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(Working Papers)

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by Cecilia Frale and Libero Monteforte
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FAMIDAS: A MIXED FREQUENCY FACTOR MODEL WITH MIDAS STRUCTURE

by Cecilia Frale* and Libero Monteforte**

Abstract

In this paper a dynamic factor model with mixed frequency is proposed (FaMIDAS), where the past observations of high frequency indicators are used following the MIDAS approach. This structure is able to represent with richer dynamics the information content of the economic indicators and produces smoothed factors and forecasts. In addition, the Kalman filter is applied, which is particularly suited for dealing with unbalanced data set and revisions in the preliminary data. In the empirical application for the Italian quarterly GDP the short-term forecasting performance is evaluated against other mixed frequency models in a pseudo-real time experiment, also allowing for pooled forecast from factor models.

JEL Classification: E32, E37, C53.
Keywords: mixed frequency models, dynamic factor models, MIDAS, forecasting.

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1 Introduction*

The impact of the recent financial crisis on the real economy was underestimated by a number of forecasters. Both academia and policymakers are now thinking about the ability of macroeconometric models to make predictions about the economy and identify early signals of turning points. In practice, short-term forecasting mainly relies on two sets of instruments: bridge models and factor models. Bridge models link timely indicators with low frequency target variables, whereas factor models extract a common component from a set (usually large) of series. In their standard formulation, bridge and factor models have shown some limitations with respect to two major topics: the time aggregation bias and the ragged-edge data problem, which is a relevant issue for real time forecasts.

Recently, there has been an increase in research papers on these two approaches with extensions in different directions, including mixed frequency models which represent a promising field of research. Mixed frequency models are particularly useful for extracting the information content from high frequency indicators that are used as proxies for target variables observed at lower frequency and with a time lag. Given that this is what economic forecasters do in their day to day work, these models are of particular interest to them. Moreover, these models provide a tool for time series disaggregation, given that the target variable is estimated at a higher frequency.

The mixed frequency literature was initially developed using state space factor models, estimated via the Kalman filter. Most of the applications exploit monthly series, such as industrial production or confidence surveys, to predict quarterly GDP. This approach was used by Mariano and Murasawa (2003), Mittnik and Zadrozny (2004), Proietti and Moauro (2006), Aruoba et al. (2009), Camacho and Perez Quiros (2009) and Frale et al. (2010a). These models can also be used as a multivariate tool for time series disaggregation, as done in Frale et al. (2010b), Harvey and Chung (2000), Moauro and Savio (2005).

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1On the comparison of the different models for short term predictions see Barhoumi, Benk, Cristadoro, Reijer, Jakaitiene, Jelenek, Rua, Rünstler, Ruth and Nieuwenhuyze (2009).

2The problem of the unbalanced data set in large scale factor models has been tackled with different solutions in Altissimo et al. (2007) and Marcellino and Schumacher (2010). On time aggregation bias see Marcellino (1999).
A different approach relates to the recent literature on Mixed Data Sampling Regression Models (MIDAS) proposed by Ghysels, Santa-Clara and Valkanov (2002, 2006). MIDAS mainly differ from mixed frequency factor models as they are univariate, with lag polynomials being used to combine high frequency indicators with the low frequency target variable. There is a small, but fast growing, literature on MIDAS models. Most of the early applications refer to financial econometrics, but there have recently been a number of papers on GDP and inflation. Clements and Galvão (2010) and Andreu et al. (2008) suggest a MIDAS to forecast US macro variables on a monthly and daily basis. Monteforte and Moretti (2010) propose a MIDAS to predict monthly inflation on a daily basis in real time. Marcellino and Schumacher (2010) use a MIDAS to deal with an unbalanced large data-set and for predicting the GDP by means of monthly factors.

In this paper we combine the two approaches and we propose a state space factor model with mixed frequency, where the past observations of high frequency indicators follow a MIDAS structure. This feature is new in the literature and enables the exploitation, in a parsimonious way, of a larger number of lags of the high frequency indicators. This is particularly useful in forecasting as it explicitly takes into account the cross correlation between indicators and the target variable. Moreover, the MIDAS polynomial produces smooth factors, which is a desirable property as it implies less volatile forecasts. This is a relevant issue especially for policy analysis and turns out to be quite important in periods of high variability of macroeconomic data, such as during economic crises. Our approach of combining factor models and MIDAS regression complements the one of Marcellino and Schumacher (2010). They propose a large scale mixed frequency factor model where monthly factors are aggregated to quarterly by using a MIDAS structure, while we proposes a small scale model where the mixed frequency is in the state space and the MIDAS component is only used to consider more lags of the indicators.

