

# The Italian capital stock through the lens of financial accounts

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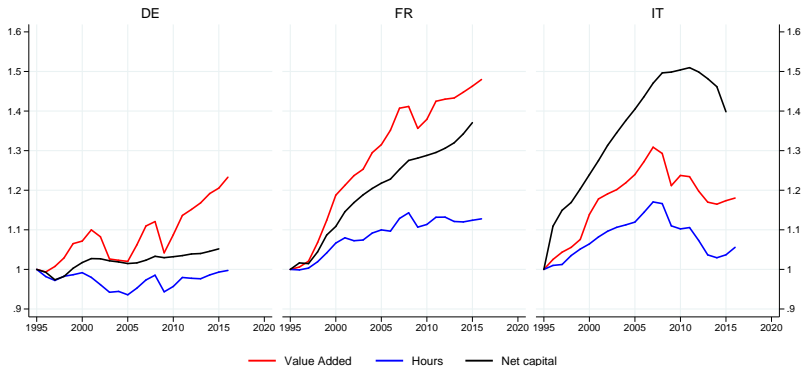


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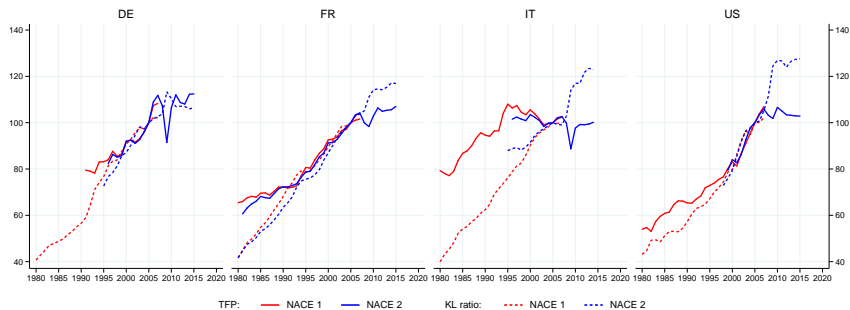
*How financial systems work: evidence from financial accounts*

Banca d'Italia, Rome, 30/11-01/12 2017

## Value added, hours and capital stock (business sector)



## TFP and the capital/labour ratio (manufacturing sector)



Measurement of capital stock involves a number of complex technical assumptions (permanent inventory, service lives of capital goods, depreciation and retirement rates) which might lag behind actual developments, especially at times of rapid changes in technology, market structure and production chains.

Complement official measurement of capital stock, based on those assumptions, with alternative estimates based on market value of business sector (and different assumptions!)

# Capital stock and market value

$$V_t = \max_{\{k_t\}_0^\infty} \sum_0^\infty R^{-t} \left\{ \Pi(k_{t-1}) - p_t^I l_t - C(l_t, k_{t-1}) \right\}$$

$$k_t = (1 - \delta)k_{t-1} + l_t, \quad C_l > 0, \quad C_{ll} > 0$$

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$$\text{FOC} \begin{cases} q_t = \frac{1}{R} (\Pi_K(k_t) - C_K(l_{t+1}, k_t) + q_{t+1}(1 - \delta)) \\ q_t = p_t^l + C_l(l_t, k_{t-1}) \end{cases}$$

Competitive product markets, CRS  $C(l, k)$  and  $F(k, \cdot)$ :

$$q_t = V(k_t)/(p_t^l k_t) = v(k_t)/k_t$$

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Compare official valuation of  $k$  with  $k$  derived from observed  $v$  under alternative choices for  $\delta$  and  $\gamma$ .

Financial accounts - market value of NFC sector

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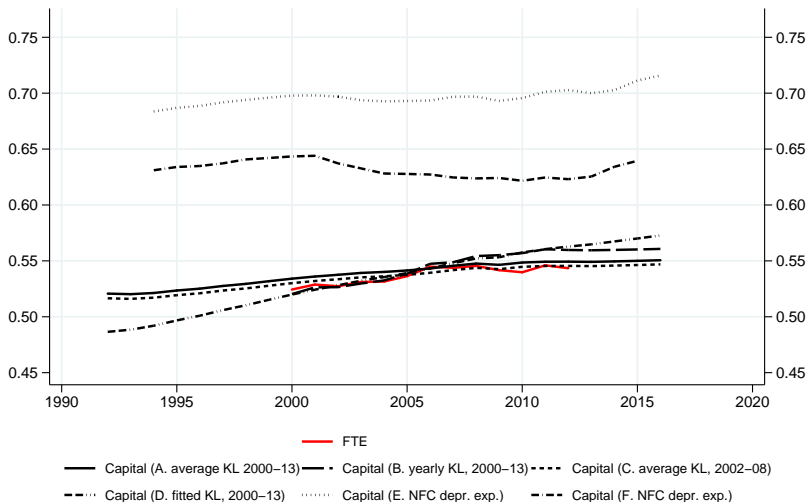
Capital accounts -  $K, I, D$  by NACE and asset type

