Monetary policy rules for the euro area:
what role for national information?

by P. Angelini, P. Del Giovane, S. Siviero and D. Terlizzese
The purpose of the Temi di discussione series is to promote the circulation of working papers prepared within the Bank of Italy or presented in Bank seminars by outside economists with the aim of stimulating comments and suggestions.

The views expressed in the articles are those of the authors and do not involve the responsibility of the Bank.

Editorial Board:
ANDREA BRANDOLINI, FABRIZIO BALASSONE, MATTEO BUGAMELLI, FABIO BUSSETTI, RICCARDO CRISTADORO, LUCA DE DOLA, FABIO FORNARI, PATRIZIO PAGANO; RAFFAELA BISCIGLIA (Editorial Assistant).
MONETARY POLICY RULES FOR THE EURO AREA:
WHAT ROLE FOR NATIONAL INFORMATION?

by Paolo Angelini*, Paolo Del Giovane*, Stefano Siviero* and Daniele Terlizzese*

Abstract

Using a simple multi-country econometric model covering the three main countries of the euro area, the paper focuses on the role that can be played by information at the national level in defining the monetary policy of the Union. We find that the performance of a central bank that chooses the nominal interest rate to minimize a standard quadratic loss function of area-wide inflation and output gap improves significantly if the reaction function includes national variables — as opposed to the case in which the interest rate reacts to area-wide variables only. Our results suggest that asymmetries within the euro area are relevant to the central bank; overall, we interpret them as making a case for exploiting the available national information in the conduct of the single monetary policy.

JEL classification: E52, E58.

Keywords: monetary policy rules, Eurosystem.

Contents

1. Introduction .................................................................................................................. 7
2. Related literature ......................................................................................................... 11
3. A small empirical model for the main euro-area economies .................................... 13
4. Design of the experiments .......................................................................................... 16
5. The results .................................................................................................................. 20
6. Preliminary conclusions and possible extensions ....................................................... 25
Tables and figures ........................................................................................................... 28
References ......................................................................................................................... 41

* Bank of Italy, Economic Research Department.
1. Introduction

The role of national information in the decision-making process of the Eurosystem has been a point of controversy in the debate on the new-born institution. On the one hand, several elements suggest that national developments do not play a significant role in shaping monetary policy decisions. To begin with, strategy is presented in ECB documents as focusing exclusively on area-wide developments and effects of monetary action, neglecting events in individual member countries. Other features of the Eurosystem’s communication strategy also convey the same orientation, which is well summarized by the following President Duisenberg’s statement at the press conference following the Governing Council meeting of 9 September 1999: “... our decisions today, again and as always, were based on a *euro area-wide analysis* of economic and financial developments — *and nothing else*” (italics added).

On the other hand, some observers (see, e.g., De Grauwe, Dewachter and Aksoy, 1999; De Grauwe, 2000; De Grauwe and Piskorski, 2001) maintain that the prominent role played by NCB governors within the Governing Council of the Eurosystem is likely, in practice, to give national developments a greater weight than might be warranted. According to this view, while the ECB makes every effort to convince the public that only area-wide developments are relevant to its policy stance, monetary policy decisions are likely to be influenced, *de facto*, by national interests.

This debate centers on a positive issue. Both parties agree that only area-wide developments should be relevant, but one argues that, as a matter of fact, national considerations loom (unduly) large. However, the discussion begs the question of whether the neglect of information pertaining to the national level is appropriate from a normative

---

1 The views expressed are the authors’ own and do not necessarily reflect those of the Banca d’Italia. Previous drafts of the paper were presented at the conferences “Ricerche quantitative per la politica economica - 1999,” Banca d’Italia-CIDE, Perugia, 15-18 December 1999, “The Euro - What’s in the Future?,” BCI-Greta, Venice, 8-9 June 2000, “The role of policy rules in the conduct of monetary policy,” ECB, Frankfurt, 11-12 March 2002. We are indebted to Albert Ando, Pietro Catte, Luca Dedola, Riccardo Fiorito, Libero Monteforte, Fabio Panetta, Paolo Sestito and other participants in the Banca d’Italia-CIDE, BCI-Greta and ECB Conferences for helpful comments, as well as to Lawrence Christiano and Richard Clarida for stimulating discussions. Any errors are our own.