The combination of mixed frequency and MIDAS structure allow matching two different and relevant issues: having a monthly index for business cycle analysis, like for dating the cycle and mitigate the noise effect of preliminary data in real time applications. In the empirical application with Italian data, the predictive performance of the Mixed Frequency Factor MIDAS (FaMIDAS in the following) is compared with a multivariate (VAR) model, a mixed frequency univariate model (ADL) and with two mixed-frequency factor models (with single and multiple factors). The results seem to suggest that the FaMIDAS prevails at larger horizons in real time forecasting. This is not surprising, as the factor produced by FaMIDAS is smooth and thus less affected by the short-run variability of the data. The next Section gives an overview of the model, while Section 3 deals with estimation and data issues. Section 4 reports the results of the forecasting exercise and Section 5 draws conclusions.
2 The Model

This section presents the main model of the paper. The aim of this new approach is to increase the flexibility of factor models and thus to improve their ability to reproduce the underlying structural model of economic agents in a framework that is essentially a reduced form. As a matter of fact factor models are pure statistical models, with lack of economic interpretation. Therefore, including a richer dynamics as we do by using a MIDAS structure may be also seen as an indirect way to capture the behavior of economic agents. An example of this would be the expectation formation process, which might induce changes over time in the correlation among time series.

A complementary approach has been followed by Marcellino and Schumacher (2010), where they combine factors and MIDAS in a different structure. In particular we extract a monthly factor using MIDAS polynomial on each indicator, while they adopt a MIDAS structure to project monthly factors for quarterly forecasts. In the following the two main ingredients of the model, and the way in which they are integrated, are presented.

2.1 The factor model with mixed frequency

There are many possible ways of linking a set of indicators available at high frequency to the target variable observed at shorter time intervals.

In particular, we start from a dynamic factor model that decomposes a vector of N time series, $\mathbf{y}_t$, with different frequencies (e.g. monthly and quarterly), into one (or more) common nonstationary components, $f_t$, and some idiosyncratic, $\gamma_t$, specific to each series. Both the common factor and the idiosyncratic components follow autoregressive standard processes as shown by the following representation:

$$y_t = \vartheta_0 f_t + \vartheta_1 f_{t-1} + \gamma_t + \mathbf{S}_t \mathbf{\beta}, \quad t = 1, ..., n,$$
$$\phi(L) \Delta f_t = \eta_t, \quad \eta_t \sim \text{NID}(0, \sigma^2),$$
$$\mathbf{D}(L) \Delta \gamma_t = \delta + \gamma_t^*, \quad \gamma_t^* \sim \text{NID}(0, \Sigma_{\gamma^*}),$$

(1)

where $\phi(L)$ is an autoregressive polynomial of order $p$ with stationary roots and $\mathbf{D}(L)$ is a diagonal matrix containing autoregressive polynomials of order $p_i$ ($i=1$ to $N$). The vector $\delta$ contains the drifts of the idiosyncratic components. The regression matrix $\mathbf{S}_t$ contains the values of exogenous variables that are used to incorporate calendar effects (trading day regressors, Easter, length of the month, etc.) and intervention variables (level shifts, additive outliers, etc.), and the elements of $\mathbf{\beta}$ that are used for initialisation and other fixed effects. The disturbances $\eta_t$ and $\gamma_t^*$ are mutually uncorrelated at all leads and lags.

The model states that each series in differences, $\Delta y_{it}$, is obtained as the sum of a common
autoregressive process of order $p$, $\phi(L)^{-1}\eta_{it}$, an individual $AR(p_i)$ process, $d_i(L)^{-1}\eta_{it}^*$ and a mean term $\delta_i$. The error terms, $\eta_{it}$ and $\eta_{it}^*$ are difference stationary and independent.

Variables are considered in level as common in the unobservable components approach and the cointegration is ruled out on purpose as extensively argued in Fralle et al. (2010b). The model is cast in a linear State Space Form (SSF) and, assuming that the disturbances have a Gaussian distribution, the unknown parameters are estimated by maximum likelihood, using the prediction error decomposition, performed by the Kalman filter.

