

## Forecasting US Birth Rates with Google Trends

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# Outline

- Data and Determinants for US fertility
- Short-Term emphasis
- New Leading indicators
- Forecasting models
- Out-of-sample evaluation
- Some robustness (state level)

# Motivation

- A simple Supply-Side Decomposition
- Macro-based accounting framework

$$GDP_t = \frac{GDP_t}{Hours_t} \times \frac{Hours_t}{Workers_t} \times \frac{Workers_t}{LaborForce_t} \times \frac{LaborForce_t}{Population_t} \times Population_t$$

The diagram illustrates the decomposition of GDP into three components. The equation is shown with curly braces underneath each fraction, and a box below each brace containing a label. The first brace is under  $\frac{GDP_t}{Hours_t}$  and labeled "Efficiency in production". The second brace is under  $\frac{Hours_t}{Workers_t} \times \frac{Workers_t}{LaborForce_t}$  and labeled "Labor market developments". The third brace is under  $\frac{LaborForce_t}{Population_t} \times Population_t$  and labeled "Demographic developments".

- We concentrate on the last part (demographic developments)

# Motivation

- Fertility is the major component of population dynamics
- The size and structure of population is entirely dependent on fertility
- Trends in fertility are the most difficult demographic variable to project
- Fertility rates represent the most important modeling variable in any population model
- These models are of critical importance
- Forecasts of births and birth rates are fundamental to forecasts of future population sizes (Keyfitz, 1972).
- Yet the forecasting of births and birth rates, even in highly developed countries has proven to be quite difficult to do

# Introduction

- Demographers model long-run fertility (see for example Booth, IJF, 2006, for a review)
- However short-term perspective is useful to spot diverging trends (for example to assess the impact on births of a crisis)
- Our approach:
  - Pure time series models with leading indicators:
  - GDP, Unemployment rate dynamics (Goldstein et al., PDR, 2009)
  - We also add Economic Policy Uncertainty (EPU) index by Baker, Bloom, and Davis (2016) as an additional leading factor affecting birth rates
- For a shorter sample (from 2004 onwards) we suggest using Google Index based on Google Trends: fertility-related web searches (in different contexts: Choi and Varian, 2009; D'Amuri and Marcucci, 2017; Ginsberg et al., 2009, Da, Engelberg, and Zha, 2011, etc.)

# Forecasting the US Birth Rates Using Google - Preview

- We predict the US Birth Rates using:
  - Traditional macro indicators:
    - GDP
    - UR
  - New web-based indicators:
    - EPU (Economic Policy Uncertainty) Index by Baker, Bloom and Davis (2016)
    - Google Trends indicators
  - We find forecasting improvements with both web-based indicators

# “The Social Science (Big) Data Revolution” (Gary King)

- “Between the dawn of civilization and 2003, we only created five exabytes of information; now we’re creating that amount every two days” (1 exabyte =  $2^6$  bytes  $\approx 1.15 \times 10^{18}$  bytes, i.e.  $10^9$ GB)
- “In 2010 human race created 800 exabytes of information” (around 800 billion gigabytes,  $1\text{GB} = 10^9$  bytes)
- 90% of the world’s data was created in the last 2 years
- Most of the World’s Data is **Unstructured**
  - 2009 HP survey: 70%
  - Gartner: 80%
  - Jerry Hill (Teradata), Anant Jhingran (IBM): 85%
- “There’s a systemic gap between the low-frequency data employed by governments and the **high-frequency data of business**’ (Hal Varian, Google)’
- “Data is like food. We used to be **data poor**, now the problem is **data obesity**’ (Hal Varian, Google)’

# Big Data

One of the 3 V's: **Variety**: Different sources, different types

## Define **BIG DATA**



## Google Trends data

- *Google Trends* (previously separated from *Google Insights for Search*) tracks relative changes in Google search queries from January 2004
- Google search queries
  - web searches
  - news searches
  - image searches
  - product searches
  - YouTube searches
- Different Geographical areas and levels (national, state and metropolitan area level) based on the originating IP address
- Available to the public for free download online at [www.google.com/trends/](http://www.google.com/trends/)

## Features of *Google Trends* data

- Google Trends data represent **how many web searches** are done for a particular *keyword*, relative to the total # of searches in certain geographical area over time
- indicate the **likelihood of a random user to search for a particular keyword on Google** from a certain location at a certain time on a relative basis
- are gathered **using IP address information** from Google logs and **updated daily**
- are gathered only if the number of searches exceeds a certain **threshold of traffic**
- are such that **repeated queries** from a single user/IP over a short period of time are eliminated
- are **available world-wide** (by country, by region, by city)
- are **normalized** (divided by the total website traffic in the geographical area) ⇒ comparability issues ⇒ Search Volume Index (*SVI*)
- are **scaled** (from 0 to 100) dividing each data point by the maximum
- available **monthly, weekly, daily**, and **intra-daily** (only on shorter samples)