2 According to the initial exposition of the ECB strategy “… policy decisions must be made in a manner that reflects conditions across the euro area in its entirety, rather than specific regional or national developments” (ECB 1999, p. 47). Also, monetary policy decisions are motivated in terms of economic developments in the area as a whole, both in the Bulletin and in the press releases following the Governing Council meetings. Furthermore, the statistical section of the ECB Monthly Bulletin shows only aggregate statistics for the area, with no national breakdown, except for fiscal positions.
viewpoint. In our opinion, the widespread agreement that national information should, in principle, play no role in the single monetary policy stems from a failure to distinguish clearly between objectives (in a formal model, the arguments of the monetary authorities’ loss function) and the process through which policy decisions are made (the reaction function). It is far from self-evident that from a normative viewpoint the process through which policy decisions are made should utterly disregard national developments. Indeed, the appropriate policy might require that the monetary authorities react to national developments, rather than (or in addition to) area-wide aggregates, even if their objectives are framed exclusively in area-wide terms. This may be the case if the economies of the area are characterized by significant structural differences — in particular concerning the monetary transmission mechanism — and/or are hit by asymmetric shocks. In these circumstances, a given shock may have different short-term and medium-term effects on the economy of the area depending on which country is hit first or more sharply. The effects of the shock will reflect not only the relative importance of that country (its relative GDP), but also the structural relations that characterize its economy, as well as its trade links with the rest of the Union.  

This paper addresses this normative issue. Taking for granted that the NCB Governors’ interpretation of their role in the Governing Council is consistent with their mandate and thus corresponds to that recently reasserted by the ECB president, we assess the usefulness of country-specific information to monetary policy within a monetary union. In particular, we ask to what extent and in what manner the Eurosystem should take information at the national level into account in making its monetary policy decisions; to answer this question, we assess the cost of disregarding this information or not using it properly.

To this end, we follow the standard approach to policy evaluation recently revived by a growing literature on monetary policy rules (see, e.g., the contributions in Taylor, 1999):

---

3 An additional justification for the use of country-level information — of a logically different nature — is provided by cases in which the value of an economic variable of a specific country is a leading indicator for area-wide developments. For instance, in spite of its small size, Belgium’s manufacturing survey is considered a very good leading indicator for area-wide industrial production growth, due to the fact that Belgium is a large supplier of intermediate goods to the French and German manufacturing industry.

4 “… in a monetary union, there is only one monetary policy, and this must be directed to a single objective. As laid down in the Treaty, each member of the Governing Council is therefore well aware that he or she is not a representative of a country or central bank but acts in a personal capacity in deciding the appropriate conduct of monetary policy for the euro area as a whole.” Press conference following the Governing Council meeting of 30 March 2000.
we search for reaction functions that minimize the expected value of an intertemporal loss function, under the constraint provided by a simplified multi-country model of the euro area. Assuming that the monetary authority is exclusively interested in area-wide objectives (the arguments of the loss function are area-wide variables only), we compute and compare the performance of two classes of simple optimal reaction functions. “Multi country information-based rules” (MCIB) allow the interest rate to be a function of country-specific variables (plus the lagged value of the interest rate to allow for some instrument smoothing). By contrast, rules in the second class, which we label “area-wide information-based rules” (AWIB), are restricted so that their arguments can only be area-wide variables; in other words, the monetary authority is assumed not to observe country variables separately but only their aggregation. We then compare the minimized expected loss under the two alternative policy rules, interpreting the difference as the cost of neglecting country-specific information. As a benchmark, we also compute the fully optimal rule (FO) in our linear-quadratic framework (Chow, 1975), assuming no restrictions on the set of state variables to which the policy maker is allowed to react.