The SSF is suitably modified to take into account the mixed frequency nature of the series. Following Harvey (1989), the state vector is augmented by an ad hoc cumulator function which translates the problem of aggregation in time into a problem of missing values. The cumulator is defined as the observed aggregated series at the end of the season (e.g. last month of quarter), otherwise it contains the partial cumulative sum of the disaggregated values (e.g. months) making up the aggregation interval (e.g. quarters) up to and including the current one. The model might include a procedure for expressing volumes in chain link prices and therefore allows matching the monthly estimates with national account identities published by national statistical offices.

Given the multivariate nature of the model and the mixed frequency constraint, the maximum likelihood estimation can be numerically complex. Therefore, the univariate filter and smoother for multivariate models proposed by Koopman and Durbin (2000) is used as it provides a very flexible and convenient device for handling high dimension data sets and missing values. The main idea is that columns in the matrix $y_t$, $t = 1, \ldots, n$ are stacked on top of one another to yield a univariate time series whose elements are processed sequentially.

### 2.2 The MIDAS for the lags combination

As is well known in the literature of leading indicators, the anticipating power of an economic series for any target variable is purely an empirical concept. Even more cumbersome is the case of mixed frequency data, where the indicators are available at higher frequency with respect to the target, so that not even autocorrelation analysis is helpful. Consider, for example, that we want to use a well-known leading indicator such as the Business Climate or Purchase Manager Index (PMI) to have a preliminary assessment of the state of the economy before the release of GDP, which is observed on average two month after the end of a quarter. Although it is well known that such indicators have a leading power, we do not know exactly the leading power (in terms of quarters) of the monthly PMI. Even more, we might prefer a more flexible model, so that the leading order can change over time. In our view, a more efficient and suitable solution to this issue is the application of MIxed DAta Sampling models (MIDAS) which summarize and combine the information content of the
indicators and their lags with weights jointly estimated. Usually the treatment of mixed data sample is solved by first aggregating the highest frequency in order to reduce all data to the same frequency and then, in a second step, estimating a regression. This implies imposing some restrictions on the parameters of the aggregating polynomial and does not exploit all the information available. The MIDAS models overcome this problem as they exploit full information without imposing any restrictions on the parameters that are estimated jointly. Some restrictions could be introduced to reduce the parameter space and avoid the cost of parameter proliferation.

MIDAS models have recently encountered considerable success due to their simplicity and good performance in empirical applications. To introduce them, as in the seminal paper by Ghysels et al. (2002, 2006), suppose \( Y_t \) is a time series variable observed at a certain fixed frequency and let \( X_t \) be an indicator variable sampled \( m \) times faster. A MIDAS regression takes the form:

\[
Y_t = \beta_0 + B(\theta, L^{1/m})X_t^m + \epsilon_t
\]

where \( B(\theta, L^{1/m}) = \sum_{k=0}^{K} b(\theta, k)L^{k/m} \) is a polynomial of length \( K \) and \( L^{1/m} \) is an operator such that \( L^{k/m}X_t^m = X_{t-k/m}^m \). In other words the regression equation is a projection of \( Y_t \) into a higher frequency series \( X_t^m \) up to \( k \) lags back.

The MIDAS structure mainly involves two elements: the reconciliation of different frequency and the use of lagged values of the indicators.

In our application, the MIDAS component is only used in order to include in a parsimonious structure past values of indicators, whereas the time aggregation problem is solved inside the factor model as shown in Section 2.1. This allows better interpretation of the cyclical pattern of the economic indicators and comparability with benchmark dynamic models.

Regarding the weight structure, two main possibilities have been proposed in the literature. First, a parametrization that refers to Almon lags:

\[
b(k; \theta) = \frac{\exp(\theta_1 k + ... \theta_q k^q)}{\sum_{j=1}^{q} \exp(\theta_1 k + ... \theta_q k^q)}.
\]

Second, weights drawn by a Beta distribution, such as:

\[
b(k; \theta_1, \theta_2) = \frac{f(k; \theta_1, \theta_2)}{\sum_{j=1}^{k} f(k; \theta_1, \theta_2)}
\]

where \( f(x, a, b) = \frac{x^{a-1}(1-x)^{b-1}}{B(a, b)} \), \( B(a, b) = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)} \) and \( \Gamma(a) = \int_0^\infty e^{t} x^{a-1} dx \).

