i(k; z, \omega, \psi') = \max_{k'} \left\{ \Omega e^{\frac{\phi}{\alpha\theta}} z k^\phi - (k' - (1 - \delta)k) - c_k \frac{(k' - (1 - \delta)k)^2}{k} + \frac{1}{1 + r} \mathbb{E} [V^i(k'; z', \omega', \psi'') | (z, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} z' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N} \left(\begin{pmatrix} (1 - \rho)\mathcal{V}_i + \rho z + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix} \right) \quad \text{and:} \quad \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

Define $\nu = z - \mathcal{V}_i$. We can rewrite the Bellman problem for firm i as a function of ν instead of z :

$$(19) \quad V^i(k; \nu + \mathcal{V}_i, \omega, \psi') = \max_{k'} \left\{ \Omega e^{\frac{\phi}{\alpha\theta}} (\nu + \mathcal{V}_i) k^\phi - (k' - (1 - \delta)k) - c_k \frac{(k' - (1 - \delta)k)^2}{k} + \frac{1}{1 + r} \mathbb{E} [V^i(k'; \nu' + \mathcal{V}_i, \omega', \psi'') | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N} \left(\begin{pmatrix} \rho\nu + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix} \right) \quad \text{and:} \quad \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

We can rewrite this previous problem in a simpler fashion:

$$V^i(k; \nu + \mathcal{V}_i, \omega, \psi') = \max_{k'} \left\{ e^{\frac{\nu_i}{1-\theta}} \left(\Omega e^{\frac{\phi}{\alpha\theta}} \nu \left(\frac{k}{e^{\frac{\nu_i}{1-\theta}}} \right)^\phi - \left(\left(\frac{k'}{e^{\frac{\nu_i}{1-\theta}}} \right) - (1 - \delta) \left(\frac{k}{e^{\frac{\nu_i}{1-\theta}}} \right) \right) - c_k \frac{\left(\left(\frac{k'}{e^{\frac{\nu_i}{1-\theta}}} \right) - (1 - \delta) \left(\frac{k}{e^{\frac{\nu_i}{1-\theta}}} \right) \right)^2}{\left(\frac{k}{e^{\frac{\nu_i}{1-\theta}}} \right)} \right) + \frac{1}{1 + r} \mathbb{E} [V^i(k'; \nu' + \mathcal{V}_i, \omega', \psi'') | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} \rho\nu + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\psi^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

This last representation is equivalent to:

$$\begin{aligned} \left(\frac{V^i(k; \nu + \mathcal{V}_i, \omega, \psi')}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right) &= \max_{k'} \left\{ \left(\Omega e^{\frac{\Phi}{\alpha\theta}} \nu \left(\frac{k}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right)^\phi - \left(\left(\frac{k'}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right) - (1-\delta) \left(\frac{k}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right) \right) \right. \right. \\ &\quad \left. \left. - c_k \frac{\left(\left(\frac{k'}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right) - (1-\delta) \left(\frac{k}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right) \right)^2}{\left(\frac{k}{e^{\frac{\mathcal{V}_i}{1-\theta}}}\right)} \right) + \frac{1}{1+r} \mathbb{F} \left[\left(\frac{V^i(k'; \nu' + \mathcal{V}_i, \omega', \psi'')}{e^{\frac{\mathcal{V}_i}{1-\theta}}} \right) | (\nu, \omega, \psi') \right] \right\} \end{aligned}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} \rho\nu + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\psi^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

It is clear from the previous equation that:

$$V_*^i(k; \nu + \mathcal{V}_i, \omega, \psi') = e^{\frac{\mathcal{V}_i}{1-\theta}} \times V_*\left(\frac{k}{e^{\frac{\mathcal{V}_i}{1-\theta}}}; \nu, \omega, \psi'\right) \quad \text{and: } k_*^i(k; \nu + \mathcal{V}_i, \omega, \psi') = e^{\frac{\mathcal{V}_i}{1-\theta}} \times k_*\left(\frac{k}{e^{\frac{\mathcal{V}_i}{1-\theta}}}; \nu, \omega, \psi'\right)$$

Consider a history of shock $(\omega_0, \psi_1, \omega_1, \psi_2, \dots, \omega_T, \psi_{T+1})$. Let $k_*(t=0), k_*(t=1), \dots, k_*(t=T)$ be the optimal sequence of capital for a firm with no long-term mean productivity $\mathcal{V}_i = 0$. We show by induction that $e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(t=0), e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(t=1), \dots, e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(t=T)$ is the optimal sequence of capital for the firm with \mathcal{V}_i .