## Aggregation, Normalization and Scaling

- For region  $r$ , the SVI for week  $\tau$  is constructed aggregating the daily data for each day  $t$ . Given the search volume on a term “V”,  $(V_{t,r})$  in region  $r$  on day  $t$  and the total search volume in that region  $T_{t,r}$  we have the following for a total of  $T$  weeks
- Search Share for day  $t$  and week  $\tau$ :

$$S_{t,r} = \frac{V_{t,r}}{T_{t,r}} \quad \text{and} \quad S_{\tau,r} = \frac{1}{7} \sum_{t=Sunday}^{Saturday} S_{t,r}$$

- Web Search Volume for week  $\tau$ :

$$S_{\tau,r}^* = \frac{100}{\max_{\tau}(\mathbf{S}_{\tau,r})} \frac{1}{7} \sum_{t=Sunday}^{Saturday} S_{t,r}$$

where  $\tau = 1, \dots, T$

# Matching options for “fertility”-related web queries in Google Trends

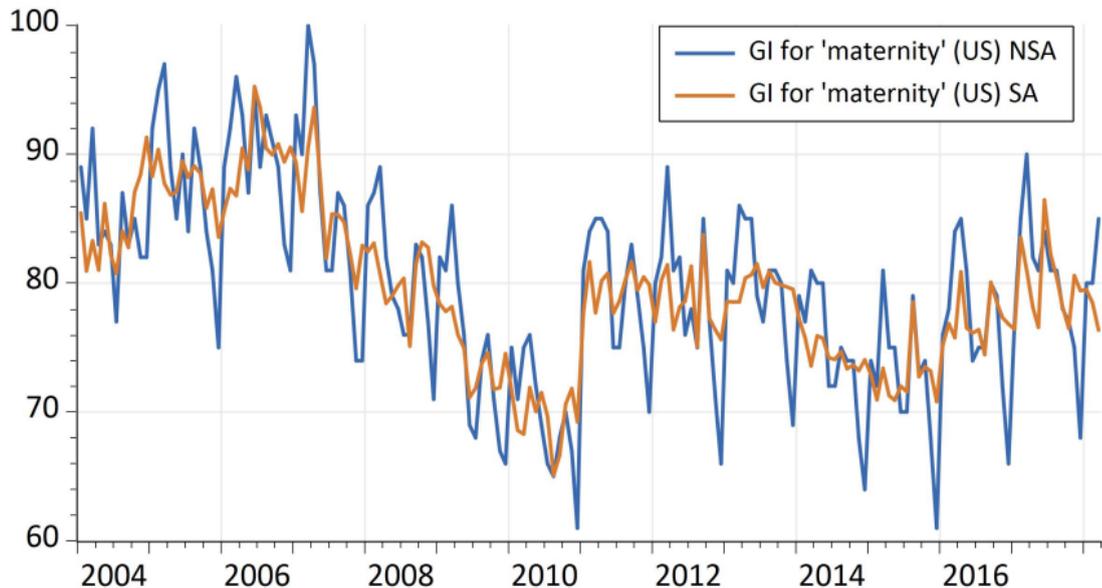
- typing `maternity leave`: GI includes searches containing both `maternity` and `leave` in any order and along with additional terms before (e.g. `using short term disability for maternity leave`) and after (e.g. `maternity leave replacement`)
- typing `"pregnancy test"`: GI includes searches with that specific order in quotes along with additional terms before and after (e.g. `"pregnancy test" calculator`)
- typing `"ovulation" + "pregnancy test"`: GI includes searches with either `"ovulation"` or `"pregnancy test"`, but not both

## Which **keyword(s)** to forecast birth rates?

- We tried to imagine what an average American internet user who wanted to have children would type in the Google bar. For example:
  - 'maternity'
  - 'pregnancy'
  - 'ovulation'

