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The (mis)specification of discrete duration models  
with unobserved heterogeneity: a Monte Carlo study

by Cheti Nicoletti and Concetta Rondinelli

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# THE (MIS)SPECIFICATION OF DISCRETE DURATION MODELS WITH UNOBSERVED HETEROGENEITY: A MONTE CARLO STUDY

by Cheti Nicoletti<sup>†</sup> and Concetta Rondinelli<sup>‡</sup>

## Abstract

Empirical researchers usually prefer statistical models that can be easily estimated using standard software packages. One such model is the sequential binary model with or without normal random effects; such models can be adopted to estimate discrete duration models with unobserved heterogeneity. But ease of estimation may come at a cost. In this paper we conduct a Monte Carlo simulation to evaluate the consequences of omitting or misspecifying the unobserved heterogeneity distribution in single-spell discrete duration models.

**JEL Classification:** C23, C25.

**Keywords:** discrete duration models, unobserved heterogeneity, Monte Carlo simulations.

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# 1 Introduction<sup>1</sup>

This paper provides a guide for applied econometricians in using conventional software to estimate single-spell discrete duration models. To this aim we carry out a set of Monte Carlo exercises to evaluate the consequences, in terms of bias, of using sequential binary models with or without normal random effects.

As first noticed by Yamaguchi (1991) and Jenkins (1995), single-spell discrete duration models can be easily estimated by considering parametric models for repeated binary measures such as probit, logit or complementary log-log. Moreover, they can be extended to take account of unobserved heterogeneity by introducing a random component, which represents a scalar function of time-invariant unobserved variables.<sup>2</sup> It is then possible to estimate model parameters by maximizing the likelihood function integrated over the unobserved random effect. The resulting model is a mixture of hazard functions with respect to the unobserved random component. The estimation of these mixture models requires either assuming a specific parametric distribution for the random component, or using a non-parametric maximum likelihood estimation.

In principle non-parametric maximum likelihood estimation is the best solution to minimize the potential bias caused by improper parametric distributional assumptions.<sup>3</sup> Nevertheless, the computation of the non-parametric estimator is not usually feasible using commands built into common software packages. For this reason many non-specialists adopt easier estimation methods either by imposing specific parametric distributions for the unobserved heterogeneity or by ignoring the unobserved heterogeneity altogether.

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<sup>2</sup>This way to control for unobserved heterogeneity was first introduced for continuous duration models; see Lancaster (1979, 1990), Heckman and Singer (1984) and van den Berg (2001).

<sup>3</sup>See, for continuous time, Heckman and Singer (1984) and, for discrete time, Baker and Melino (2000) and Zhang (2003).

In discrete duration models the assumption of a normal distribution can be computationally convenient.<sup>4</sup> Under this assumption, discrete duration models can be easily estimated as binary models with normal random effects using widely available statistical softwares.<sup>5</sup>

In this paper we use a Monte Carlo study to evaluate the consequences of ignoring the unobserved heterogeneity or misspecifying its parametric distribution when estimating single-spell discrete duration models. While Baker and Melino (2000), Zhang (2003), Gaure et al. (2007) and Mroz and Zayats (2008) consider the consequences of choosing different numbers of support points when imposing a non-parametric distribution for the unobserved heterogeneity,<sup>6</sup> we evaluate the consequences of imposing a normal random effect. On the other hand, similarly to Baker and Melino (2000), Zhang (2003) and Gaure et al. (2007), we consider the effect of neglecting unobserved heterogeneity.

One important issue - overlooked by Baker and Melino (2000), Zhang (2003) and Gaure et al. (2007) - is that the residual variance in sequential binary models changes if unobserved heterogeneity is ignored or if a non-parametric distribution with too few or too many support points is used. Since the coefficients in binary models are usually normalized by dividing them by the residual standard deviation, models with high (low) residual variances produce coefficients that are attenuated (amplified). As suggested by Mroz and Zayats (2008), the attenuation (amplification) biases that Baker and Melino (2000), Zhang (2003) and Gaure et al. (2007) find could be due at least in part to this neglected issue.

In this paper we show that the coefficient bias, caused by the omission of the unobserved heterogeneity or by imposing an incorrect normality assumption, can be a consequence of the

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<sup>4</sup>In continuous duration models, the unobserved heterogeneity distribution is often chosen to be gamma for analytical convenience (see Lancaster, 1979) and theoretical reasons (see van den Berg, 2001 and Abbring and van den Berg, 2007).

<sup>5</sup>For example, Stata provides the commands `xtcloglog`, `xtlogit` and `xtprobit` (`cloglog`, `logit` and `probit`) to estimate binary models with normal random effects (without normal random effects) and error terms with extreme value, logistic and normal distributions. For more details on discrete duration models we refer to Holford (1976), Prentice and Gloeckler (1978), Allison (1982), Narendranathan and Stewart (1993) and Sueyoshi (1995).

<sup>6</sup>Studies of the consequences of misspecification of the unobserved heterogeneity in continuous duration models have been conducted by Heckman and Singer (1984), Lancaster (1985), Trussell and Richards (1985), Ridder (1987), Huh and Sickles (1994) and Dolton and van der Klaauw (1995).

coefficient normalization issue. Given this difficulty in comparing covariate coefficients across different models, we also consider another way to evaluate the consequences of adopting simplified duration models. We check whether their predicted effects of changes in covariates on expected duration and survival probabilities are close to the true effects.

The paper is organized as follows. Section 2 considers the effects of neglecting unobserved heterogeneity while Section 3 considers the effects of its misspecification. In both sections we first discuss the theoretical consequences and then assess these possible consequences through a Monte Carlo simulation exercise. In Section 4 we summarize the main findings.

## 2 Ignoring unobserved heterogeneity

### 2.1 Consequences

Ignoring unobserved heterogeneity in duration models can cause a bias in estimating the duration dependence. More precisely, omitting the unobserved heterogeneity causes an overestimation of the negative duration dependence (see for example Lancaster, 1990 and van den Berg, 2001). People who have a high unobserved random component are more likely to complete their duration early, so that the sample of individuals that survive is a selected sample with relatively small random effects.<sup>7</sup> This selection process is known as “weeding out” or “sorting effect”.

Omitting unobserved heterogeneity may also bias the coefficients estimation of the explanatory variables in the hazard model. For example, neglecting unobserved heterogeneity in mixed proportional (continuous time) hazard models causes an underestimation of the proportionate response of the hazard function with respect to the explanatory variables.<sup>8</sup>

The bias is again due to a weeding out effect. Let us assume that the unobserved heterogeneity is given by a time-invariant scalar random effect,  $\theta$ , independent of the explanatory variables; while the observed heterogeneity is given by a scalar function  $\mu = m(X; \beta)$ , where  $X$  is a vector of individual time-invariant explanatory variables and  $\beta$  is the vector of the cor-

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<sup>7</sup>Notice that, without loss of generality, we assume that the unobserved random component is positively related to the hazard function.

<sup>8</sup>See van den Berg (2001) for a formal proof.

responding coefficients. Without loss of generality, we assume in this section that the hazard function conditional on the observed explanatory variables and the unobserved heterogeneity is positively related to both  $\theta$  and  $\mu$ . A hazard model ignoring the unobserved heterogeneity is a hazard function conditional on the observed characteristics,  $X$ , but unconditional on the unobserved heterogeneity,  $\theta$ , which we call the “observed hazard function”. The difference in the observed hazard function between survivors with high and low values of  $\mu$  reflects also a gap in their values of  $\theta$ . Survivors with a large  $\mu$  have on average a smaller  $\theta$  than do survivors with a small  $\mu$ , so that the difference between the observed hazard functions is on average lower than that we would observe if the survivors had the same value for  $\theta$ . If we fail to recognize that the lower difference between the observed hazards is due to a difference in the unobserved heterogeneity, we would erroneously estimate an attenuated effect of the explanatory variables on the hazard.

More rigorously, the weeding out effect on the covariate coefficients can be described as the consequence of a lack of independence between the random effect for individual  $i$ ,  $\theta_i$ , and its observed heterogeneity,  $m(X_i; \beta)$ , given a duration  $T_i \geq \tau$ , where  $\tau$  is a scalar strictly higher than zero, say the failure of the condition  $(\theta_i \perp\!\!\!\perp m(X_i; \beta) \mid T_i \geq \tau)$ . Notice, instead, that hazard models assume that  $(\theta_i \perp\!\!\!\perp X_i)$  which implies that  $(\theta_i \perp\!\!\!\perp m(X_i; \beta) \mid T_i \geq 0)$ . We assume here that  $(T_i \mid X_i, \theta_i)$  is identically and independently distributed (i.i.d.) across individuals.