Let us point out that although the debate summarised above could lead one to think that national developments should in principle play no role whatsoever in the Eurosystem’s strategy, there is reason to believe that this may partly reflect the Eurosystem’s effort to convey to the public the idea that its objectives are strictly area-wide. Actually, however, the process by which decisions are made (the reaction function) does exploit national information — and, as we have just argued, quite legitimately so. The Eurosystem currently uses a multi-country approach to the econometric modeling of the area (the ECB uses its own multi-country model, in addition to an area-wide one, and national econometric models developed and managed by the NCBs have a prominent role in the forecasting framework); national information is regularly exchanged and carefully analyzed within the Eurosystem; national statistics are available earlier than area statistics (which are prepared by Eurostat and by the ECB collecting the national information) and in many cases represent a more timely complement to the available area-wide indicators.5 Thus, our main thesis — that national-level information is

5 It is worth noting that this is not the case in the US, where aggregate data for the entire country are available before regional data. This aspect is highlighted in reports of Goldman Sachs (1999) and JPMorgan (1999), which describe how they “create” area-wide statistics for the euro area from the more timely releases of national statistics.
relevant to the euro-area policymaking process — may well be less controversial than it may appear.

It should be acknowledged that the claim of this paper — that the heterogeneity across euro-area countries warrants consideration of national developments in the implementation of monetary policy — faces a natural objection. Why are similar concerns not raised for other monetary unions? The answer, we believe, is that the heterogeneity among the euro-area countries is, a priori, likely to be larger. The differences in institutional features and economic structures (e.g. legal system, contract enforcement and corporate law, labor market arrangements, independent fiscal policies) are much more pronounced than in other monetary unions or federal nations (the US being the most obvious comparison), and are likely to persist for some time in the future. In addition, convergence of fundamentals (such as the inflation rate, the level of interest rates, the budget deficits and the public debt) has been only a recent — and in some cases incomplete — achievement; language and cultural differences, tending to hinder labor mobility, may be a relevant obstacle for the foreseeable future. We therefore conjecture that the potential loss associated with the neglect of country-specific information could be large. At any rate, measuring this loss is precisely our purpose.

The organization of the paper is as follows. Section 2 briefly describes some of the literature that has dealt with the issue of national vs. aggregate information in a monetary union. In particular, we briefly discuss the approach in De Grauwe (2000), De Grauwe and Piskorski (2001), Monteforte and Siviero (2002), whose focus is similar and whose results are in some cases complementary to ours. Section 3 illustrates the simple euro-area multi-country model used in the analysis. We restrict our attention to the three main countries — France, Germany and Italy. This choice is made primarily for practical reasons, but in any case these countries are broadly representative of the area, accounting for over 70 per cent of its GDP. Each country is modeled separately (but trade links are allowed for) and the area-wide variables are obtained ex-post, via aggregation. Sections 4 and 5 describe the setup of the exercise and report the empirical results. The last section summarizes the preliminary conclusions and discusses the possible extensions of our research.
2. Related literature

Several recent papers have dealt with the relevance of regional information in a monetary union.

De Grauwe, Dewachter and Aksoy (1999) concentrate on the possibility that the members of the ECB Governing Council (all of them or just the NCB Governors) care about national interests, as opposed to those of the area, and examine the implications for the welfare of the member countries under different hypotheses on the voting procedures of the Governing Council.

De Grauwe (2000) uses a simple two-country theoretical model (one Phillips curve for each country) to analyse two cases. In the first, the policymaker chooses inflation to minimize a loss function constructed as a weighted average of the two national losses, under the constraint given by a multi-country model; in De Grauwe’s terminology, in this case the central bank makes use of national information. In the second exercise, in which the loss function is defined over area-wide variables and the model is area-wide, the central bank is assumed to ignore national information. He finds that in the presence of asymmetries the central bank can improve monetary policy effectiveness by exploiting national information.