There is no clear a priori reason for preferring one parametrization over another, and the choice should clearly depend on the research problem under analysis. It should be noted
that, as a rule of thumb, the Beta function, given its flexibility, seems more suitable when the
number of lags considered is large, whereas the simplicity of the Almon weights might be
preferable in the case of a small number of time lags.

Looking at the recent literature, Marcellino and Schumacher (2010) used the Almon
weights for the estimation of GDP in real time, whereas Monteforte and Moretti (2010) found
the Beta transformation more appropriate for the estimation of inflation which involves daily
data and more than 20 lags.

2.3 The FaMIDAS

This section presents how to combine the dynamic factor model with mixed frequency and
the MIDAS structure of lags described in the previous section.

Starting from the model in equation (1) let us partitioning the set of time series, \( y_t \), into
two groups, \( y_t = [y_{1,t}, y_{2,t}]' \), where the second block represents the target variable available
at lower frequency and the first part is a MIDAS structure based on high frequency indicators
\( x_t \) so that \( y_{1,t} = [b(L_k, \theta)x_t]' \).

The FaMIDAS follows from the following equations:

\[
\begin{align*}
\begin{bmatrix} b(L_k, \theta)x_t \\ y_{2,t} \end{bmatrix} &= \vartheta_0 f_t + \gamma_t + S_t \beta, \quad t = 1, \ldots, n, \\
\phi(L) \Delta f_t &= \eta_t, \quad \eta_t \sim \text{NID}(0, \sigma_\eta^2), \\
D(L) \Delta \gamma_t &= \delta + \eta_t^*, \quad \eta_t^* \sim \text{NID}(\theta, \Sigma_{\eta^*}),
\end{align*}
\]

Model 2 collapse to model 1 if \( K=0 \) and \( \vartheta=0 \). In our application \( b(L_k, \theta) \) is the exponential
Almon lag polynomial: \( \sum_{k=0}^{K} w(k, \theta) L^k \) with

\[
w(k, \theta) = \frac{\exp(\theta_1 k + \theta_2 k^2)}{\sum_{k=0}^{K} \exp(\theta_1 k + \theta_2 k^2)}.
\]

Actually this formalization represents a parsimonious way of including in the model
lagged values for the common factor.

The dynamic factor model is estimated by specifying an AR(2) process for the common
component and the idiosyncratic components of the monthly indicators in difference. For
GDP, the idiosyncratic component is formulated as a random walk with drift. This restricted
specification is motivated by the fact that there are identification problems of the kind that
have been discussed by Proietti (2006) with reference to the Litterman model, which affect
the estimation of autoregressive effects.

For the MIDAS polynomial the weights sum up to 1 so that their size is fully comparable.
As far as the maximum lag length is concerned, the target horizon of forecasting and the
economic meaning of the series could suggest the appropriate number. One can consider alternatively to include the lagged values of indicators in the matrix $y_t$ without the MIDAS restriction. This approach, not only has a cost in terms of degree of freedom, as the number of parameters to be estimated would increase considerably, but it fails to consider the time series dimension of lagged values. In fact, without the MIDAS restriction lagged values of the indicators would be included in the model as part of different series.

The model is cast in State Space Form and the Maximum Likelihood estimates are obtained through suitable filtering procedures based on the Kalman filter prediction error decomposition. Starting from a trial for all parameters, including those in the MIDAS structure, the procedure is run iteratively so that the weights in the MIDAS maximize the Likelihood function associated with the factor model. The standard procedure documented in Frale et al. (2010b) is therefore modified adding the restrictions which link the hyperparameter $\theta_{1,2}$ to the parameters $w(k, \theta)$.

In the empirical application we investigate the content of nowcasting and forecasting GDP each month in real time, exploiting the information coming from timely indicators of economic activity. We also discuss the performance of the FaMIDAS model compared to other mixed frequency model and to more standard formalizations. We show that the integrated approach used in our framework provides flexibility in working with data expressed at different frequency, released with different delay and revised every time a new observation is published. Furthermore we stress how our model efficiently deals with dynamic cross correlation among indicators available at different frequencies.

### 3 The Empirical Application

The aim of the empirical application is to exploit the information of the most relevant monthly economic indicators, available earlier than the official statistics, to disaggregate, nowcast and forecast quarterly GDP. This is used to estimate the unobserved monthly GDP, both for the past (a monthly indicator of the known quarterly GDP) and for the future. It is worth noting that in this model the monthly indicator is fully consistent with the quarterly data in terms of time aggregation. Thus we obtain an indicator that can be used both in sample as a monthly measure of GDP to date the cycle and out of sample as a leading indicator.