There are some continuous duration models for which the attenuation bias due to omitted unobserved heterogeneity reduces to a rescaling by a factor (a bias proportionally identical) for all explanatory variables coefficients or to a bias only for the intercept. Lancaster (1985) proves analytically that omitting unobserved heterogeneity in mixed proportional hazard models with baseline distribution given by a Weibull distribution causes a rescaling by a constant factor for all coefficients. Ridder (1987) analytically shows that the omission in mixed proportional hazard models with known baseline hazard and with no right censoring causes a bias only for the intercept. Moreover, Ridder (1987) suggests that replacing the baseline with a non-parametric flexible specification should produce an almost unbiased estimation of the covariates coefficients.

Ridder’s suggestion is supported by his Monte Carlo study and by some other empirical

studies: see Dolton and van der Klaauw (1995), Meyer (1990), and Trussell and Richards (1985). By contrast, the conjecture is not confirmed by the Monte Carlo experiment in Baker and Melino (2000), when they consider the omission of unobserved heterogeneity in discrete duration models with single spells. This contradictory result may be due to the fact that in discrete duration models the coefficients are identified only up to a scale normalization and models with different specifications use different normalizations, which Baker and Melino (2000) do not consider.

It is easy to prove analytically that the omission of the unobserved heterogeneity causes only a rescaling by a factor of the covariate coefficients when considering sequential probit models with normal random effects  $\theta_{it}$  that are i.i.d. across individuals and time  $t$ , and independent of the explanatory variables,  $X_{it}$ , and with known duration dependence function. This is because  $(\theta_{it} \perp\!\!\!\perp m(X_{it}; \beta) \mid T_i \geq \tau)$  for any  $\tau \geq 0$ . The proof is an application of the analytical results in Arulampalam (1999).

Similar analytical results do not exist for more general discrete duration models. In this paper we carry out a Monte Carlo simulation exercise to study the consequences of omitting unobserved heterogeneity in more general cases. In particular, we simulate sequential binary models where

- a.** the unobserved random effect is time-invariant and follows a normal, a gamma or a discrete distribution with two points of support,
- b.** the error distribution is logistic instead of normal,
- c.** and the covariates are i.i.d. across individuals and time or i.i.d. across individuals but not time.

Cases (a) and (b) were considered by Baker and Melino (2000) who found that ignoring unobserved heterogeneity component causes an attenuation bias for the covariate coefficients. We replicate their Monte Carlo study to re-evaluate the consequences of ignoring unobserved heterogeneity, but take into account the coefficient normalization.

Mroz and Zayats (2008) reconsider the Monte Carlo study of Baker and Melino (2000) to compare the effects of alternative non-parametric specifications of the unobserved heterogeneity distribution when taking account of the normalization issue. Baker and Melino



(2000) conclude that non-parametric maximum likelihood estimation that penalizes specifications with many mass points produces better results; however, Mroz and Zayats (2008) present opposite results.

Case (c) is a useful extension to understand whether the estimation bias depends on the type of covariates used. If the covariates  $X_{it}$  are i.i.d. across individuals and time, then the estimation bias should be reduced because the independence between the unobserved component and the observed covariates tends to hold even when conditioning to  $T_i > 0$ , that is  $(\theta_i \perp\!\!\!\perp X_{it} \mid T_i \geq \tau)$ , where  $\tau > 0$ .

If, on the contrary, covariates are i.i.d. across individuals but time-invariant or correlated across time, then we expect an attenuation bias. However, this bias could consist of a rescaling by a constant factor for all covariate coefficients.

## 2.2 Monte Carlo simulation: Data Generating Processes

We consider the same data generating processes (DGPs) used in the Monte Carlo study of Baker and Melino (2000) and generalize them to consider both time-varying and time-invariant explanatory variables.

We assume that duration is measured in discrete time. This is quite often the case when observations are grouped into intervals or when the event whose occurrence defines the end of a duration (terminating event) can occur only in discrete time. We record an event taking place in the interval  $(t - 1, t]$  as occurred in  $t$ .

We assume that the probability that an individual  $i$  experiences a terminating event in  $t$  conditional on survival to  $(t - 1)$  is given by:

$$Pr(d_{it} = 1 \mid d_{it-1} = 0) = Pr(z_{it}^* < 0 \mid z_{it-1}^* \geq 0) \quad (1)$$

where  $d_{it}$  is a dummy variable indicating the event occurrence in  $t$  for individual  $i$ , and  $z_{it}^*$  is a continuous latent variable which is lower than zero if  $d_{it} = 1$  and higher or equal to zero otherwise. We assume that  $z_{it}^*$  obeys the following linear model:

$$z_{it}^* = X_{it}\beta - f(t) + \theta_i + \epsilon_{it} \quad (2)$$

where  $X_{it}$  is a vector of explanatory variables,  $\beta$  is the corresponding vector of parameters,

$f(t)$  is a deterministic function of elapsed duration,  $\theta_i$  is an individual random effect representing unobserved heterogeneity,  $\epsilon_{it}$  is a residual error term distributed as a logistic with zero mean and variance  $\pi^2/3$  and both  $\theta_i$  and  $\epsilon_{it}$  are independent of the explanatory variables.<sup>9</sup> Then we can write the hazard probability conditional on the observed explanatory variables,  $X_{it}$ , and on the unobserved heterogeneity,  $\theta_i$ , as

$$Pr(d_{it} = 1 | d_{it-1} = 0, X_{it}, \theta_i) = \frac{1}{1 + \exp(z_{it})} \quad (3)$$

where

$$z_{it} = X_{it}\beta - f(t) + \theta_i. \quad (4)$$

By choosing differing specifications for the observed explanatory variables,  $X_{it}$ , the duration dependence function,  $f(t)$ , and the unobserved heterogeneity,  $\theta_i$ , we produce different DGPs.

We organize the simulations in two main sets. In the first set, exercise **A**, we focus on the effect of omitting unobserved heterogeneity when using different types of explanatory variables. In particular the three DGPs use three typologies of observed explanatory variables: **A1** time-varying variables, **A2** time-invariant variables and **A3** variables given by the sum of a time-invariant variable and a time-varying one, say mixture variables. For each of these DGPs we consider two types of duration dependence function, one increasing and one decreasing, and three distributions for the unobserved heterogeneity, a discrete (with two support points), a gamma and a normal distribution. This provides us with 18 different DGPs.

In the second set of simulations, exercise **B**, we consider both time-invariant and time-varying covariates and focus on the effect of omitting the unobserved heterogeneity when considering or not considering duration dependence in the simulated and estimated models. Again we consider three types of distribution for the unobserved heterogeneity, whereas only one specification is given to the duration function and the vector of covariates that includes both time-invariant and mixture variables. This second simulation exercise produces six types of DGPs.

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<sup>9</sup>The definition of the above discrete hazard model and the notation used are consistent with Baker and Melino (2000).

For each of the DGPs in simulation exercises **A** and **B** we consider three sample sizes: 500, 1000 and 5000 individuals.

As in Baker and Melino (2000) we draw 100 samples for each DGP, follow the individuals for 40 periods and consider all durations greater than 40 as censored.

In the following, we discuss in more detail how the explanatory variables, the duration dependence function and the unobserved heterogeneity distribution are specified for different types of DGP.

### Observed explanatory variables.

As in Baker and Melino (2000) we fix the variance of the observed heterogeneity in the hazard model,  $Var(X_{it}\beta)$ , to be equal to 0.25 for all our simulations.

In exercise **A** the observed heterogeneity of the hazard model is specified as follows:

$$X_{it}\beta = X_{1,it}\beta_1 + X_{2,it}\beta_2. \quad (5)$$

where  $X_{1,it}$  and  $X_{2,it}$  are normal random variables, and  $\beta_1$  and  $\beta_2$  are fixed parameters which we set to be equal to 1 and 0.5.