Assume that: $k_*^i(t=0) = e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(t=0)$. At date 1, the firm with \mathcal{V}_i has exogenous state variables $(\nu_1 + \mathcal{V}_i, \omega_1, \psi_{2+1})$ at date 1, so that: $k_*^i(t=1) = k_*^i(e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(t=0); \nu_1 + \mathcal{V}_i, \omega_1, \psi_2) = e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(k_*(t=0); \nu_1, \omega_1, \psi_2) = e^{\frac{\mathcal{V}_i}{1-\theta}} k_*(t=1)$.

This result is useful for simulation purposes. To simulate the model in the presence of a long-run component in TFP, we just need to simulate the optimal capital from the Bellman problem of a firm with $\mathcal{V}_i = 0$ and we can then simply calculate the optimal capital stock of a firm facing a similar sequence of shocks by multiplying the capital stock by $e^{\frac{\mathcal{V}_i}{1-\theta}}$

B.2 Derivation of model moments

Our formulation of distorted expectations implies that:

$$\log\left(\mathbb{F}_{it-1}\left[e^{\frac{\Phi}{\alpha\theta}\nu_{it}}\right]\right) = \frac{\Phi}{\alpha\theta}((1-\rho)\mathcal{V}_i + \rho(\nu_{it-1} + \gamma\omega_{it-1}) + \psi_{it}) + \frac{1}{2}\left(\frac{\Phi}{\alpha\theta}\right)^2\sigma_\omega^2$$

Since k_{it} is purchased at date $t-1$, the date $t-1$ true forecast for date- t sales is:

$$\mathbb{F}_{it-1}[p_{it}y_{it}] = \frac{\Omega}{1-(1-\alpha)\theta}\mathbb{F}_{it-1}\left[e^{\frac{\Phi}{\alpha\theta}\nu_{it}}\right]k_{it}^\Phi$$

So that the true log-sales forecast error at date t is:

$$\begin{aligned} FE_{it} &= \log(p_{it}y_{it}) - \log(\mathbb{F}_{it-1}[p_{it}y_{it}]) \\ &= \frac{\Phi}{\alpha\theta}\nu_{it} - \log\left(\mathbb{F}_{it-1}\left[e^{\frac{\Phi}{\alpha\theta}\nu_{it}}\right]\right) \\ &= -\frac{\Phi}{\alpha\theta}(\gamma\rho\omega_{it-1}) + \frac{\Phi}{\alpha\theta}\omega_{it} - \frac{1}{2}\left(\frac{\Phi}{\alpha\theta}\right)^2\sigma_\omega^2 \end{aligned}$$

$\frac{\Phi}{\alpha\theta}\omega_{it} - \frac{1}{2}\left(\frac{\Phi}{\alpha\theta}\right)^2\sigma_\omega^2$ corresponds to rational expectation errors. $-\frac{\Phi}{\alpha\theta}(\gamma\rho\omega_{it-1})$ corresponds to expectation errors due to managers' distorted forecasts.

Accounting for mis-reporting of true forecasts, observed forecast errors are given by:

$$\begin{aligned}\widehat{FE}_{it} &= \log(p_{it}y_{it}) - \log\left(\widehat{\mathbb{F}}_{it-1}[p_{it}y_{it}]\right) \\ &= \log(p_{it}y_{it}) - \log(\mathbb{F}_{it-1}[p_{it}y_{it}]) - \zeta_{it} \\ &= -\frac{\Phi}{\alpha\theta}(\gamma\rho\omega_{it-1}) + \frac{\Phi}{\alpha\theta}\omega_{it} - \frac{1}{2}\left(\frac{\Phi}{\alpha\theta}\right)^2\sigma_\omega^2 - \zeta_{it},\end{aligned}$$

where ζ_{it} is the “noise” introduced by managers in their reported forecasts.