The GDP is estimated directly, leaving the bottom-up approach (estimation by aggregation of sectoral value added or components of demand) for future research. Although the model is specified in levels in order to easily deal with the time constraint, the results and the forecasting experiment are presented in growth rates, which is the reference measure for
both policy makers and academics.

As for the variable selection, a wide set of indicators is considered, with series referring to different aspects of the economy. These are mainly national statistics data, such as industrial production; survey data, such as climate, expectations and PMI (Purchasing Manager Index); financial data, such as spreads and money (M2); and other data such as the CPB index of world trade, production of paper, electricity consumption and traffic flows of heavy goods vehicles. Although the information set has a small scale, the models incorporate a variety of properly chosen indicators referring to the real economy as well as finance, national and international, in the service and manufacturing sectors. Variables are taken directly from the source in seasonally adjusted values, except for electricity consumption and traffic of trucks which have been seasonally adjusted using the Tramo-Seats routine and smoothed when needed. For the model selection process we follow the standard approach in the literature, based, for example, on statistical significance of the indicators and BIC or Akaike criteria for the lag length selection.

After some empirical robustness checks, the sample ranging from January 1990 up to the most recent observations at the time of writing (April 2009) was found to have the best trade-off among representativeness of the sample size, availability of long time series and data quality. Some benchmark models have been estimated.

The central model is our factor model with MIDAS structure (FaMIDAS), based on an information set with 4 indicators and combinations of up to 4 lags: Industrial production, German PMI, Business climate, Electricity consumption. Alternative lag lengths have been evaluated accordingly to a reasonable forecast horizon (maximum 6 months ahead) and the economic meaning of the indicators. We compare the empirical performance of our FaMIDAS with two multivariate models.

Then we consider a baseline model (MIXFAC) specified as in equation (1) and based on the same information set than the FaMIDAS, but without MIDAS component and one lag of the first two series.

Finally we also estimate a factor model with 2 factors (MIX2FAC), as discussed in Frale et al. (2010a), which includes additional indicators: Industrial production of paper, world trade, Treasury Italian yields (10Y), Money supply, traffic flows of heavy goods vehicles.

The baseline MIXFAC model involves both survey and national account data. The MIX2FAC model includes more soft indicators and the second factor captures also financial swings, as they comes up ex-post. Finally, using FaMIDAS, it is possible to consider up to four lags of each economic indicator of MIXFAC.

The estimated maximum likelihood parameters are listed in Table 1, whereas the monthly

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3No calendar effect neither intervention variables are included in the matrix $S_t$
indicators are shown in Figure 1. In addition, Figure 2 shows the estimated GDP in monthly growth rates and the common factors for the three models. The graph clearly shows that the FaMIDAS produces a smoother factor which is a desirable property, likely a product of the fact that the MIDAS structure sums over time lags. Similarly, the disaggregated monthly GDP from the FaMIDAS is more stable than the same obtained by the other two mixed frequency models (MIXFAC and MIX2FAC). Moreover, the confidence bands of the predictions, shown as fan charts in Figure 3, reveal smaller incertitude in the FaMIDAS model than in the other mix-frequency formulations.

The inspection of the spectral density of the estimated monthly GDP for the MIDAS and MIXFAC, shown in Figure 4, suggests that the FaMIDAS structure is able to capture standard business cycle frequencies and, therefore, might perform better in short-term forecasting than in nowcasting. Analyzing the minor volatility in terms of spectrum of frequencies, it turn out that the FaMIDAS picks up the less volatile components of the spectrum and thus the estimates are less affected by the noise of data revisions that occur in real time analysis. Indeed the fact that previsions from the FaMIDAS are less volatile makes them particularly useful for dealing with real time data which are subject to revision and, therefore, suffer for high degree of uncertainty.

The forecasting performance analysis of the three models requires an empirical application, which is presented in the next section. On the contrary, the production of a monthly measure of GDP which is a derivative of this framework is not the focus of this paper.