We consider three different simulations for the variables,  $X_{1,it}$  and  $X_{2,it}$ :

**A1** two independent time-varying variables identically and independently distributed (i.i.d.) across individuals and time with zero means and variances 0.125 and 0.5;

**A2** two independent time-invariant variables i.i.d. across individuals with zero means and variances 0.125 and 0.5;

**A3** and two independent variables defined as the sum of a time-invariant variable and a time-varying one, say mixture variables; more precisely,  $X_{1,it}$  ( $X_{2,it}$ ) is the sum of a time-varying variable defined as **A1** but with variance 0.0625 (0.25) and a time-invariant variable defined as in **A2** but with variance 0.0625 (0.25).

Simulation **A1** represents an extreme case that is interesting from a theoretical viewpoint but less common from an empirical one. In empirical examples explanatory variables are usually correlated across time so that the assumption of explanatory variables i.i.d. across individuals and time does not seem to be very plausible. Simulation **A2** represents the

opposite extreme case where all the explanatory variables are supposed to be time-invariant: the case considered by Baker and Melino (2000). Finally, simulation **A3** represents an intermediate case where the explanatory variables are given by the sum of a time-invariant component and a time-varying one. Earnings and income can be examples of such types of variables. Earnings and income (or their logarithm transformations) are usually assumed by economists to be the sum of a permanent component and a transitory one (see for example Moffitt and Gottschalk, 2002).

In simulation exercise **B** we specify the observed heterogeneity of the hazard model as:

$$X_{it} \beta = X_{1,i} \beta_1 + X_{2,i} \beta_2 + X_{3,it} \beta_3 + X_{4,it} \beta_4 \quad (6)$$

where  $X_{1,i}$  and  $X_{2,i}$  are time-invariant variables,  $X_{3,it}$  and  $X_{4,it}$  are mixture variables and  $\beta' = [1, 0.5, 1, 0.5]$ . To be more specific  $X_{1,i}$  and  $X_{2,i}$  are time-invariant variables defined as in **A2** but with variances 0.0625 and 0.25,  $X_{3,it}$  and  $X_{4,it}$  are mixture variables defined as in **A3** but with variances 0.0625 and 0.25, and all explanatory variables are independent.

### Duration Dependence.

In exercise **A** we consider, as in Baker and Melino (2000), the following deterministic time function

$$f(t) = 1 - \exp\left(\frac{1-t}{5}\right) \quad (7)$$

for a positive duration dependence and

$$f(t) = \exp\left(\frac{1-t}{5}\right) - 1 \quad (8)$$

for a negative duration dependence.

In simulation exercise **B** we consider instead  $f(t) = 0$  for no duration dependence and again  $f(t) = \exp\left(\frac{1-t}{5}\right) - 1$  for a negative duration dependence.

### Unobserved Heterogeneity.

In both exercises **A** and **B** three distributions for the unobserved heterogeneity  $\theta_i$  are assumed: discrete, gamma and normal. To be consistent with Baker and Melino (2000) we set  $E(\theta_i) = 1.8$  and  $Var(\theta_i) = 1$  and for the discrete distribution we consider two support

points with equal probability, that is:

$$\theta_i = \begin{cases} 0.8 & \text{with probability 0.5} \\ 2.8 & \text{with probability 0.5.} \end{cases} \quad (9)$$

### 2.3 Monte Carlo simulation: estimation models

Using the data simulated in exercise **A** we estimate a sequential logit model as specified in (3) but ignoring the unobserved heterogeneity and approximating the duration dependence function with either a cubic polynomial in  $t$  or using a step function. As in Baker and Melino (2000) we consider a step function given by

$$\phi(t) = \sum_{\tau=1}^{40} \phi_{\tau} D_{t\tau} \quad (10)$$

where

$$D_{t\tau} = \begin{cases} 1 & \text{if } t = \tau \\ 0 & \text{otherwise} \end{cases}$$

and  $\phi_{\tau}$ ,  $\tau = 1, \dots, 40$  are the corresponding coefficients. However, because few individuals survive after 15 periods, we allow the coefficients to vary for each period until  $\tau = 14$  and then we impose constant coefficients within the following time intervals:  $\tau = 15 - 19$ ,  $20 - 24$ ,  $25 - 29$ ,  $30 - 40$ .

Using the data simulated in exercise **B** we estimate again a sequential logit model ignoring the unobserved heterogeneity and approximating the duration dependence function with either a zero function (no duration dependence) or the above step function.

### 2.4 Results

In this section we present the results of the Monte Carlo simulation exercises **A** and **B**.

The results of exercise **A** are reported in Table 1, which is divided into three panels providing the estimated coefficients for time-varying covariates (top panel **A1**), time-invariant covariates (middle panel **A2**) and mixture covariates (bottom panel **A3**). We report the average and the standard deviation over 100 replications for the covariate coefficients,  $\beta_1$  (the true value of which is 1) and  $\beta_2$  (which true value is 0.5), and their ratio  $\beta_1/\beta_2$ . By row we

specify the type of DGP used to generate the simulated data. More precisely, we consider six types of DGPs: sequential logit model with negative or positive duration dependence and with unobserved heterogeneity following a discrete with two mass points, a gamma or a normal distribution (labeled “Discrete UH”, “Gamma UH” and “Normal UH”). By column we specify instead the sample size (500 or 1000 observations or individuals) and the type of estimation model used: sequential logit model omitting random effects and with duration dependence approximated by a step function (labeled “Step DD”) or by a cubic polynomial (labeled “polynomial DD”).

If the omission of the unobserved heterogeneity causes an attenuation bias because of a rescaling by a constant factor of the coefficients, then the ratio between coefficients would be correctly estimated. This seems supported by the results in Table 1 when using any type of covariates. Moreover, when using time-varying covariates that are i.i.d. across individuals and time (top panel **A1**), the attenuation problem for the coefficients does not seem significant. When, instead, the covariates are i.i.d. across individuals and time-invariant, the attenuation problem is more severe (middle panel **A2**). Finally, the attenuation bias magnitude seems to be intermediate between the two previous extreme cases for mixture covariates (bottom panel **A3**).

Using different distributions for the simulated unobserved heterogeneity components and different specifications for the simulated duration dependence (negative or positive) produces some very small and insignificant differences in the coefficients. Similarly, the way we estimate the duration dependence (by considering either a step or a cubic polynomial function) does not affect the results.

Finally, increasing the sample size from 500 to 1000 observations leads to a slight improvement in the results, meaning that the attenuation bias for  $\beta_1$  and  $\beta_2$  decreases a little and the average ratio between coefficients becomes even closer to its true value. We find again a slight improvement in the results when the number of observation are increased to 5000 (results are not reported but are available upon request to the authors).

To summarize, ignoring unobserved heterogeneity in sequential logit models seems to cause an attenuation of the covariate coefficients due to a rescaling by a constant factor. This attenuation bias is almost completely canceled when using covariates that are i.i.d. across

individuals and time, while it is very significant when the covariates are highly autocorrelated.

As emphasized in Section 2.1, ignoring unobserved heterogeneity may cause an estimation bias for the covariate coefficients as well as for the duration dependence function. To check whether the duration dependence is well estimated we compare the true (simulated) and estimated duration dependence functions under the different DGPs simulated in Monte Carlo exercise **A1** (see Figures 1). We consider a negative and a positive true dependence function, equations (8) and (7), in the Figure 1 panels (a) and (b) respectively. The estimated dependence functions are computed by using the estimated intercept and coefficients (both averaged across the 100 replications considered in our Monte Carlo exercise) of the cubic polynomial used to approximate the duration dependence function. We draw three estimated duration dependence functions, one for each type of unobserved heterogeneity distribution simulated (labeled as before “Discrete UH”, “Gamma UH” and “Normal UH”).

Ignoring the unobserved heterogeneity causes an overestimation of the negative duration dependence and a spurious negative dependence when the true one is positive. Furthermore, it seems that the duration dependence function is better estimated at low durations.

Sometimes empirical researchers are interested in the effect of covariates on survival probabilities and expected duration. For this reason we also report the true (simulated) and estimated effects of changes in the covariate  $X_1$  on the survival function and expected duration in Table 5.<sup>10</sup> For each row the results are obtained under some of the DGPs simulated in Monte Carlo exercise **A1**. The simulated DGPs are sequential logit models with two possible choices for the duration dependence (positive and negative) and three types of unobserved heterogeneity distribution (labeled as before “Discrete UH”, “Gamma UH” and “Normal UH”). The true and estimated survival functions (expected duration) are computed fixing the variable  $X_2$  at its mean, zero, and the variable  $X_1$  at three values, its mean (zero) and its mean plus or minus half its standard deviation. The expected duration is given by  $E(TI_{T \leq 40} | X_1, X_2 = 0)$  where  $I$  denotes the indicator function taking value 1 for durations shorter or equal to 40 and 0 otherwise; the survival function is given by

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<sup>10</sup>Since both the estimated survival functions and the expected durations are based on hazard functions that ignore the unobserved heterogeneity, we consider their true (simulated) counterparts after integrating out the random effect through simulation.