The variance of log-sales forecast errors in the data is therefore given by:

$$\text{Var}[\widehat{FE}_{it}] = \sigma_\zeta^2 + \left(\frac{\Phi}{\alpha\theta}\right)^2((1 + \gamma^2\rho^2)\sigma_\omega^2)$$

The covariance of date- t and date- $t-1$ reported log-sales forecast errors writes:

$$\text{Cov}[\widehat{FE}_{it}, \widehat{FE}_{it-1}] = -\left(\frac{\Phi}{\alpha\theta}\right)^2\gamma\rho\sigma_\omega^2$$

Distorted beliefs lead to persistence in forecast errors. An unusually large innovation ω_{it-1} implies a positive forecast error today. For an agent over-weighting such unusually large realization (i.e. $\gamma > 0$), this large innovation means a high forecast for date t sales, which leads, on average, to a negative forecast error at date t .

A regression of reported log-sales forecast errors at date t on reported log-sales forecast errors at date $t - 1$ leads to a regression coefficient κ_{FE} :

$$\kappa_{FE} = -\frac{\left(\frac{\Phi}{\alpha\theta}\right)^2\gamma\rho\sigma_\omega^2}{\sigma_\zeta^2 + \left(\frac{\Phi}{\alpha\theta}\right)^2((1 + \gamma^2\rho^2)\sigma_\omega^2)}$$

B.3 Proof of Equation 12

We first take capital as given, and maximize profit with respect to labor given wage. We obtain:

$$EBIT_{it} = (1 - \theta(1 - \alpha))Y^{1-\phi}e^{\frac{\Phi z_{it}}{\alpha}}k^\Phi\left(\frac{(1 - \alpha)\theta}{w}\right)^{\frac{1-\alpha}{\alpha}\Phi}$$

In the absence of adjustment costs to capital, the firm selects its capital stock k_{it} at date $t - 1$ to maximize date t profits. Given a user cost of capital $R = r + \delta$, this leads to the first-order condition:

$$\alpha\theta\frac{p_{it}y_{it}}{k_{it}} = R\left[\frac{e^{\frac{\Phi z_{it}}{\alpha}}}{\underbrace{\mathbb{F}_{t-1}e^{\frac{\Phi z_{it}}{\alpha}}}_{\equiv 1 + \tau_{it}}}\right]$$

Time to build acts like a wedge τ_{it} between the effective cost of capital and the frictionless cost of capital. This wedge has a rational and a bias component. Given that the mean of z is zero and that the TFP shocks z are normally distributed, the log-wedge is given by:

$$\log(1 + \tau_{it}) = \frac{\Phi}{\alpha}z_{it} - \ln\left(\mathbb{F}_{t-1}\left[e^{\frac{\Phi}{\alpha}z_{it}}\right]\right) = \ln(p_{it}y_{it}) - \ln(\mathbb{F}_{t-1}[p_{it}y_{it}]) = FE_{it}$$

In other words, the log-sales forecast error acts as a capital wedge for the firm. Based on this observation, we know from [Hsieh and Klenow \(2009\)](#) that aggregate TFP depends solely on the wedge

dispersion, i.e. on the dispersion of the log-sales forecast errors.

B.4 Formulas for computing aggregate output and TFP

Write $K^* = \int_i k_i^* di$ the average capital in an economy with $w = 1$, $Y = 1$ and $\mathcal{V}_i = 0$ for all i . Similarly, let $Y^* = \int_i p_i y_i di$ be the average sale in this economy. K^* and Y^* can be found by solving the firm-level problem described in Equation 17 assuming that $A = w = 1$.