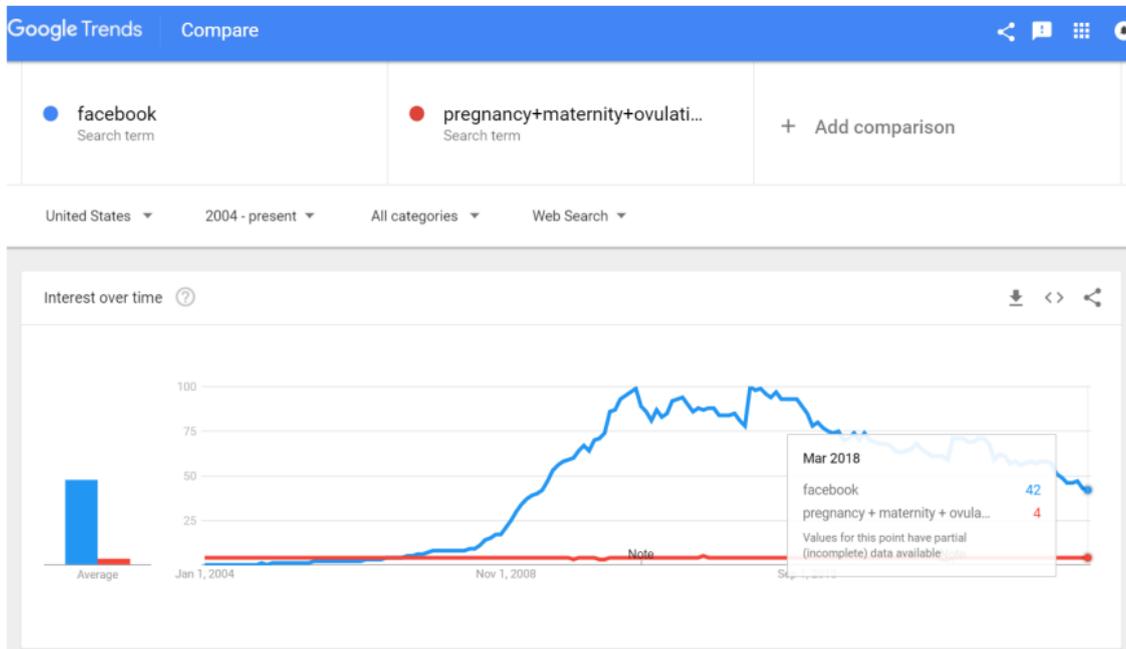
# Peculiar seasonality

Monthly Google index for "maternity" - Sample: Jan. 2004 - Mar. 2018



# Relevance of our preferred keyword?

Incidence of keywords "maternity" + "pregnancy" + "ovulation" vs other popular keywords  
"facebook" (**highest incidence**)



# Economic Policy Uncertainty

How is it built by Baker, Bloom and Davis (2016)?

- Counting articles from newspapers containing (E)conomic, (P)olicy and (U)ncertainty words

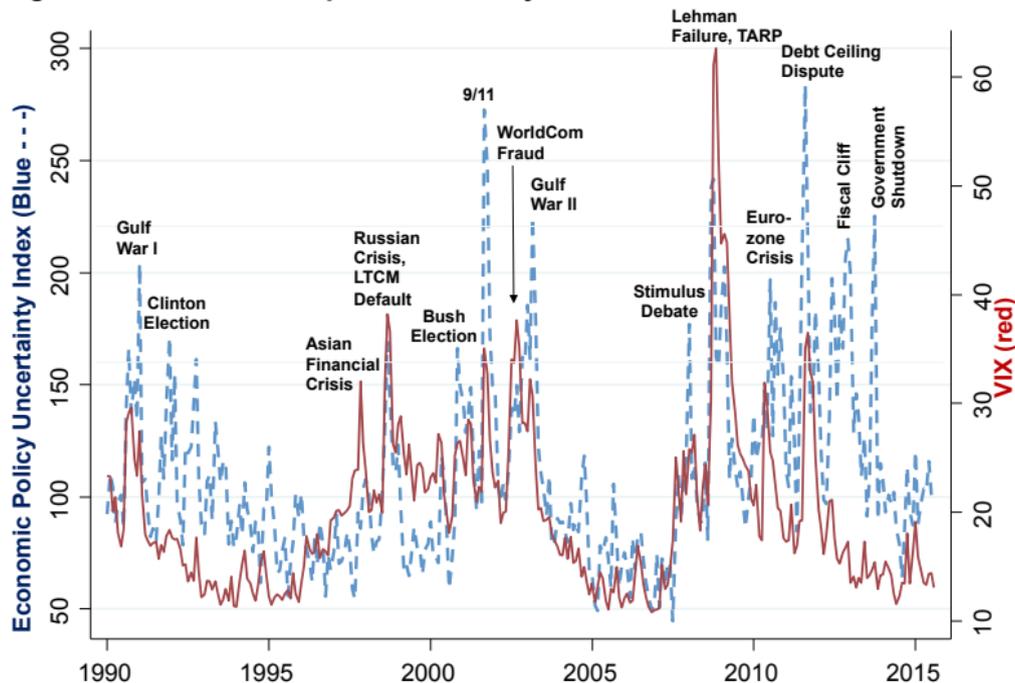
(E) “economic” or “economy”;

(U) “uncertain” or “uncertainty”;

(P) “congress”, “deficit”, “Federal Reserve”, “legislation”, “regulation” or “White House”

# US Economic Policy Uncertainty (EPU) index vs VIX

Figure 6: U.S. EPU Compared to 30-Day VIX



Notes: The figure shows the U.S. EPU Index from Figure 1 and the monthly average of daily values for the 30-day VIX.

## The setup of the forecasting horse-race

- **Timing:**  $T = R + P$  observations
  - In the '**Long sample**' (1990.1-2013.12) we have  $T = 288$
  - In the '**Short sample**' (2004.1-2013.12) we have  $T = 120$
- The first  $R$  are used to estimate the models (**in-sample**) while the last  $P$  are used for **out-of-sample** evaluation.
- Want to predict  $u_t$  using linear AR models w/ and w/o exogenous leading indicators  $x_t$ :
  - $x_t = \{GI_t, \dots, GI_{t-k}\}$
  - $x_t = \{GDP_t, \dots, GDP_{t-k}\}$
  - $x_t = \{UR_t, \dots, UR_{t-k}\}$
  - $x_t = \{EPU_t, \dots, EPU_{t-k}\}$
- $GI1_t =$  'Maternity',  $GI2_t =$  'Pregnancy', and  $GI3_t =$  'Ovulation'.