4 Forecasting evaluation

In this section the three models under analysis are compared with respect to their forecasting ability for the Italian GDP by using a rolling experiment in a window of the latest 5,4 years up to the end of 2007. The rolling exercise is made in pseudo-real time, so as to mimic the delay of different indicators, which has been proved to be relevant for correctly assessing which model performs best. Therefore the forecasting evaluation is made with specification of the month of the prediction inside the quarter (e.g. first month, second or third), which corresponds to a different information set. It is worth stressing that the Kalman filter is particularly suitable for this issue given that it solves endogenously the problem of the unbalanced sample produced by the difference in timing of publication of the monthly indicators. Consider the example of making a forecast for GDP in the 1st of January 2011.

\footnote{We prefer to exclude the biennium 2008-2009 from the sample to avoid that the exceptional conditions of the economic crisis affect the results. In addition, at the time of writing, data from 2008 upwards were still preliminary and subject to revision.}
The last release of GDP refers to the third quarter of 2010 and thus before making forecast for one or two parters ahead, it is required to estimate the last quarter of GDP for 2010 which is still unknown. Analogously, monthly indicators are published with a certain delay. In January, for example, we would have soft indicators, such as PMI or Business climate, for December 2010, while Industrial production for November 2010 would be release around the 15 of January 2011. Therefore indicators need to be forecasted for closing the quarter that should be predicted so as to balance the sample.

The Kalman filter allows doing this step endogenously as it solves directly the ragged-edge data issue by using the prediction routine. Moreover, every time a new observation for an indicator is released, all the series are generally revised for prior years and the MIDAS component helps reducing the statistical noise of the revisions in real time.

In Table 2 we show RMSE of the three mixed frequency factor models and of two additional benchmark models. To disentangle the contribution of the mixed frequency structure, we also consider a quarterly VAR (estimated with order 2 on the bases of the AIC criteria) that includes the same information set as the MIXFAC. Moreover, to assess the gain of the multivariate structure we consider a univariate ADL modified as in Proietti (2006) to replicate a mixed frequency structure. We also considered as benchmark a model similar to the Factor-MIDAS of Marcellino and Schumacher (2010), where the MIDAS structure is applied to the common factors. Although the two authors use a large dataset of indicators, we constrained the information set to be coherent with the other models for sake of comparison. We see that all factor models easily outperform the other two benchmark models. Considering, in particular, the three mixed frequency models, we see that the differences in predictive ability are small and the ranking changes with the sample, the forecasting horizon and the monthly information. The ranking is also subject to the loss function as it is slightly different in the RMSFE and MAPE. For the case of a linear specification we see (Table 3) that the absolute value of the forecast errors are almost always smaller for the FaMIDAS in $Q_{t+1}$ and $Q_{t+2}$. Looking jointly at RMSE and MAPE, it seems that the MIX2FAC is more suited for nowcasting, FaMIDAS makes the lowest RMSE for one quarter-ahead and Factor-MIDAS tends to prevail for two quarters ahead.

More generally, given the apparent absence of clear dominance of one model, we performed the DMW tests (Diebold and Mariano(1995) and West (1996)) of equal forecast ability to check if the ranking showed by RMSE is statistically significant. In particular, we tested the hypothesis that FaMIDAS has the same predictive information as the other two models. The results, in Table 4, are coherent with the evidence shown in the previous table: MIX2FAC dominates for 1-step ahead predictions, whereas FaMIDAS tends to make the smallest error for 2-step ahead forecasts, respect to all models including the Factor-MIDAS.
Since the seminal paper by Bates and Granger (1969), it is well know that combining different models results in a smaller forecast error than selecting a single specification. The general idea is that the combination of different specifications, by averaging, mitigate the model misspecification, instability and estimation error of each specific model (Timmermann 2006). Therefore, the pooling forecast is particularly suitable when the combined models show significant heterogeneity.

The application presented above matches this requirement, given that the models differ in terms of components (number of factors and lags), as well as for the best forecast horizon. In the bottom panel of Table 2 and Table 3 we report the real time errors for the pooled model with equal weights\(^5\). The combination of the three models, the MIXFAC, MIX2FAC and FaMIDAS appears useful in real time, as the error size is always close to those of the best model.

In fact, the forecasts produced by the pooling of different models dominates the single models more often for the RMSE than for the MAPE. A more proper combination would require a dedicated analysis that we leave for future research.

To summarize, we find that the mixed frequency factor models outperform standard VAR and univariate mixed frequency ADL. The differences in the forecasting ability of the three factor models are small, time dependent and not always statistically significant. In general, it emerges that MIXFAC and MIX2FAC appear more suited for nowcasting, while FaMIDAS and Factor-MIDAS seem better for forecasting. Northwithstanding the small differences in RMSE a forecast combination of the three factor models reduces further the error, likely thanks to the heterogeneity in the structure of the three models.