Recall that, in our general equilibrium model, the sale of firm i in an economy with aggregate output Y is given by:¹⁷

$$p_{it} y_{it} = Y^{1-\theta} e^{\nu_{it}} (k_{it}^\alpha l_{it}^{1-\alpha})^\theta,$$

where ν_{it} is the revenue productivity in our firm-level model. After labor optimization, given a wage w on the labor market, firm i 's sales at date t is simply:

$$p_{it} y_{it} = (1 - (1 - \alpha)\theta)^{\frac{1-\alpha}{\alpha}} \frac{Y^{(1-\theta)\frac{\Phi}{\alpha\theta}}}{w^{\phi\frac{1-\alpha}{\alpha}}} e^{\frac{\Phi}{\alpha\theta}\nu_{it}} k_{it}^\Phi = \underbrace{\left(\frac{e^{\frac{\Phi}{\alpha\theta}\nu_i} Y^{(1-\theta)\frac{\Phi}{\alpha\theta}}}{w^{\phi\frac{1-\alpha}{\alpha}}} \right)}_{=e^{\frac{\Phi}{\alpha\theta}\lambda_i}} (1 - (1 - \alpha)\theta)^{\frac{1-\alpha}{\alpha}} e^{\frac{\Phi}{\alpha\theta}(\nu_{it}-\nu_i)} k_{it}^\Phi$$

Using the same proof as in Section B.1, it is direct to show that, for a firm with long-term productivity \mathcal{V}_i and in an economy with aggregate output Y and wage w , the optimal capital stock for a firm i is simply given by:

$$k_{it} = e^{\frac{\lambda_i}{1-\theta}} k_{it}^*,$$

where k_{it}^* is the capital stock chosen by a firm with a similar history of shocks (ω, ψ) , a long-term productivity of $\mathcal{V}_i = 0$ and $w = Y = 1$. Recall that $e^{\frac{\lambda_i}{1-\theta}} = \frac{e^{\frac{\mathcal{V}_i}{1-\theta}} Y}{w^{\frac{(1-\alpha)\theta}{1-\theta}}}$.

Therefore, since k_{it}^* is orthogonal to \mathcal{V}_i , the aggregate capital stock is given by:

$$K = \frac{Y}{w^{\frac{(1-\alpha)\theta}{1-\theta}}} \left[\int_i e^{\frac{\mathcal{V}_i}{1-\theta}} di \right] K^*$$

In a similar way, we can relate the sales of firm i , with long-term productivity \mathcal{V}_i in the actual economy (w, Y) , to the sales of a firm with a similar history of shocks (ω, ψ) , with long-term productivity 0 and in an economy with $w = Y = 1$:

$$p_{it} y_{it} = \underbrace{e^{\frac{\Phi}{\alpha\theta}\lambda_i} \times e^{\frac{\Phi}{1-\theta}\lambda_i}}_{=e^{\frac{\lambda_i}{1-\theta}}} p_{it}^* y_{it}^*$$

Therefore, since $p_{it}^* y_{it}^*$ is orthogonal to \mathcal{V}_i , we obtain a simple expression for the equilibrium wage:

$$w^{\frac{(1-\alpha)\theta}{1-\theta}} = \left[\int_i e^{\frac{\mathcal{V}_i}{1-\theta}} di \right] Y^*$$

In the actual economy, firm i labor demand is simply:

$$l_{it} = \left(\frac{(1-\alpha)\theta}{w} \right) p_{it} y_{it}$$

Therefore, aggregate labor demand writes:

$$L^d = \left(\frac{(1-\alpha)\theta}{w} \right) Y$$

¹⁷We omit the constant B for convenience, without loss of generality.

In equilibrium, labor supply equals labor demand:

$$\frac{L_0}{w_0^\epsilon} w^{1+\epsilon} = (1-\alpha)\theta Y$$

By substituting the equilibrium wage, one can derive an expression for aggregate output as a function of Y^* :

$$Y = \frac{L_0}{(1-\alpha)\theta w_0^\epsilon} \left(\left[\int_i e^{\frac{\nu_i}{1-\theta}} di \right] Y^* \right)^{(1+\epsilon)\frac{1-\theta}{(1-\alpha)\theta}}$$