$\Pr(T > t \mid X_1, X_2 = 0)$  and is computed at  $t = 5$  and  $10$ .

Both the survival function and the effects of changes in  $X_1$  are well estimated at durations of 5 and 10, while their estimation slightly deteriorates with longer durations.

The true and estimated expected duration values are very close; as a consequence, the effects of changes in  $X_1$  on the expected duration is well estimated. These results are quite encouraging if compared with similar effects computed by Mroz and Zayats (2008) (see their Table 2) when using non-parametric maximum likelihood estimation to take account of unobserved heterogeneity as in Baker and Melino (2000). Our results of the estimated effects of  $X_1$  on the expected duration are much better compared with the ones that are computed using non-parametric maximum likelihood estimation and adopt the Hannan-Quinn Information Criterion suggested by Baker and Melino (2000).

Furthermore, the differences between the true and estimated survival function (expected duration) as well as the true and estimated effects of changes in  $X_1$  on the survival function (expected duration) do not change across DGPs considered in the full Monte Carlo exercise **A**.<sup>11</sup>

When we simulate a hazard model with two time-invariant and two time-varying variables (see equation [6] and simulation exercise **B**) and estimate it ignoring the unobserved heterogeneity, the covariate coefficients seem again to be significantly underestimated. Moreover, the underestimation of the coefficients tends to be slightly larger for the pair of time-invariant variables than for the pair of time-varying ones.<sup>12</sup> In other words, it seems that the rescaling factor is slightly dissimilar for different types of variables (time-varying and invariant variables). Indeed, the ratios between coefficients seem to be correctly estimated when considering two variables of the same type and to be slightly biased when considering the ratio between two different types of variables. Nevertheless, since the standard deviations for coefficient ratios are quite high, the differences in the rescaling factor are not significant. This result is confirmed even when using a larger sample size of 5000 observations. In conclusion, we find again that omitting the unobserved heterogeneity causes an attenuation of the covariate coefficients due to a rescaling factor that differs slightly and not significantly by

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<sup>11</sup>The results of the entire Monte Carlo exercise **A** are available from the authors upon request.

<sup>12</sup>The detailed results of exercise **B** are not reported but are available from the authors upon request.



typology of variable.

More generally the rescaling factor of a covariate could depend on its association with the duration and with other variables.<sup>13</sup> Nevertheless, even if each type of covariate had a different rescaling factor, we could still infer the statistical significance of each variable and compare significance across variables. This is because tests of significance, such as the Wald chi-square, are based on the ratio between the estimated covariate coefficient and its standard error, so that the rescaling factor cancels out.

When the estimation models ignore both the unobserved heterogeneity and the duration dependence, the underestimation of covariate coefficients is reduced and the rescaling factor becomes more similar for variables of different types. The ratios between coefficients are not biased, especially when considering a sample size of 5000 observations.

In conclusion, the two main findings of this section are that ignoring the unobserved heterogeneity in sequential logit models causes a rescaling of the covariates coefficients and an underestimation of the duration dependence, but the effect of covariates on the survival function and expected duration does not seem to be badly estimated. Since coefficients in binary models are only identified up to a scale normalization, applied researchers should not be concerned about the rescaling problem.

## **3 Misspecifying the unobserved heterogeneity distribution**

### **3.1 Consequences**

Heckman and Singer (1984) argue that an incorrect assumption about the distribution of the unobserved heterogeneity in hazard models can have severe consequences. In particular, they find that the parameter estimates for a model with Weibull baseline hazard are very sensitive to changes in the distribution assumed for the unobserved heterogeneity. Similar

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<sup>13</sup>Note that the use of variables that change almost monotonically with the duration or of covariates which are collinear can cause identification problems.

results are found also by Trussell and Richards (1985), Hougaard et al. (1994), Baker and Melino (2000), Zhang (2003) and Gaure et al. (2007). However, Ridder and Verbakel (1983) criticize the findings of Heckman and Singer (1984) and highlight the fact that a non-flexible specification of the baseline hazard may explain their (Heckman and Singer, 1984) findings.

In this paper we consider the heterogeneity misspecification problem in single-spell discrete duration models specified as sequential binary models.

Since sequential binary models with a normal distribution for the unobserved heterogeneity term can be easily estimated using conventional softwares, we wonder if practitioners should worry about the possible consequences of an incorrect normality assumption. For this reason, we carry out a Monte Carlo exercise where we evaluate the effect of imposing a normal distribution for the unobserved heterogeneity component when its true distribution is a gamma or a discrete distribution with two support points.

In addition, we consider the potential consequences of misspecifying the distribution of the residual error as well as of the unobserved heterogeneity in sequential binary models. This can be useful to guide empirical researchers in the choice of the sequential binary models (probit, logit or complementary log-log) to estimate discrete hazard models.

Before presenting the Monte Carlo exercise, we emphasize that identification of unobserved heterogeneity and duration dependence in duration models with single spells can be problematic.

In case of continuous duration and single spells, Elbers and Ridder (1982) prove that it is possible to non-parametrically identify mixed proportional hazard models with covariates. The identification is possible because this model is multiplicative in the duration and in the covariates, whereas the observed hazard function (i.e. the hazard function integrated over the unobserved heterogeneity component) is not. This implies that the interactions between duration and covariates in the observed hazard allow identifying the unobserved heterogeneity and the duration dependence in the mixed proportional hazard models (see van den Berg, 2001). On the contrary, a mixed hazard model that allows for interaction between covariates and duration would not be identified, except when using time varying covariates (see Brinch, 2007).

Similarly, single-spell discrete duration models with unobserved heterogeneity cannot be

identified if we allow covariate coefficients to change with duration and consider only time invariant covariates. This result is emphasized by Mroz and Zayats (2008) and Mroz (2008).<sup>14</sup>

The duration models with normal random effect considered in the next section are theoretically identified because they include time varying covariates without interaction with duration.

### 3.2 Monte Carlo simulation: DGPs and estimation models

As in Section 2, we carry out a Monte Carlo experiment by simulating 100 samples from a set of DGPs (data generator processes).

The DGPs used to generate the data are sequential logit models with unobserved heterogeneity following three alternative types of distribution (discrete, gamma or normal), with a negative time duration dependence and two explanatory variables given by two mixture variables. For more details on the DGPs we refer to Monte Carlo exercise **A3** described in Section 2.2.

Our estimation models are sequential binary models with normal random effects and duration dependence approximated by a cubic polynomial in the duration. We consider three models: (1) sequential logit, (2) sequential probit and (3) sequential complementary log-log models. We estimate these sequential binary models with random effects by using Stata, which approximates the integral of the likelihood function with respect to the random effects by using an adaptive Gauss-Hermite quadrature (see StataCorp, 2005).<sup>15</sup>

The simulation exercise is carried out as the previous ones were by drawing 100 samples for each DGP and three different sample sizes: 500, 1000 and 5000 individuals. We consider durations longer than 40 periods as being censored.

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<sup>14</sup>Mroz (2008) considers this identification problem for sequential binary models with unobserved heterogeneity used to estimate count models with only one observed count for each individual. These models are analytically equivalent to the single-spell discrete duration models with unobserved heterogeneity that are considered in this paper.

<sup>15</sup>An alternative estimation method is the simulated maximum likelihood. See Gourieroux and Monfort (1996) and Train (2003).

### 3.3 Results

This section provides the results of the effects of misspecifying the unobserved heterogeneity or the residual error distribution.

Tables 2, 3 and 4 report the average and the standard deviation over 100 replications for the two covariate (mixture variable) coefficients,  $\beta_1$  (which true value is 1) and  $\beta_2$  (which true value is 0.5), their ratio  $\beta_1/\beta_2$ , the fraction of residual variance explained by individual random effects ( $\rho$ ), the average number of iterations and the number of cases out of 100 of successful convergence of the maximum likelihood algorithm.<sup>16</sup> Each Table considers a different estimation model (sequential logit, probit or complementary log-log) and is divided into three panels reporting results produced using three different sample sizes: 500, 1000 and 5000 observations. The simulated data used in all three Tables are generated from the same DGP: a sequential logit model with negative duration dependence and unobserved heterogeneity following three alternative distributions (discrete with two mass points, gamma and normal that are labeled “Discrete UH”, “Gamma UH” and “Normal UH”).