# The setup of the forecasting horse-race

- Forecasting scheme: we use a **rolling** scheme.
  - 'In Sample' (2004.2-2008.12)  $w/R = 60$
  - 'Out-Of-Sample' (2009.1-2013.12)  $w/P = 60$
- We use **direct** forecasts.
  - Benchmark  $AR(p)$  with  $p$  selected by BIC recursively ex-ante at each forecast origin

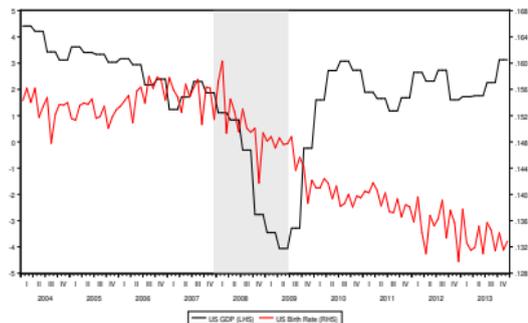
$$y_{t+h}^h = \beta_0 + \beta_1(L)y_t + \eta_{t+h}, \quad t = 1, 2, \dots, T \quad (1)$$

- versus  $AR-X(p)$  model w/ LI  $x_t$  with lags  $p$  and  $q$  selected by BIC recursively and sequentially ( $p_{max} = q_{max} = 4$ )

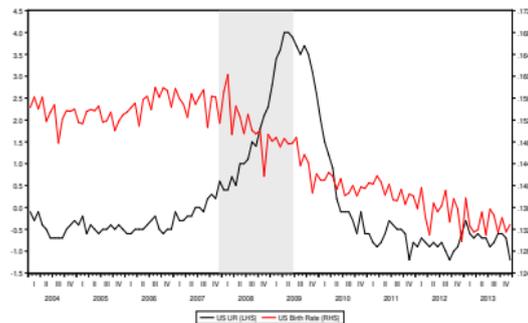
$$y_{t+h}^h = \beta_0 + \beta_1(L)y_t + \beta_2(L)x_t + \varepsilon_{t+h}, \quad t = 1, 2, \dots, T \quad (2)$$

# Google Web Searches for US Birth-related Keywords

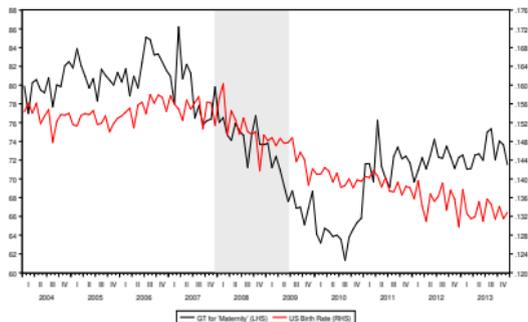
## GDP



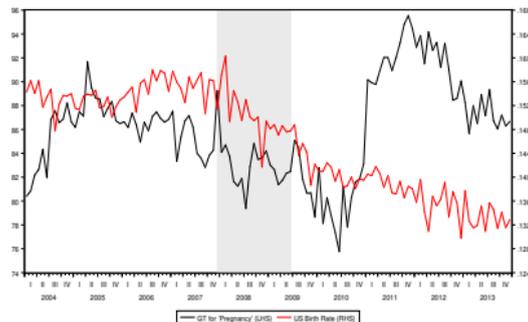
## UR



## GI1 - 'Maternity'



## GI2 - 'Pregnancy'



## Forecasts of US Birth Rates

Short sample: IS: 2004M1-2008M12 - OOS: 2009M1-2013M12<sup>1</sup>

$t + \dots$	6	12	18	24
$AR(p)$ (RMSE)	3.634	3.566	3.655	4.611
$DGDP_t$	0.956	1.005	1.278	1.384
$DUR_t$	1.019	1.175	1.466++	1.529++
$EPU_t$	0.942	0.949	0.822	1.002
$GI1_t$	0.972	0.988	0.955	0.848
$GI2_t$	0.999	1.032++	1.017+	1.011
$GI3_t$	1.03	1.152	1.16	1.138