DeGrauwe and Piskorski (2001), sticking to policy rules that are always defined over national data (i.e., the monetary authority is assumed to react to national information), study the welfare implications of focusing on national vs. area-wide definitions of the loss function. Specifically, in one case they assume the preferences of the ECB to be a weighted average of the national loss functions and compute the optimal policy rule that is consistent with such preferences, under the constraint provided by a multi-country model. Alternatively, they assume preferences that are in line with the statutory provisions of the ECB and are therefore based on area-wide aggregates, and again derive the optimal policy rule that is consistent with such preferences, under the same constraint. Finally, for each choice of the loss function they compare the performance of the two policy rules; they find that in all cases the welfare differences are small, on the order of 5 to 10 per cent.

The three papers briefly described above are all, in different ways complementary to our analysis. In particular, De Grauwe, Dewachter and Aksoy (1999) associate the use of information about the individual countries with the nationalistic attitude of the Governing
Council members (and the voting procedure adopted in the Council), while in our paper the usefulness of this information is examined assuming an area-wide formulation of the Eurosystem strategy, unambiguously shared by the Council in its entirety. De Grauwe and Piskorski (2001) always keep the policy rule defined in terms of country-specific variables, focusing on how the results are affected by changes in the definition of preferences.

By contrast, we explore the implications of using and of not using country-specific variables in the design of the policy rule, always keeping the loss function defined over area-wide aggregates. We take their conclusion that only limited welfare differences are discernible in the cases considered to mean that, once one allows monetary policy to react to country-specific variables, the optimal policy is relatively insensitive to changes in the specification of the loss function. This is fully consistent with our own finding that the substantial improvement comes when country-specific elements are allowed for in the reaction function, even in a simplified and constrained form.

The exercise performed by Monteforte and Siviero (2002) is also complementary to ours. They rely on the same three-country model used in this paper and on its area-wide counterpart, estimated on aggregate data. Assuming a loss function defined over area-wide aggregates, simple optimal rules (whose arguments are solely aggregate variables) are computed under the constraint provided by either model. The performance of the rules is then assessed assuming the multi-country model to be the “true” data generating process. The results show significant welfare losses when the central bank relies on the area-wide model.

Wyplosz (1999) focuses on the problems posed for the ECB by the lack of synchronisation across EMU economies. He performs two exercises: in the first, the ECB is assumed to set its policy rate using a Taylor rule in which output growth and inflation are weighted averages of the corresponding time-series of the participating countries. In the second, the output variable is replaced with an index that assigns 50 per cent of the weight to the average output and 50 per cent to the output of the country that is experiencing a particularly strong deviation of growth from the average. He finds that the resulting interest rate series differ little, both because the interest rate autoregressive coefficient is large and because the output coefficient in the rule is small.

---

6 In this framework, as in De Grauwe (2000) and in the present paper, the welfare effects of neglecting national information are therefore negative by definition.
Benigno (1999) analyses monetary policy in a monetary union using a two-region, general equilibrium model with monopolistic competition and price stickiness, showing that if the degrees of rigidity are different, policy should assign a greater weight to the region where rigidity is greater.

3. A small empirical model for the main euro-area economies

The euro-area economy is described by a simple two-equation model for each of the three main economies (Germany, France and Italy, which account for over 70 per cent of the area GDP), consisting of an aggregate supply equation (also referred to as Phillips curve) and an aggregate demand equation (also referred to as IS curve). The first equation determines inflation in each country as a function of lagged inflation and the output gap in that country, and of inflation “imported” from the other two. The sum of the coefficients on lagged and imported inflation is constrained to be one (a restriction accepted by the data), so that an accelerationist version of the Phillips curve holds for all countries. The second equation relates the output gap of each country to its own lagged values and the real interest rate, as well as to the output gap in the other two countries (a design meant to capture the trade links among euro area economies). Euro-area GDP and inflation are generated via identities, as weighted averages of the corresponding individual country variables. The output gaps are aggregated using 1999 GDP weights (under PPP); 1999 consumer spending weights (under PPP) are used to aggregate the inflation rates (for full details as to data construction, see Monteforte (2002)).