5 Conclusions

The short-term forecasting literature has shown an increasing interest in mixed frequency models. These models are particularly useful in real time forecasting as they deal with the unbalanced data set problem and they reduce the temporal aggregation bias created by the different frequencies of the observable indicators. In this paper we combine two approaches: dynamic mixed frequency factor models and MIDAS. Our model, that we call FaMIDAS, is designed for applications in real time as it reduces the problem of the unbalanced data set and it is less affected by revisions of preliminary data. Moreover it can take into account changes over time of the leading power of timely high frequency indicators used for forecasting.

As by product we obtain a monthly index of GDP which is per-se relevant for business

\(^5\)Although the simple average of forecast is not optimal, under general circumstances and symmetric loss functions it can generate a smaller loss (see Elliott and Timmermann (2004))
cycle analysis, as for example for defining a chronology of the cycle, application that we left for future research.

In the empirical application we estimate the FaMIDAS against benchmark models and mixed frequency factor models with different structures. Overall the FaMIDAS produces smoother estimates for the disaggregate target variable and better forecasts for one quarter ahead. In order to reduce further the prediction error a simple pooling forecasts is proposed.
Appendix: The State space representation and temporal aggregation

Consider the factor model proposed in section 2.3:

\[
\begin{align*}
\mathbf{y}_t &= \begin{bmatrix} b(L_k, \theta) \mathbf{x}_t \\ \mathbf{y}_{2,t} \end{bmatrix} = \vartheta_0 f_t + \gamma_t + S_t \beta, \quad t = 1, \ldots, n, \\
\phi(L) \Delta f_t &= \eta_t, \quad \eta_t \sim \text{NID}(0, \sigma_{\eta}^2), \\
D(L) \Delta \gamma_t &= \delta + \eta^*_t, \quad \eta^*_t \sim \text{NID}(0, \Sigma_{\eta^*}).
\end{align*}
\]

where \(b(L_k, \theta) \mathbf{x}_t\) is the MIDAS polynomial for the combination of lags of the monthly economic indicators and \(\mathbf{y}_{2,t}\) is the aggregated variable that gathers the flow subject to temporal aggregation (e.g. the quarterly GDP). \(D(L)\) is a matrix containing autoregressive loading of the idiosyncratic components. The common factor and the idiosyncratic components follow standard autoregressive processes and thus the model can be easily casted in State Space Form (SSF).

Consider the standard way to recast in SSF a general AR(\(p\)) process \(\phi(L) \Delta f_t = \eta_t\) with \(\phi(L) = (1 - \phi_1 L - \phi_2 L^2 - \ldots - \phi_p L^p)\):

\[
f_t = e_{1,p+1}' \alpha_t, \quad \alpha_t = T_f \alpha_{t-1} + H \eta_t,
\]

where

\[
\alpha_t = \begin{bmatrix} f_t \\ f^*_t \end{bmatrix}, \quad T_f = \begin{bmatrix} 1 & e_{1p}' T_\phi \\ 0 & T_\phi \end{bmatrix}, \quad T_\phi = \begin{bmatrix} \phi_1 \\ \vdots \\ \phi_{p-1} \\ \phi_p & 0' \end{bmatrix}.
\]

and \(f^*_t = T_\phi f^*_{t-1} + e_{1p} \eta_t, \quad H = [1, e_{1p}']', e_{1p} = [1, 0, \ldots, 0]'.\)

And then apply the previous representation to the common factor and each idiosyncratic. The SSF of the complete model results:

\[
\mathbf{y}_t = \begin{bmatrix} b(L_k, \theta) \mathbf{x}_t \\ \mathbf{y}_{2,t} \end{bmatrix} = Z \alpha_t + S_t \beta, \quad \alpha_t = T \alpha_{t-1} + W b + H \epsilon_t,
\]

where the state vector and the vector of errors are obtained stacking the single SSF representation of the autoregressive processes, namely: \([\alpha_t = \alpha'_{f,t}, \alpha'_{\gamma_1,t}, \ldots, \alpha'_{\gamma_N,t}]'\), for the state and \(\epsilon_t = [\eta_t, \eta^*_{1,t}, \ldots, \eta^*_{N,t}]'\) for the vector of errors.