Long sample: IS: 1990M1-2008M12 - OOS: 2009M1-2013M12

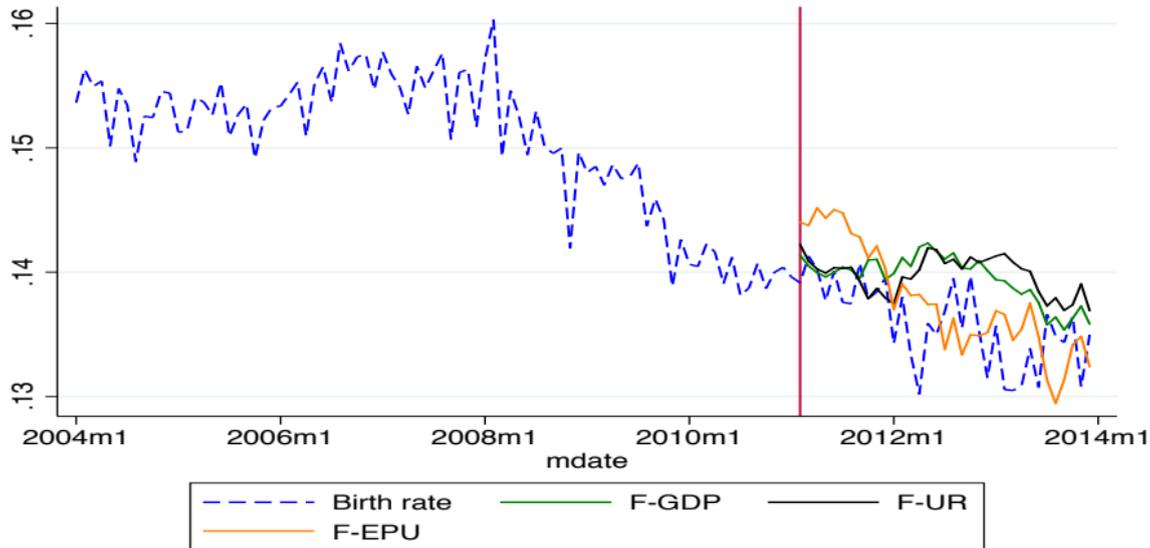
$t + \dots$	6	12	18	24
$AR(p)$ (RMSE)	0.982	1.100	1.247	1.162
$DGDP_t$	0.890	0.968	1.103	1.063
$DUR_t$	0.944	1.097	1.221	1.139
$EPU_t$	0.859**	0.988	0.867***	0.897**

<sup>1</sup>\*, \*\*, \*\*\* indicate significance at 10%, 5%, and 1% respectively of the Diebold and Mariano's (1995) test of equal forecast accuracy, when competing models beats the benchmark. +, ++, and +++ are defined in the same way when the benchmarks outperforms.

RMSE in red and ratios w.r.t. benchmark in black.

# Long sample forecasts

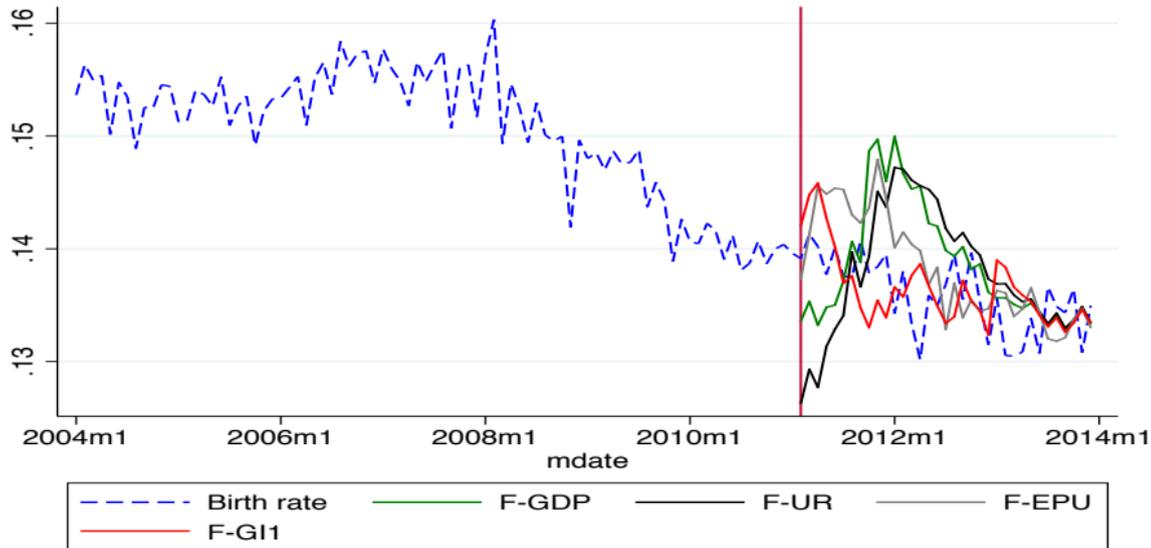
24-month-ahead - Sample: 1990M1-2013M12<sup>2</sup>



<sup>2</sup> $R = 228$ ,  $P = 60$ , In-sample = 1990:M1-2008:M12; Out-of-sample = 2009:M1-2013:M12

# Short sample forecasts

24-month-ahead - Sample: 2004M1-2013M12<sup>3</sup>



<sup>3</sup> $R = 60$ ,  $P = 60$ , In-sample = 2004:M1-2008:M12; Out-of-sample = 2009:M1-2013:M12

# CSSSED

$CSSSED_{m,\tau} = \sum_{\tau=R}^T (\hat{e}_{bm,\tau}^2 - \hat{e}_{m,\tau}^2)$  'best' competing model w.r.t. the  $AR(P)$  benchmark