We can similarly relate aggregate TFP to K^* and Y^* :

$$TFP = ((1-\alpha)\theta)^{1-\alpha} \left[\int_i e^{\frac{\nu_i}{1-\theta}} di \right]^{\frac{\theta}{1-\theta}} (Y^*)^{\frac{1-(1-\alpha)\theta}{\theta}} (K^*)^{-\alpha}$$

Let $K_0^* = \int_i k_i^{*,0} di$ be the average capital stock for *rational firms* with $w = Y = 1$ and $\nu_i = 0$, for all i . Similarly, let $Y_0^* = \int_i p_i^{*,0} y_i^{*,0} di$ be the average sales in this economy with rational firms. Aggregate TFP in general equilibrium with rational firms is simply given by:

$$TFP_0 = ((1-\alpha)\theta)^{1-\alpha} \left[\int_i e^{\frac{\nu_i}{1-\theta}} di \right]^{\frac{\theta}{1-\theta}} (Y_0^*)^{\frac{1-(1-\alpha)\theta}{\theta}} (K_0^*)^{-\alpha}$$

Therefore, the TFP loss due to distortion in forecasts can simply be expressed as:

$$\log(TFP_0) - \log(TFP) = \alpha(\log(K^*) - \log(K_0^*)) + \frac{1-(1-\alpha)\theta}{\theta}(\log(Y_0^*) - \log(Y^*))$$

B.5 Optimism / pessimism bias

Consider a firm with a fixed belief b_i and a long-term productivity ν_i , so that:

$$\nu_{it} = \rho\nu_{it-1} + (1-\rho)\nu_i + \psi_{it} + \omega_{it} \quad \text{and: } \nu_{it} \stackrel{\mathbb{F}}{\sim} \mathcal{N}(\rho\nu_{it-1} + (1-\rho)(\nu_i + b_i), \sigma_\omega^2)$$

The firm's optimization problem admits the following Bellman representation:

$$V^i(k; z, \omega, \psi') = \max_{k'} \left\{ \Omega e^{\frac{\Phi}{\alpha\theta} z} k^\phi - (k' - (1-\delta)k) - c_k \frac{(k' - (1-\delta)k)^2}{k} + \frac{1}{1+r} \mathbb{F}[V^i(k'; z', \omega', \psi'') | (z, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} z' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} (1-\rho)(\nu_i + b_i) + \rho z + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

Using the notations from Appendix B.1, it is direct to see that the optimal policy for this firm can be expressed as a function of the optimal policy of a firm with $b_i = 0$ and $\nu_i = 0$:

$$k_*^i(k; \nu + \nu_i + b_i, \omega, \psi') = e^{\frac{\nu_i + b_i}{1-\theta}} \times k_*\left(\frac{k}{e^{\frac{\nu_i + b_i}{1-\theta}}}; \nu, \omega, \psi'\right)$$

However, note that unlike in Appendix B.1, given a history of shock $\omega_0, \psi_1, \omega_1, \psi_2 \dots, \omega_T, \psi_{T+1}$, the capital stock of a firm with b_i and ν_i is *not* a constant multiple of the capital stock of the firm with $b_i = 0$ and $\nu_i = 0$. This is because if ν_1 is the productivity of the firm with $b_i = 0$ and $\nu_i = 0$ at date 1, the productivity of the firm with b_i and ν_i at date 1 is $\nu_1 + \nu_i$, not $\nu_1 + \nu_i + b_i$.

To numerically solve the model with a fixed bias in belief, we first find the optimal policy function for a firm with no biased belief ($b_i = 0$) and no long-run mean in productivity ($\mathcal{V}_i = 0$), $k_*(k; \nu, \omega, \psi')$. We then draw a history of shock $(\omega_{it}, \psi_{it})_t$, which allows us to calculate a history of actual TFP $(\nu_{it})_t$, with $\nu_{it} = \rho\nu_{it-1} + (1 - \rho)\mathcal{V}_i + \omega_{it} + \psi_{it}$. We then calculate the optimal capital stock of the firm recursively through:

$$k_{it+1} = k_*^i(k_{it}; \nu_{it}, \omega_{it}, \psi_{it+1}) = e^{\frac{\nu_i + b_i}{1-\theta}} \times k_*\left(\frac{k_{it+1}}{e^{\frac{\nu_i + b_i}{1-\theta}}}; \nu_{it} - \mathcal{V}_i - b_i, \omega_{it}, \psi_{it+1}\right)$$