Institutional sectors accounts - NFC FTE by NACE, total consumption of fixed capital and investment expenditure



Alternative estimates of NFC's share of non-residential private non financial sector capital stock.

## Share of non financial private sector non-residential $K$ of NFC



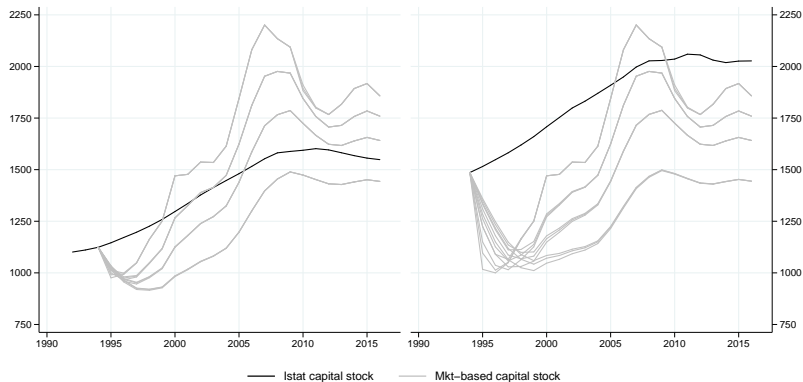
$$\gamma k_t^2 + k_{t-1}(1 - (1 - \delta)\gamma)k_t - v_t k_{t-1} = 0$$

Initial condition: highest and lowest estimate of  $k_{1994}^{NFC}$ .

Consider several combinations of upward ( $\gamma^+$ ) and downward ( $\gamma^- = \rho\gamma^+$ ) adjustment parameters such that  $\rho \geq 1$ .

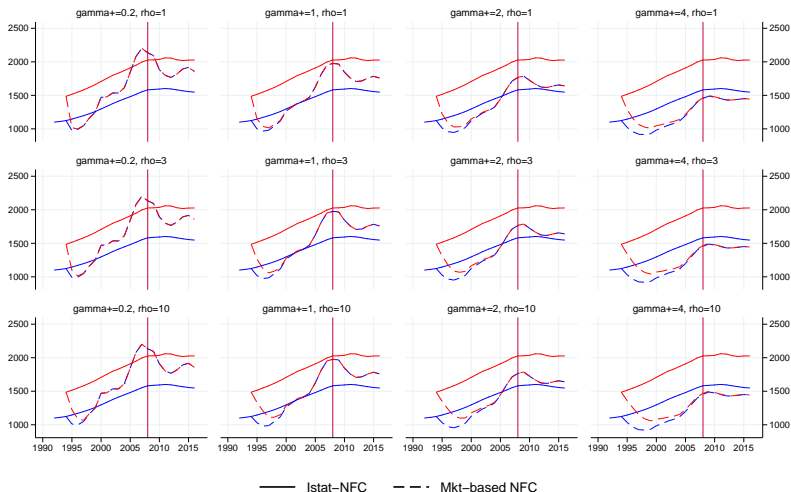
Compare with highest and lowest direct estimates of  $k_t^{NFC}$ .

## Istat and market-based estimated NFC capital stock





## The role of initial conditions and adjustment parameters



Initial drop likely to be a reflection of overestimation of initial conditions. Market valuations suggest a lower level of the capital stock, perhaps a consequence of the restructuring following the early 90's Lira crisis.

Faster subsequent growth than in official estimates between late 90s and onset of global financial crisis consistently with the signs of restructuring of the Italian economy detected before the crisis.

Drop since the onset of the crisis, stronger than in official estimates and consistent with decline of installed capacity and potential output detectable from other sources.

# Conclusions

Theoretically based accounting exercise to construct alternative estimate of capital stock from market valuations.

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Many assumptions: theoretical (no bubbles, competitive product markets, quadratic costs, CRS technology, freely adjustable inputs other than capital) as well as computational (values of adjustment cost function, share of NFC capital, value of non incorporated businesses)  $\Rightarrow$  many potential extensions.