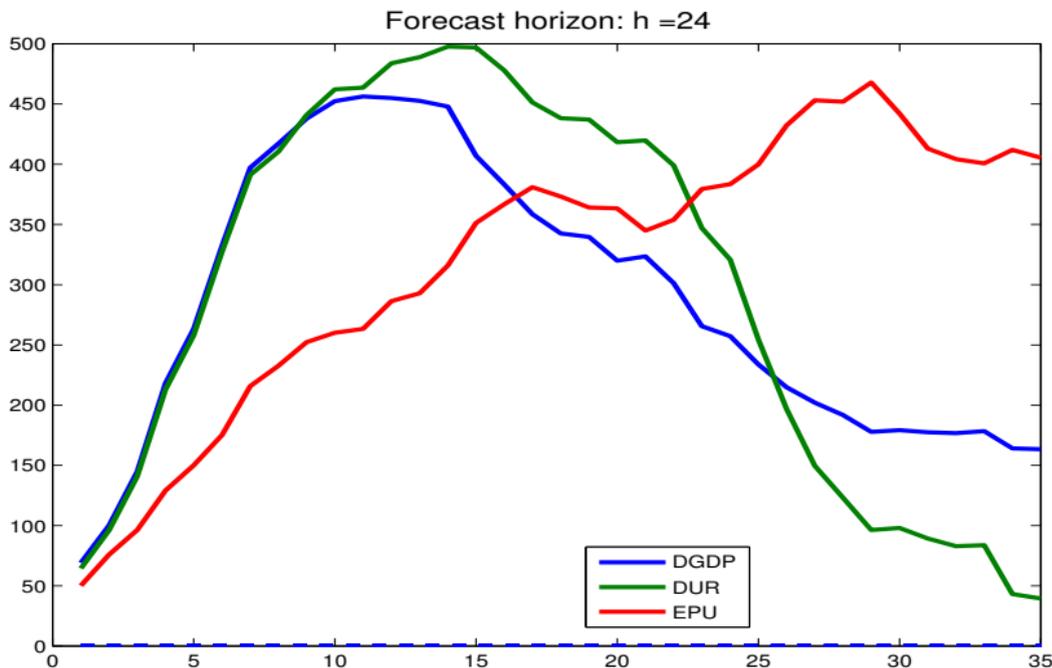
$$CSSSED_{m,\tau} = \sum_{\tau=R}^T (\hat{e}_{bm,\tau}^2 - \hat{e}_{m,\tau}^2) \quad (3)$$

$$\hat{e}_{k,\tau} = u_{\tau} - \hat{u}_{k,\tau|t} \quad (4)$$

- where  $\hat{e}_{bm,\tau}^2$  is the squared forecast error of the AR benchmark model and  $\hat{e}_{m,\tau}^2$  denotes the same for the competing model
- What happens if the benchmark model ( $bm$ ) outperforms the competing model ( $m$ )?
- $\hat{e}_{bm,\tau}^2 < \hat{e}_{m,\tau}^2 \Rightarrow CSSSED_{m,\tau} < 0$
- And if the competing model  $m$  beats the benchmark  $bm$ ?
- $\hat{e}_{bm,\tau}^2 > \hat{e}_{m,\tau}^2 \Rightarrow CSSSED_{m,\tau} > 0$

# Predictive Relative Performance with CSSED - Long sample

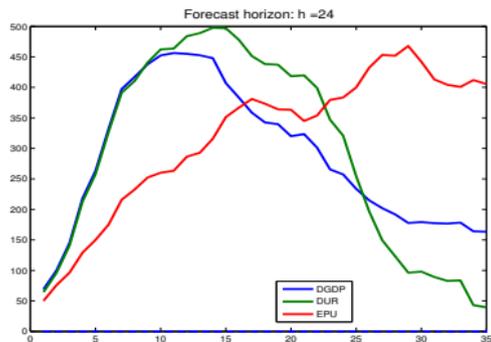
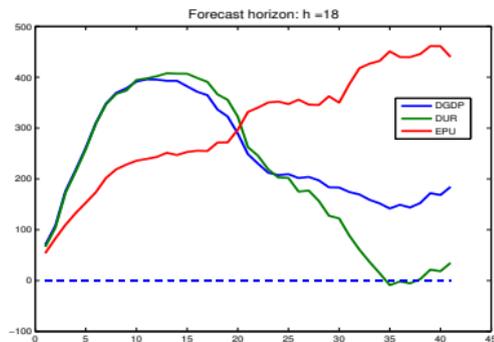
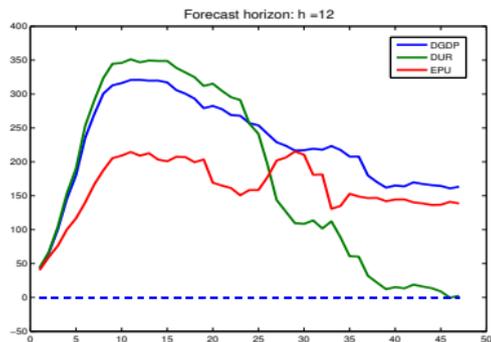
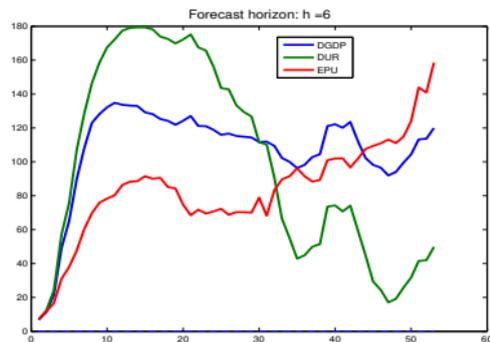
$$CSSED_{m,\tau} = \sum_{\tau=R}^T (\hat{e}_{bm,\tau}^2 - \hat{e}_{m,\tau}^2) \text{ 'best' competing model w.r.t. the } AR(P) \text{ benchmark}^4$$