To calculate aggregate TFP in this economy, we use a similar approach to the one described in Appendix B.4. We start by computing the average steady-state capital in the economy with $w = 1$, $Y = 1$ and $\mathcal{V}_i = 0$ for all i , but with γ and σ_b at their estimated value. Denote this steady state capital by $K^* = \int_i k_i^* di$. Similarly, let $Y^* = \int_i p_i y_i di$ be the average steady-state sales in this economy. Both K^* and Y^* can be found by solving the model in the way described above.

Recall that, in our general equilibrium model, the sale of firm i in an economy with aggregate output Y is given by:¹⁸

$$p_{it}y_{it} = Y^{1-\theta} e^{\nu_{it}} (k_{it}^\alpha l_{it}^{1-\alpha})^\theta,$$

where ν_{it} is the revenue productivity in our firm-level model. After labor optimization, given a wage w on the labor market, firm i 's sales at date t is simply:

$$p_{it}y_{it} = (1 - (1 - \alpha)\theta)^{\frac{1-\alpha}{\alpha}} \frac{Y^{(1-\theta)\frac{\Phi}{\alpha\theta}}}{w^{\frac{1-\alpha}{\alpha}}} e^{\frac{\Phi}{\alpha\theta}\nu_{it}} k_{it}^\Phi = \underbrace{\left(\frac{e^{\frac{\Phi}{\alpha\theta}\nu_i} Y^{(1-\theta)\frac{\Phi}{\alpha\theta}}}{w^{\frac{1-\alpha}{\alpha}}} \right)}_{=e^{\frac{\Phi}{\alpha\theta}\lambda_i}} (1 - (1 - \alpha)\theta)^{\frac{1-\alpha}{\alpha}} e^{\frac{\Phi}{\alpha\theta}(\nu_{it} - \mathcal{V}_i)} k_{it}^\Phi$$

We now relate the optimal investment decision of firms in an economy with $w = 1 = Y$ and $\mathcal{V}_i = 0$ to that of an economy with arbitrary w and Y and a long-term mean in TFP \mathcal{V}_i .

Consider first the Bellman problem of the firm with long-term productivity of $\mathcal{V}_i = 0$, bias (b) and $w = Y = 1$:

$$V_b(k; \nu, \omega, \psi') = \max_{k'} \left\{ \Omega e^{\frac{\Phi}{\alpha\theta}\nu} k^\Phi - (k' - (1 - \delta)k) - c_k \frac{(k' - (1 - \delta)k)^2}{k} + \frac{1}{1+r} \mathbb{E}[V(k'; \nu', \omega', \psi'') | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} \rho\nu + (1 - \rho)b + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\nu^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\psi^2 \end{pmatrix}\right) \text{ and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2), \text{ and}$$

$$\Omega = (1 - (1 - \alpha)\theta).$$

Let $k_b^*(k; \nu, \omega, \psi')$ be the optimal policy function of this problem. Consider now the problem of a firm with the same bias b , but with $w \neq 1$, $Y \neq 1$ and $\mathcal{V}_i \neq 0$:

$$V_b^i(k; z, \omega, \psi') = \max_{k'} \left\{ \left(\frac{Y^{1-\Phi}}{w^{\frac{1-\alpha}{\alpha}}} \right) \Omega e^{\frac{\Phi}{\alpha\theta}z} k^\Phi - (k' - (1 - \delta)k) - c_k \frac{(k' - (1 - \delta)k)^2}{k} + \frac{1}{1+r} \mathbb{E}[V^i(k'; z', \omega', \psi'') | (z, \omega, \psi')] \right\}$$

¹⁸We omit the constant B for convenience, without loss of generality.

with:

$$\begin{pmatrix} z' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} (1-\rho)(\mathcal{V}_i + b) + \rho z + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