The system matrices of the measurement equation become:

\[
Z = \begin{bmatrix} \theta_0; & \theta_1; & 0; & \text{diag}(e_{p1}', \ldots, e_{pN}') \end{bmatrix}, \quad T = \text{diag}(T_f, T_{\gamma_1}, \ldots, T_{\gamma_N}), \\
H = \text{diag}(H_f, H_{\gamma_1}, \ldots, H_{\gamma_N}).
\]
The matrix $W$ is time invariant and selects the drift $\delta_t$ for the appropriate state element of the idiosyncratic component.

The temporal aggregation problem is solved following the strategy proposed by Harvey (1989). The block of variables subject to temporal aggregation, $y_2$, are replaced by an ad hoc cumulator variable, $y_{2,t}^c$, defined so that it coincides with the (observed) aggregated series at the end of the larger interval (e.g. quarter), otherwise it contains the partial cumulative value of the aggregate in the seasons (e.g. months), as follow:

$$y_{2,t}^c = \psi_t y_{2,t-1}^c + y_{2,t}, \quad \psi_t = \begin{cases} 0 & t = \delta(t - 1) + 1, \quad \tau = 1, \ldots, \lceil n/\delta \rceil \\ 1 & \text{otherwise} \end{cases}$$

The cumulator is used to replace the second block of the measurement equation and to augment the state equation as follow:

$$\alpha_t^* = \begin{bmatrix} \alpha_t \\ y_{2,t}^c \end{bmatrix}, \quad y_t^\dagger = \begin{bmatrix} b(L_k, \theta)x_t \\ y_{2,t}^c \end{bmatrix}$$

The final measurement and transition equation are therefore:

$$y_t^\dagger = Z^*\alpha_t^* + S_t\beta, \quad \alpha_t^* = T^*\alpha_{t-1}^* + W^*\beta + H^*\varepsilon_t, \quad (6)$$

with system matrices:

$$Z^* = \begin{bmatrix} Z_1 & 0 \\ 0 & I_{N_2} \end{bmatrix}, \quad T^* = \begin{bmatrix} T & 0 \\ Z_2T & \psi_tI \end{bmatrix}, \quad W^* = \begin{bmatrix} W \\ Z_2W + S_2 \end{bmatrix}, \quad H^* = \begin{bmatrix} I \\ Z_2 \end{bmatrix}H. \quad (7)$$
References


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** Means significant at 5%, * at 10%.

The sample period ranges from 1990M1 to 2009M4. Business Climate is provided by ISAE; Electricity is the monthly consumption of electricity provided by TERN; PMI Germany is the Purchase Manager Index for Germany in manufacturing and services; IP paper is the Industrial production of paper and cardboard; World trade is the indicator of trade produced by the CPB- Netherlands Bureau for Economic Policy Analysis; Money supply includes currency and deposits; Motorway flow refers to trucks and it is provided by Autostrade.
Table 2: Rolling forecasting experiment: RMSE.

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Note: Each entry represents the RMSE of the rolling forecast of GDP growth rates, aggregated to the quarterly frequency, by month of the quarter in which the prevision is made, horizon of prevision and window length. The best values among the models (except for the pooling) are underlined. The VAR is estimated on a balanced quarterly sample. The ADL is estimated as documented by Proietti (2006) by using the routines provided by the author.
Table 3: Rolling forecasting experiment: MAPE.

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Note: Each entry represents the MAE of the rolling forecast of GDP growth rates, aggregated to the quarterly frequency, by month of the quarter in which the prevision is made, horizon of prevision and window length. The best values among the models (except for the pooling) are underlined. The VAR is estimated on a balanced quarterly sample. The ADL is estimated as documented by Proietti (2006) by using the routines provided by the author.
Table 4: Diebold-Mariano test by horizon of previsions and month in the quarter (Student-T).

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Note: Rolling forecast window: 2003-2007; Values adjusted by the Newey-West correction.
Figure 1: Monthly Indicators and Quarterly GDP- Italy
Figure 2: Estimated Monthly GDP and common factors.

GDP Monthly Growth Rates

Note: Axis are shown in normalized scale for the common factors.
Figure 3: Forecasts and fan charts

Note: The filled area is the 95% confidence band.
Figure 4: Spectral Density of the Monthly GDP.

Note: The horizontal axis represents frequencies from 0 to $\pi$, while on the vertical axis the estimated spectral density of the monthly GDP in growth rates.
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