<sup>4</sup> $R = 228$ ,  $P = 60$ , In-sample = 1990:M1-2008:M12; Out-of-sample = 2009:M1-2013:M12

# Predictive Relative Performance with CSSED - Long sample

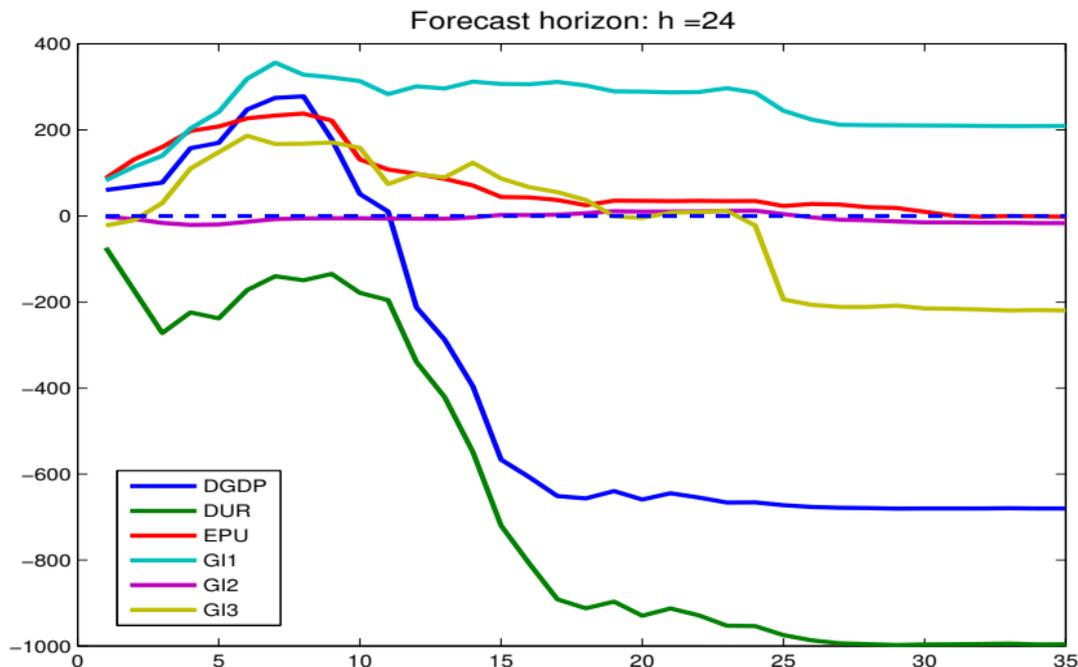
$CSSED_{m,\tau} = \sum_{\tau=R}^T (\hat{e}_{bm,\tau}^2 - \hat{e}_{m,\tau}^2)$  'best' competing model w.r.t. the  $AR(P)$  benchmark<sup>5</sup>



<sup>5</sup> $R = 228$ ,  $P = 60$ , In-sample = 1990:M1-2008:M12; Out-of-sample = 2009:M1-2013:M12

# Predictive Relative Performance with CSSED - Short sample

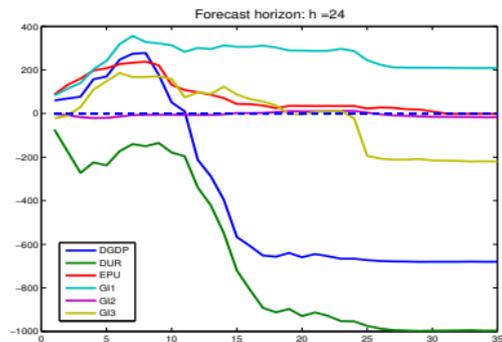
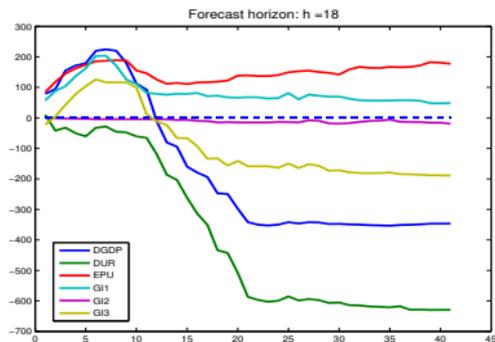
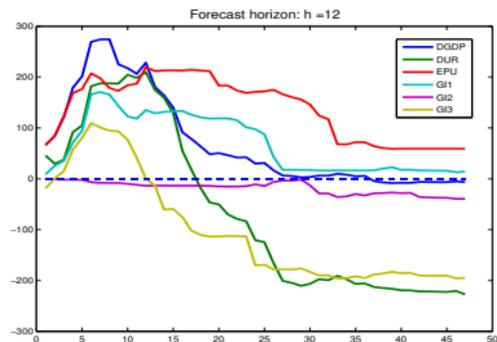
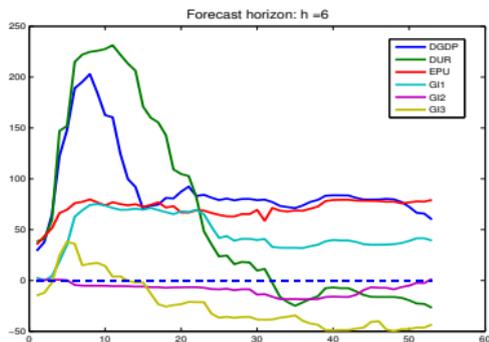
$$CSSED_{m,\tau} = \sum_{\tau=R}^T (\hat{e}_{bm,\tau}^2 - \hat{e}_{m,\tau}^2) \text{ 'best' competing model w.r.t. the } AR(P) \text{ benchmark}^6$$