Looking at the results in Table 2, where both estimation and simulated models are sequential logit models, the covariate coefficients do not seem to be underestimated. They seem to be well estimated even when the unobserved heterogeneity is erroneously assumed to follow a normal distribution instead of a gamma or a discrete distribution. This is an encouraging result for practitioners who would like to use easy-to-implement estimation methods to take account of unobserved heterogeneity.

In Table 3, where the estimation model is given by a sequential probit model while the true DGPs are sequential logit models, the two covariate coefficients are underestimated but their ratio is still unbiased. Again we do not find relevant differences when considering DGPs with different distributions for the random effects.

Finally, in Table 4 we change the estimation model to a sequential complementary log-log model. The two covariate coefficients seem to be slightly underestimated while the ratio between them is unbiased. The coefficients seem slightly lower than the ones shown in Table 2 and the bias is reduced again to a rescaling. The results are not affected by the distribution

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<sup>16</sup>We report averages and standard deviations only for cases where convergence was achieved.

assumed for the unobserved heterogeneity in the DGPs.

Increasing the sample size has the same effect for all three types of models (logit, probit and complementary log-log): the attenuation bias does not change significantly, the standard deviations decrease, and the number of unsuccessful convergence cases is reduced to zero.

The fraction of the residual variance explained by the individual unobserved heterogeneity,  $\rho$ , seems very slightly and insignificantly underestimated when using sequential logit or complementary log-log models, and it is more significantly underestimated when considering a sequential probit. Note that a higher underestimation of the  $\rho$  coefficient seems to be associated with a higher attenuation bias for the coefficients. This seems to confirm Baker and Melino’s (2000) conclusion that an underestimation (overestimation) of the dispersion of the unobserved heterogeneity leads to an attenuation (amplification) of the covariate coefficients. However, we conclude that this attenuation (amplification) bias is a consequence of the covariate coefficient normalization.

To evaluate the effect on the duration dependence estimation of misspecifying the unobserved heterogeneity distribution, we plot true and estimated baseline hazard functions (see Figure 2). The estimated baseline hazards are predicted fixing the covariates and random effects at their mean values and using the estimated coefficients (average across 100 replications) of a sequential logit (panel a), probit (panel b), and complementary log-log (panel c) model with normal random effects. The true baseline hazard is computed using the simulation model, which is a sequential logit model with covariates and random effects fixed at their mean values and coefficients fixed at their simulated values (see simulation exercise **A3** for details). For each panel there are three estimated baseline hazards corresponding to the three different types of simulated unobserved heterogeneity (labeled “Discrete UH”, “Gamma UH” and “Normal UH”). Since the true baseline hazard is computed fixing the random effect at its mean, the true baseline does not depend on the simulated distribution for the unobserved heterogeneity term.

In panel (a) Figure 2, where both estimated and simulated models are given by a sequential logit, the true baseline hazard has a profile similar to the three estimated baseline hazards.

When we change the estimation model to a sequential probit as in Figure 2 panel (b), the

estimated baseline hazards have a slightly different profile with respect to the true baseline hazard but they are similar for short durations.

Finally, when using a sequential complementary log-log model to estimate the duration model (see Figure 2, panel c), we find that the profile of the estimated baseline hazards follows the true one.

In Table 6, we study the difference between the true and estimated survival function (expected duration), as well as the true and estimated effects of changes in the covariate  $X_1$  on the survival function (expected duration). The expected duration is given by  $E(TI_{T \leq 40} | X_1, X_2 = 0, \theta = 1.8)$ , while the survival function is given by  $\Pr(T > t | X_1, X_2 = 0, \theta = 1.8)$  and is computed at  $t = 5$  and 10.

Both the survival function and the expected duration value are computed fixing the variable  $X_2$  and the unobserved heterogeneity at their means (zero and 1.8 respectively) and the variable  $X_1$  at three different values, its mean and its mean plus or minus half its standard deviation. We consider again the DGPs in simulation exercise **A3**. The estimation models are either sequential logit models, panel (a); or sequential probit models, panel (b); or sequential complementary log-log models, panel (c); simulated unobserved heterogeneity distributions (labeled “Discrete UH”, “Gamma UH” and “Normal UH”).

The survival function at low durations seems to be well estimated. Furthermore, differences between true and estimated effects of changes in the variable  $X_1$  on the survival function are never higher than 7%, at durations of 5, and of 10% at durations of 10.

The true and estimated expected duration values are close and the effects of changes in covariates on the expected duration have a correct sign and are quite well estimated. These covariate effects seem to be better estimated than when computed using non-parametric maximum likelihood estimation and adopting the Hannan-Quinn Information Criterion suggested by Baker and Melino (2000) (see Mroz and Zayats, 2008, Table 2).

In summary, the misspecification of the unobserved heterogeneity distribution does not seriously affect the estimation results. Changes in the error distribution (logistic, normal and extreme value) bias the duration dependence estimation but cause only a rescaling of the coefficients. Furthermore, the estimated effects of changes in  $X_1$  on the survival function and expected duration have a correct sign and are relatively close to the true ones.

## 4 Conclusions

In this paper we assess the consequences of estimating single-spell discrete duration models by adopting two types of models that can be easily estimated using standard software: sequential binary models with or without individual normal random effects.

When using a sequential binary model neglecting the unobserved heterogeneity we find that the duration dependence is underestimated, but the covariate coefficients are consistently estimated up to a scale factor. Applied researchers should not be concerned about the rescaling factor because all binary models have coefficients that are identified only up to a scale. We find that the rescaling factor could change slightly across types of variables, but even in this case we can still make a correct inference on the statistical significance of each covariate and compare the significance across variables. Neglecting the unobserved heterogeneity does not cause any relevant bias in estimating the survival and expected duration functions and in evaluating the effect of changes in the covariates on these two functions.

An incorrect normality assumption for the unobserved heterogeneity distribution biases neither the duration dependence nor the covariate coefficients estimation. On the other hand, misspecifying the error distribution, assuming a normal or an extreme value distribution instead than a logistic one, seems to cause a slight bias in the duration dependence estimation but only a proportional rescaling of the covariate coefficients. Again, there are no major biases in estimating the survival (at least at low durations) and expected duration functions and in predicting the effect of covariate changes on these two functions.

These findings are very encouraging for the practitioner who would like to adopt sequential binary models (with or without normal random effects) because they are easy to estimate using conventional statistical software. These models allow empirical researchers to correctly answer the main research questions addressed in survival analysis, but not the ones on the duration dependence.

The strategy used in this paper to study the consequences of omitting or misspecifying the unobserved heterogeneity can be easily extended to more general data generator processes. We leave these possible extensions for future research.

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**Table 1: Means and standard deviations of the coefficients estimates over 100 samples. Monte Carlo exercise A.**