Define $\nu = z - \mathcal{V}_i$. We can rewrite the Bellman problem as a function of ν instead of z :

$$V^i(k; \nu + \mathcal{V}_i, \omega, \psi') = \max_{k'} \left\{ \left(\frac{Y^{1-\Phi}}{w^{\frac{1-\alpha}{\Phi}}} \right) \Omega e^{\frac{\Phi}{\alpha\theta}(\nu + \mathcal{V}_i)} k^\phi - (k' - (1-\delta)k) - c_k \frac{(k' - (1-\delta)k)^2}{k} + \frac{1}{1+r} \mathbb{F}[V^i(k'; \nu' + \mathcal{V}_i, \omega', \psi'') | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} \rho\nu + (1-\rho)b + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

We can rewrite this previous problem in a simpler fashion:

$$V^i(k; \nu + \mathcal{V}_i, \omega, \psi') = \max_{k'} \left\{ e^{\frac{\lambda_i}{1-\theta}} \left(\Omega e^{\frac{\Phi}{\alpha\theta}\nu} \left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right)^\phi - \left(\left(\frac{k'}{e^{\frac{\lambda_i}{1-\theta}}} \right) - (1-\delta) \left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right) \right) - c_k \frac{\left(\left(\frac{k'}{e^{\frac{\lambda_i}{1-\theta}}} \right) - (1-\delta) \left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right) \right)^2}{\left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right)} \right) + \frac{1}{1+r} \mathbb{F}[V^i(k'; \nu' + \mathcal{V}_i, \omega', \psi'') | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} \rho\nu + (1-\rho)b + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2), \quad \text{and:}$$

$$e^{\frac{\lambda_i}{1-\theta}} = \frac{e^{\frac{\mathcal{V}_i}{1-\theta}} Y}{w^{\frac{\lambda_i}{1-\theta}}}.$$

This last representation is equivalent to:

$$\left(\frac{V^i(k; \nu + \mathcal{V}_i, \omega, \psi')}{e^{\frac{\lambda_i}{1-\theta}}} \right) = \max_{k'} \left\{ \left(\Omega e^{\frac{\Phi}{\alpha\theta}\nu} \left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right)^\phi - \left(\left(\frac{k'}{e^{\frac{\lambda_i}{1-\theta}}} \right) - (1-\delta) \left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right) \right) - c_k \frac{\left(\left(\frac{k'}{e^{\frac{\lambda_i}{1-\theta}}} \right) - (1-\delta) \left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right) \right)^2}{\left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}} \right)} \right) + \frac{1}{1+r} \mathbb{F}\left[\left(\frac{V^i(k'; \nu' + \mathcal{V}_i, \omega', \psi'')}{e^{\frac{\lambda_i}{1-\theta}}} \right) | (\nu, \omega, \psi')] \right\}$$

with:

$$\begin{pmatrix} \nu' \\ \omega' \end{pmatrix} \stackrel{\mathbb{F}}{\sim} \mathcal{N}\left(\begin{pmatrix} \rho\nu + (1-\rho)b + \gamma\rho\omega + \psi' \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\omega^2 & \sigma_\omega^2 \\ \sigma_\omega^2 & \sigma_\omega^2 \end{pmatrix}\right) \quad \text{and: } \psi'' \stackrel{\mathbb{F}}{\sim} \mathcal{N}(0, \sigma_\psi^2)$$

It is clear from this equation that:

$$k_b^{i,*}(k; \nu + \mathcal{V}_i, \omega, \psi') = e^{\frac{\lambda_i}{1-\theta}} \times k_b^*\left(\frac{k}{e^{\frac{\lambda_i}{1-\theta}}}; \nu, \omega, \psi'\right)$$

Consider a firm facing a history of shock (ω_t, ψ_t) .

It is direct to see from the previous result that for a firm with long-term productivity \mathcal{V}_i , bias b_i and

in an economy with aggregate output Y and wage w , the optimal capital stock is given by:

$$k_{it} = e^{\frac{\lambda_i}{1-\theta}} k_{it}^*,$$

where k_{it}^* is the capital stock chosen by a firm with a similar history of shocks (ω_{it}, ψ_{it}) , similar forecasting biases (b_i and γ) but with a long-term productivity of $\mathcal{V}_i = 0$, and $w = Y = 1$.