<sup>6</sup> $R = 60, P = 60$ , In-sample = 2004:M1-2008:M12; Out-of-sample = 2009:M1-2013:M12

# Predictive Relative Performance with CSSED - Short sample

$$CSSED_{m,\tau} = \sum_{\tau=R}^T (\hat{e}_{bm,\tau}^2 - \hat{e}_{m,\tau}^2) \text{ 'best' competing model w.r.t. the } AR(P) \text{ benchmark}^7$$



<sup>7</sup> $R = 60, P = 60$ , In-sample = 2004:M1-2008:M12; Out-of-sample = 2009:M1-2013:M12

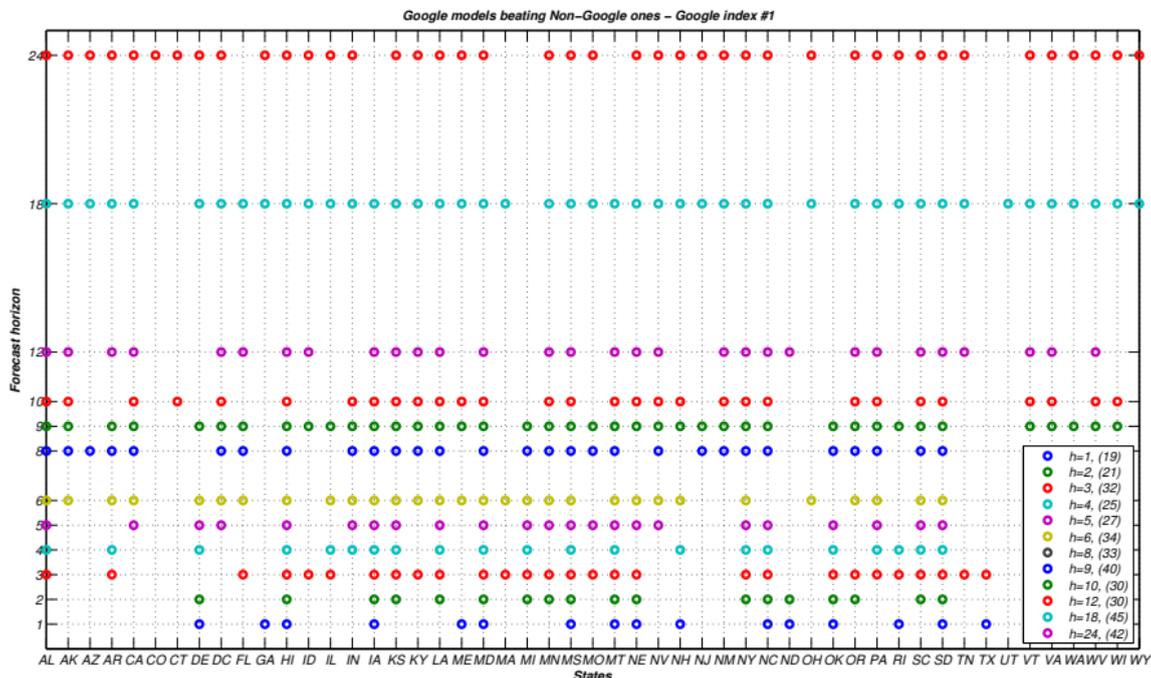
## Robustness - Forecasting birth rates across states

- We repeat the same forecasting exercise for each one of the 50 US states plus DC.
- We ran the same horse race between a benchmark  $AR(p)$  and an  $ARX(p)$  where the leading indicator could be
  - GDP
  - UR
  - EPU (federal level)
  - GI i.e. the Google Index for '*pregnancy*'<sup>8</sup>
- Good results even at the state level for Google-based models
  - At 12-month ahead, Google-based models are better for 59% of states
  - At 18-month ahead, Google-based models are better for 88% of states
  - At 24-month ahead, Google-based models are better for 82% of states

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<sup>8</sup>The GI for '*maternity*' was not populated for some states, i.e. below the Google threshold.

# Robustness - Forecasting birth rates across states<sup>9</sup>



<sup>9</sup>A circle indicates the Google-based model outperforms for state on x axis at forecast horizon on y axis. States in alphabetical order.

# Conclusion

- EPU index seems useful in forecasting US birth rates, at least in the long sample
- Google Trends data seems even more useful in forecasting birth rates at 12, 18 and 24 month ahead
- Google-based model outperform over the short sample
- Only caveat: Google Trends data available only from January 2004
- Google-based model tend to outperform even at the state level

# Thank you!

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