DGP	500 Observations						1000 Observations					
	Step DD			Polynomial DD			Step DD			Polynomial DD		
	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$
True Value	1	0.5	2	1	0.5	2	1	0.5	2	1	0.5	2
<i>Time-varying covariates, A1</i>												
<i>Negative duration dependence</i>												
Discrete UH	0.896	0.446	2.061	0.892	0.445	2.058	0.934	0.473	1.999	0.932	0.472	1.998
(sd)	0.151	0.073	0.479	0.148	0.072	0.471	0.092	0.052	0.302	0.091	0.051	0.300
Gamma UH	0.967	0.464	2.144	0.963	0.462	2.146	0.951	0.478	2.015	0.948	0.477	2.015
(sd)	0.147	0.074	0.505	0.146	0.074	0.505	0.086	0.052	0.300	0.085	0.051	0.299
Normal UH	0.922	0.459	2.081	0.919	0.457	2.082	0.928	0.474	1.978	0.926	0.473	1.979
(sd)	0.158	0.087	0.526	0.158	0.086	0.526	0.099	0.050	0.296	0.099	0.049	0.295
<i>Positive duration dependence</i>												
Discrete UH	0.903	0.444	2.086	0.900	0.442	2.090	0.911	0.458	2.014	0.909	0.457	2.015
(sd)	0.142	0.070	0.472	0.142	0.069	0.469	0.090	0.053	0.308	0.090	0.053	0.307
Gamma UH	0.927	0.454	2.106	0.922	0.450	2.109	0.911	0.456	2.023	0.908	0.455	2.021
(sd)	0.152	0.074	0.531	0.148	0.072	0.525	0.107	0.057	0.306	0.107	0.056	0.306
Normal UH	0.895	0.446	2.047	0.891	0.443	2.051	0.905	0.464	1.977	0.903	0.463	1.977
(sd)	0.167	0.073	0.459	0.165	0.072	0.457	0.095	0.053	0.319	0.095	0.052	0.321
<i>Time-invariant covariates, A2</i>												
<i>Negative duration dependence</i>												
Discrete UH	0.662	0.326	2.168	0.664	0.326	2.168	0.678	0.315	2.250	0.680	0.316	2.248
(sd)	0.147	0.077	0.790	0.147	0.077	0.787	0.112	0.060	0.675	0.112	0.060	0.672
Gamma UH	0.672	0.334	2.121	0.673	0.334	2.122	0.659	0.328	2.082	0.660	0.329	2.081
(sd)	0.144	0.075	0.688	0.145	0.075	0.687	0.104	0.061	0.533	0.104	0.061	0.530
Normal UH	0.730	0.350	2.277	0.731	0.350	2.274	0.684	0.341	2.051	0.685	0.341	2.051
(sd)	0.141	0.084	1.167	0.140	0.084	1.148	0.102	0.050	0.432	0.101	0.050	0.432
<i>Positive duration dependence</i>												
Discrete UH	0.740	0.355	2.161	0.739	0.354	2.167	0.726	0.351	2.113	0.724	0.350	2.113
(sd)	0.141	0.070	0.551	0.142	0.070	0.559	0.102	0.051	0.435	0.102	0.051	0.437
Gamma UH	0.625	0.316	2.075	0.622	0.314	2.075	0.613	0.303	2.105	0.611	0.303	2.105
(sd)	0.132	0.067	0.654	0.133	0.066	0.660	0.099	0.058	0.588	0.099	0.058	0.588
Normal UH	0.709	0.342	2.194	0.707	0.341	2.192	0.660	0.340	1.985	0.659	0.339	1.986
(sd)	0.136	0.082	0.681	0.136	0.081	0.677	0.102	0.052	0.427	0.102	0.052	0.428
<i>Mixture covariates, A3</i>												
<i>Negative duration dependence</i>												
Discrete UH	0.789	0.390	2.114	0.788	0.390	2.117	0.809	0.399	2.068	0.809	0.399	2.069
(sd)	0.154	0.083	0.636	0.153	0.083	0.638	0.113	0.058	0.418	0.114	0.058	0.419
Gamma UH	0.810	0.408	2.077	0.807	0.407	2.077	0.794	0.404	2.005	0.793	0.403	2.007
(sd)	0.159	0.082	0.637	0.159	0.083	0.635	0.115	0.056	0.414	0.114	0.056	0.414
Normal UH	0.811	0.402	2.087	0.808	0.401	2.086	0.810	0.402	2.056	0.810	0.401	2.057
(sd)	0.148	0.073	0.546	0.148	0.073	0.548	0.105	0.058	0.386	0.106	0.058	0.388
<i>Positive duration dependence</i>												
Discrete UH	0.828	0.410	2.082	0.824	0.408	2.084	0.835	0.416	2.044	0.833	0.414	2.048
(sd)	0.157	0.079	0.534	0.157	0.078	0.537	0.101	0.054	0.391	0.102	0.054	0.398
Gamma UH	0.791	0.390	2.110	0.787	0.387	2.113	0.761	0.375	2.074	0.759	0.374	2.073
(sd)	0.141	0.074	0.598	0.141	0.074	0.593	0.109	0.055	0.419	0.108	0.055	0.422
Normal UH	0.796	0.393	2.083	0.792	0.391	2.086	0.786	0.393	2.025	0.785	0.392	2.027
(sd)	0.153	0.067	0.553	0.153	0.067	0.557	0.102	0.053	0.313	0.102	0.053	0.313

Note: Characteristics of the DGPs (data generator processes) and of the estimation models are given by row and by column.

UH = unobserved heterogeneity. DD = duration dependence. Step = step function. Polynomial = cubic polynomial function.

**Table 2: Means and standard deviations of coefficient estimates over 100 samples. Estimation model: sequential logit. DGP: sequential logit.**

	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$	$\rho = \frac{\sigma_\theta^2}{\sigma_\epsilon^2 + \sigma_\theta^2}$	Iterations	Convergence
<i>True Value</i>	1	0.5	2	$\frac{1}{\frac{\pi^2}{3} + 1} = 0.233$		
<i>DGP</i>						
<i>500 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.927 (0.170)	0.455 (0.093)	2.130 (0.611)	0.174 (0.143)	6.908 (2.981)	98
Gamma UH	0.913 (0.183)	0.452 (0.087)	2.110 (0.672)	0.118 (0.072)	5.404 (2.263)	99
Normal UH	0.923 (0.158)	0.460 (0.086)	2.083 (0.550)	0.148 (0.116)	6.271 (2.759)	96
<i>1000 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.937 (0.137)	0.462 (0.071)	2.069 (0.405)	0.156 (0.093)	6.424 (2.607)	99
Gamma UH	0.942 (0.123)	0.474 (0.060)	2.012 (0.317)	0.151 (0.090)	5.889 (2.788)	99
Normal UH	0.944 (0.121)	0.470 (0.066)	2.048 (0.393)	0.170 (0.118)	6.316 (2.775)	98
<i>5000 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.956 (0.079)	0.477 (0.040)	2.013 (0.178)	0.202 (0.099)	6.850 (2.851)	100
Gamma UH	0.916 (0.064)	0.458 (0.027)	2.003 (0.163)	0.110 (0.059)	4.190 (1.522)	100
Normal UH	0.966 (0.076)	0.482 (0.034)	2.009 (0.161)	0.188 (0.102)	5.850 (2.455)	100

*Note:* Iterations = average number of iterations for the convergence of the likelihood maximization algorithm. Convergence = number of cases over 100 replications of successful convergence.  $\rho$  = fraction of residual variance explained by individual random effects.

**Table 3: Means and standard deviations of coefficient estimates over 100 samples. Estimation model: sequential probit. DGP: sequential logit.**

<i>True Value</i>	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$	$\rho = \frac{\sigma_\theta^2}{\sigma_\epsilon^2 + \sigma_\theta^2}$	Iterations	Convergence
<i>DGP</i>	1	0.5	2	$\frac{1}{1+1} = 0.5$		
<i>500 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.519 (0.099)	0.255 (0.058)	2.128 (0.587)	0.306 (0.140)	8.690 (1.495)	100
Gamma UH	0.543 (0.102)	0.270 (0.049)	2.069 (0.522)	0.307 (0.126)	8.535 (1.358)	99
Normal UH	0.528 (0.102)	0.264 (0.058)	2.089 (0.566)	0.304 (0.157)	8.455 (2.370)	99
<i>1000 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.525 (0.082)	0.257 (0.039)	2.078 (0.407)	0.292 (0.104)	8.848 (1.480)	99
Gamma UH	0.534 (0.087)	0.270 (0.039)	2.013 (0.396)	0.305 (0.112)	8.410 (1.326)	100
Normal UH	0.537 (0.079)	0.268 (0.041)	2.049 (0.407)	0.324 (0.124)	8.760 (1.457)	100
<i>5000 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.524 (0.036)	0.261 (0.017)	2.015 (0.174)	0.311 (0.044)	9.010 (1.259)	100
Gamma UH	0.542 (0.037)	0.271 (0.015)	2.004 (0.159)	0.305 (0.042)	8.740 (0.960)	100
Normal UH	0.538 (0.038)	0.268 (0.016)	2.010 (0.161)	0.315 (0.049)	8.850 (1.175)	100

*Note:* Iterations = average number of iterations for the convergence of the likelihood maximization algorithm. Convergence = number of cases over 100 replications of successful convergence.  $\rho$  = fraction of residual variance explained by individual random effects.