We can show this result by induction. Consider a history of shocks $(\omega_{it}, \psi_{it})_t$. Assume that $k_{i0} = e^{\frac{\lambda_i}{1-\theta}} k_{i0}^*$. At date 1, if ν_{i1} is the productivity of the firm with $\mathcal{V}_i = 0$, the productivity of the firm with \mathcal{V}_i is $\nu_{i1} + \mathcal{V}_i$. As a result, we know from our previous result that:

$$\begin{aligned} k_{i1} = k_b^{i,*}(k_{i0}; \nu_{i1} + \mathcal{V}_i, \omega_{i1}, \psi_{i2}) &= e^{\frac{\lambda_i}{1-\theta}} \times k_b^* \left(\frac{k_{i0}}{e^{\frac{\lambda_i}{1-\theta}}}; \nu_{i1}, \omega_{i1}, \psi_{i2} \right) \\ &= e^{\frac{\lambda_i}{1-\theta}} \times k_b^*(k_{i0}^*; \nu_{i1}, \omega_{i1}, \psi_{i2}) \\ &= e^{\frac{\lambda_i}{1-\theta}} k_{i1}^* \end{aligned}$$

In a similar way, we can relate the sales of firm i , with long-term productivity \mathcal{V}_i and bias b_i in the actual economy (w, Y) , to the sales of a firm with a similar history of shocks (ω, ψ) , with long-term productivity 0 and in an economy with $w = Y = 1$:

$$p_{it} y_{it} = \underbrace{e^{\frac{\Phi}{\alpha\theta} \lambda_i} \times e^{\frac{\Phi}{1-\theta} \lambda_i}}_{= e^{\frac{\lambda_i}{1-\theta}}} p_{it}^* y_{it}^*$$

Therefore, since $p_{it}^* y_{it}^*$ is orthogonal to \mathcal{V}_i , we obtain a simple expression for the equilibrium wage:

$$w^{\frac{(1-\alpha)\theta}{1-\theta}} = \left[\int_i e^{\frac{\mathcal{V}_i}{1-\theta}} di \right] Y^*$$

In the actual economy, firm i labor demand is simply:

$$l_{it} = \left(\frac{(1-\alpha)\theta}{w} \right) p_{it} y_{it}$$

Therefore, aggregate labor demand writes:

$$L^d = \left(\frac{(1-\alpha)\theta}{w} \right) Y$$

In equilibrium, labor supply equals labor demand:

$$\frac{L_0}{w_0^\epsilon} w^{1+\epsilon} = (1-\alpha)\theta Y$$

By substituting the equilibrium wage, one can derive an expression for aggregate output as a function of Y^* :

$$Y = \frac{L_0}{(1-\alpha)\theta w_0^\epsilon} \left(\left[\int_i e^{\frac{\mathcal{V}_i}{1-\theta}} di \right] Y^* \right)^{(1+\epsilon) \frac{1-\theta}{(1-\alpha)\theta}}$$

We can similarly relate aggregate TFP to K^* and Y^* :

$$TFP = ((1-\alpha)\theta)^{1-\alpha} \left[\int_i e^{\frac{\mathcal{V}_i}{1-\theta}} di \right]^{\frac{\theta}{1-\theta}} (Y^*)^{\frac{1-(1-\alpha)\theta}{\theta}} (K^*)^{-\alpha}$$

To calculate the TFP losses from distorted beliefs, we can simply simulate the model assuming $\gamma = \sigma_b = 0$, $Y = w = 1$ and $\sigma_Y = 0$, calculate the average capital K_0^* and sales Y_0^* in this economy, and compute:

$$\Delta \log(TFP) = \alpha (\log(K^*) - \log(K_0^*)) + \frac{1 - (1 - \alpha)\theta}{\theta} (\log(Y_0^*) - \log(Y^*))$$

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