**Table 4: Means and standard deviations of coefficient estimates over 100 samples. Estimation model: sequential complementary log-log. DGP: sequential logit.**

	$\beta_1$	$\beta_2$	$\beta_1/\beta_2$	$\rho = \frac{\sigma_\theta^2}{\sigma_\epsilon^2 + \sigma_\theta^2}$	Iterations	Convergence
<i>True Value</i>	1	0.5	2	$\frac{1}{\frac{\pi^2}{6} + 1} = 0.378$		
<i>DGP</i>						
<i>500 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.855 (0.147)	0.421 (0.086)	2.123 (0.606)	0.243 (0.127)	6.714 (2.428)	98
Gamma UH	0.861 (0.156)	0.442 (0.072)	2.010 (0.545)	0.222 (0.112)	5.890 (2.238)	100
Normal UH	0.859 (0.152)	0.430 (0.081)	2.076 (0.556)	0.224 (0.130)	6.358 (2.475)	95
<i>1000 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.871 (0.123)	0.429 (0.062)	2.069 (0.410)	0.233 (0.094)	6.602 (2.560)	98
Gamma UH	0.886 (0.107)	0.432 (0.051)	2.084 (0.381)	0.228 (0.084)	5.730 (2.348)	100
Normal UH	0.879 (0.109)	0.437 (0.062)	2.053 (0.386)	0.250 (0.131)	6.240 (2.590)	100
<i>5000 Observations:</i>						
<i>Negative duration dependence:</i>						
Discrete UH	0.882 (0.058)	0.440 (0.029)	2.013 (0.178)	0.285 (0.089)	6.710 (2.388)	100
Gamma UH	0.878 (0.054)	0.438 (0.028)	2.011 (0.160)	0.224 (0.075)	5.310 (2.246)	100
Normal UH	0.901 (0.060)	0.450 (0.027)	2.008 (0.161)	0.287 (0.097)	6.290 (2.262)	100

*Note:* Iterations = average number of iterations for the convergence of the likelihood maximization algorithm. Convergence = number of cases over 100 replications of successful convergence.  $\rho$  = fraction of residual variance explained by individual random effects.

**Table 5: True and estimated expected duration and survival function. True and estimated effects of  $X_1$  on expected duration and survival function.**

DGP	$Pr(T > t X_1, X_2 = 0)$												Impact of $X_1$ on $Pr(T > t X_1, X_2 = 0)$							
	at $X_1 = -0.5\sigma$				at $X_1 = 0$				at $X_1 = 0.5\sigma$				From $X_1 = 0$ to $X_1 = 0.5\sigma$				From $X_1 = -0.5\sigma$ to $X_1 = 0$			
	t=5		t=10		t=5		t=10		t=5		t=10		t=5		t=10		t=5		t=10	
	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR
Negative Dur.																				
Discrete	0.47	0.48	0.34	0.35	0.52	0.52	0.39	0.39	0.57	0.56	0.45	0.43	0.05	0.04	0.06	0.04	0.05	0.04	0.06	0.04
Gamma	0.46	0.47	0.32	0.33	0.51	0.51	0.37	0.37	0.57	0.56	0.43	0.42	0.05	0.05	0.06	0.05	0.05	0.05	0.06	0.04
Normal	0.47	0.51	0.33	0.38	0.53	0.55	0.39	0.43	0.58	0.60	0.45	0.47	0.05	0.04	0.06	0.04	0.05	0.04	0.06	0.04
Positive Dur.																				
Discrete	0.34	0.34	0.14	0.15	0.39	0.38	0.18	0.18	0.45	0.42	0.23	0.22	0.05	0.04	0.05	0.03	0.05	0.04	0.04	0.03
Gamma	0.32	0.33	0.12	0.13	0.37	0.37	0.16	0.16	0.42	0.42	0.21	0.19	0.05	0.04	0.05	0.03	0.05	0.04	0.04	0.03
Normal	0.33	0.37	0.13	0.16	0.38	0.41	0.17	0.19	0.44	0.45	0.21	0.23	0.05	0.04	0.05	0.03	0.05	0.04	0.04	0.03
DGP	$E(TI_{T \leq 40} X_1, X_2 = 0)$												Effect of $X_1$ on $E(TI_{T \leq 40} X_1, X_2 = 0)$							
	at $X_1 = -0.5\sigma$		at $X_1 = 0$		at $X_1 = 0.5\sigma$		From $X_1 = 0$ to $X_1 = 0.5\sigma$		From $X_1 = -0.5\sigma$ to $X_1 = 0$											
	ES	TR	ES	TR	ES	TR	ES	TR	ES	TR										
Negative Dur.																				
Discrete	6.71	6.61	6.89	6.70	6.92	6.78	0.03	0.08	0.18	0.09										
Gamma	6.73	6.56	6.99	6.96	7.10	7.33	0.11	0.37	0.26	0.40										
Normal	7.05	7.13	7.31	7.37	7.41	7.53	0.10	0.16	0.26	0.23										
Positive Dur.																				
Discrete	5.41	5.41	6.22	6.06	7.12	6.74	0.90	0.69	0.81	0.65										
Gamma	5.04	5.35	5.65	5.87	6.23	6.41	0.59	0.55	0.60	0.52										
Normal	5.24	5.81	5.93	6.36	6.65	6.93	0.72	0.57	0.70	0.55										

*Note:* ES= estimated, TR= true.  $I_{T \leq 40}$  denotes the indicator function.  $\sigma$  is the standard deviation of  $X_1$  whose mean is zero. Sample size: 5000. Estimated cubic polynomial duration dependence.

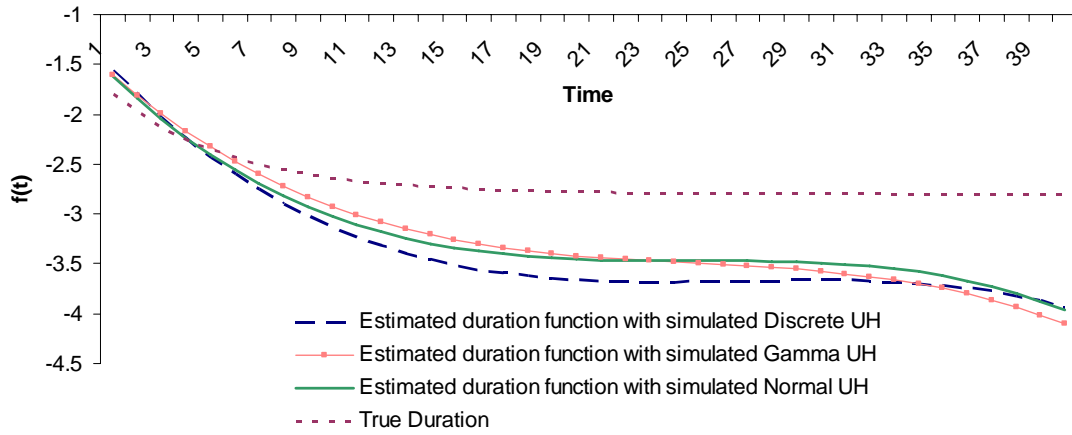
**Table 6: True and estimated expected duration and survival function. True and estimated effects of  $X_1$  on expected duration and survival function.**

	$Pr(T > t X_1, X_2 = 0, \theta = 1.8)$						Effect of $X_1$ on $Pr(T > t X_1, X_2 = 0, \theta = 1.8)$			
	at $X_1 = -0.5\sigma$		at $X_1 = 0$		at $X_1 = 0.5\sigma$		From $X_1 = 0$ to $X_1 = 0.5\sigma$		From $X_1 = -0.5\sigma$ to $X_1 = 0$	
	t=5	t=10	t=5	t=10	t=5	t=10	t=5	t=10	t=5	t=10
True	0.50	0.32	0.56	0.38	0.61	0.44	0.05	0.06	0.06	0.06
	(a) Sequential logit									
Discrete UH	0.49	0.32	0.54	0.38	0.59	0.44	0.05	0.06	0.05	0.06
Gamma UH	0.47	0.31	0.52	0.36	0.57	0.42	0.05	0.06	0.05	0.06
Normal UH	0.49	0.32	0.55	0.38	0.60	0.44	0.05	0.06	0.05	0.06
	(b) Sequential probit									
Discrete UH	0.48	0.28	0.53	0.34	0.59	0.41	0.05	0.06	0.06	0.06
Gamma UH	0.47	0.25	0.53	0.31	0.58	0.38	0.06	0.06	0.06	0.06
Normal UH	0.49	0.28	0.54	0.34	0.60	0.40	0.06	0.07	0.06	0.06
	(c) Sequential complementary log-log									
Discrete UH	0.50	0.33	0.55	0.39	0.60	0.45	0.05	0.06	0.05	0.06
Gamma UH	0.50	0.33	0.56	0.39	0.61	0.45	0.05	0.06	0.05	0.06
Normal UH	0.50	0.33	0.56	0.39	0.61	0.44	0.05	0.06	0.05	0.06
	$E(TI_{T \leq 40} X_1, X_2 = 0, \theta = 1.8)$						Effect of $X_1$ on $E(TI_{T \leq 40} X_1, X_2 = 0, \theta = 1.8)$			
	at $X_1 = -0.5\sigma$		at $X_1 = 0$		at $X_1 = 0.5\sigma$		From $X_1 = 0$ to $X_1 = 0.5\sigma$		From $X_1 = -0.5\sigma$ to $X_1 = 0$	
True	8.35		9.15		9.76		0.61		0.80	
	(a) Sequential logit									
Discrete UH	8.04		8.61		8.99		0.38		0.57	
Gamma UH	7.54		8.04		8.36		0.33		0.49	
Normal UH	8.21		8.89		9.37		0.48		0.67	
	(b) Sequential probit									
Discrete UH	8.09		9.12		10.04		0.92		1.03	
Gamma UH	7.56		8.64		9.71		1.06		1.08	
Normal UH	8.00		9.13		10.22		1.09		1.13	
	(c) Sequential complementary log-log									
Discrete UH	8.03		8.55		8.88		0.33		0.51	
Gamma UH	7.97		8.46		8.77		0.31		0.49	
Normal UH	8.29		8.94		9.40		0.46		0.65	

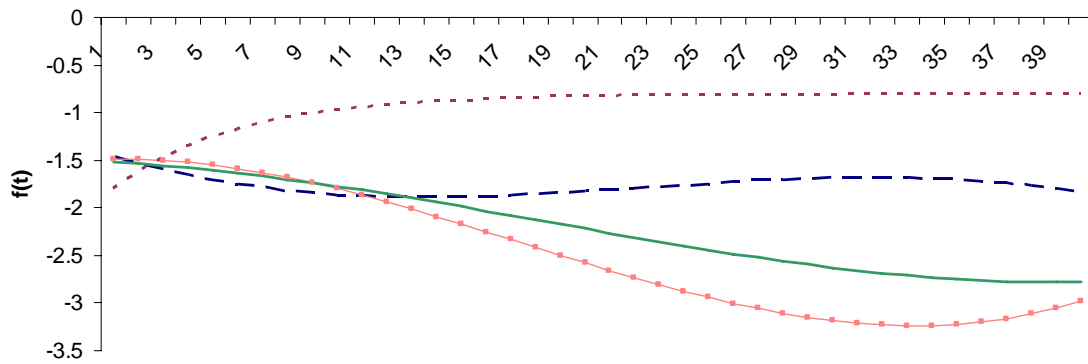
*Note:* UH= Unobserved Heterogeneity.  $I_{T \leq 40}$  denotes the indicator function.  $\sigma$  is the standard deviation of  $X_1$  whose mean is zero. Sample size: 5000. (a), (b), (c) define three different estimated models and data simulated with Discrete UH, Gamma UH and Normal UH.



Figure 1: Estimated and true negative/positive duration dependence functions. Monte Carlo exercise A1. Unobserved heterogeneity ignored. Sample size: 1000.

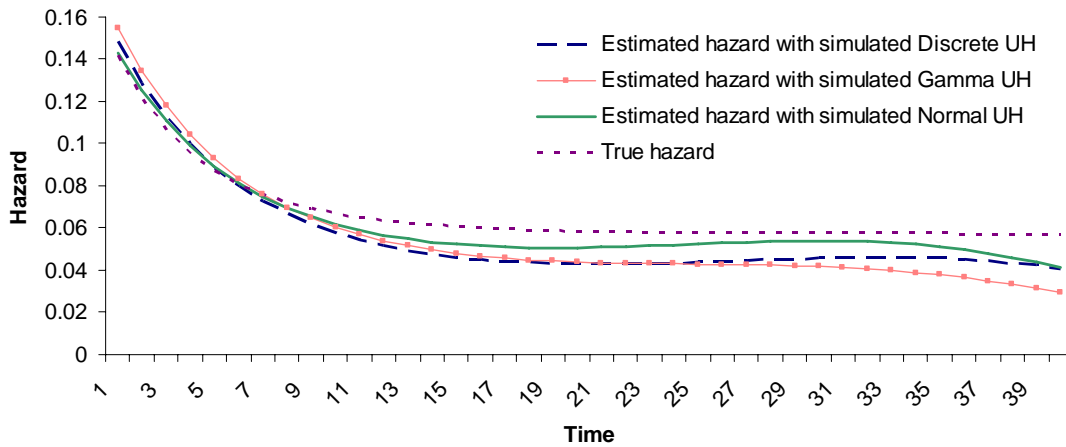


(a) negative duration dependence

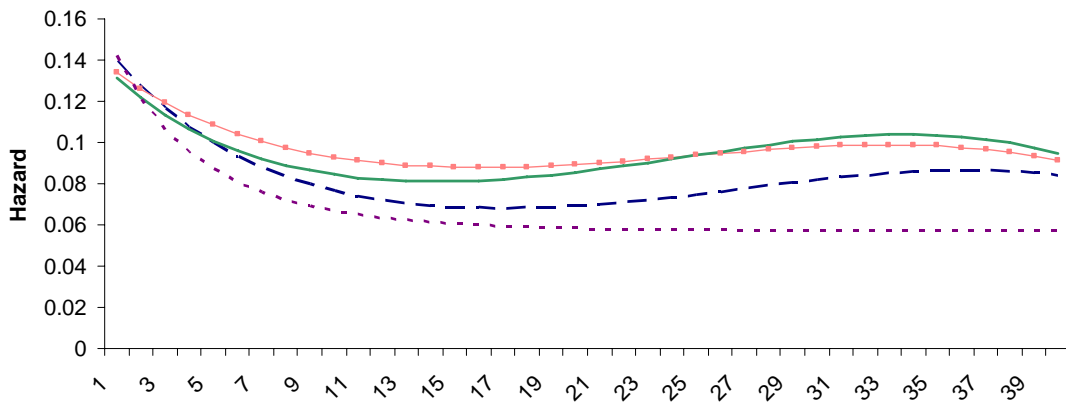


(b) positive duration dependence

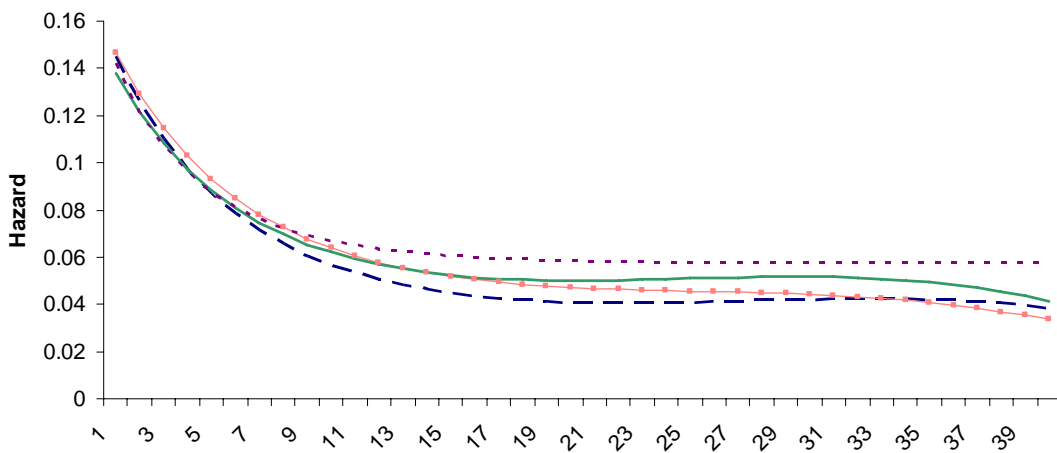
Figure 2: Estimated and true baseline hazards. DGP: sequential logit with unobserved heterogeneity. Estimation model: sequential logit/probit/cloglog with normal random effect. Sample size: 5000.



(a) Sequential logit



(b) Sequential probit



(c) Sequential complementary log-log

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