As the model allows for simultaneous cross-country linkages, it was estimated with 3SLS. For most of the sample period (from 1978.Q1 to 1998.Q4, totalling 84 observations), the exchange rates among the German, French and Italian currencies were not fixed, though constrained by the Exchange Rate Mechanism of the European Monetary System. Accordingly, the measure of “inflation imported in country i from country j” was constructed as the sum of the inflation rate in country j and the quarter-on-quarter percentage change in the exchange rate between the two countries (units of currency of country i needed for 1 unit of country j’s currency).

7 Inflation is given by the quarter-on-quarter rate of change in the households’ consumption deflator. Potential output was estimated by applying the band-pass filter (Baxter and King (1995)) to the (log) GDP for each country.

8 Given the well-known difficulties to find satisfactory empirical specifications for the exchange rate, no at-
The general form of the two-equation sub-model for country $j$ is the following:

$$
\pi_{t+1}^j = \sum_{k=1}^{\infty} \alpha_{j,k} \pi_{t+1-k}^j + \sum_{k=0}^{\infty} \beta_{j,i,k} (\pi_{t+1-k}^i + \epsilon_{t+1-k}^{i,j}) + \eta_{j,k} y_{t+1-k}^j + u_{t+1}^j \tag{1}
$$

$$
\gamma_{t+1}^j = \sum_{k=1}^{\infty} \theta_{j,k} y_{t+1-k}^j + \sum_{k=0}^{\infty} \varphi_{j,i,k} y_{t+1-k}^j + \psi_{j,k} (\gamma_{t+1-k}^j - 4 \pi_{t+1-k}^j) + v_{t+1}^j \tag{2}
$$

where $\pi_{t+1}^j$ is the quarter-on-quarter consumer inflation rate in country $j$, $\epsilon_{t+1-k}^{i,j}$ is the quarter-on-quarter rate of change in the exchange rate between country $i$ and country $j$ (units of country $j$’s currency for 1 unit of country $i$’s currency), $y_{t+1}^j$ is the output gap in country $j$, $\gamma_{t+1}^j$ is the short-term interest rate in country $j$.

The starting specification included, on the right-hand-side of each equation, the first 6 lags of all relevant variables. After all insignificant lags were dropped, the parsimonious specification presented in Table 1 was achieved. This framework is admittedly a very simple one, as it only models the three major economies in the area, and sketchily at that. While this choice was made primarily for computational reasons, a full-fledged model for the euro area including all twelve countries and paying closer attention to country-specific institutional features (e.g., labour market arrangements, tax structures, fiscal policy mechanisms) would likely result in more pronounced asymmetries. As the existence of such asymmetries is the main factor on which our findings rest, it can be conjectured that our results are likely to represent a lower bound to the welfare gains from properly exploiting all available national information.

Some insights into the main properties of the model can be obtained by looking at a few impulse responses (Figures 1-3). Given our accelerationist version of the Phillips
curve, the model cannot be meaningfully simulated unless it is augmented with a stabilising monetary policy reaction function. Accordingly, the impulse responses were computed with an optimised AWIB rule, derived as described in Section 3 below.

A unit shock was given to the stochastic disturbance of each model equation. Thus, the differences in the responses of the model to aggregate supply and aggregate demand shocks in the various countries reflect only the structural differences among the economies in the area. Monetary policy shocks correspond to a 100-basis-point, one-period increase in the short-term interest rate.

A few prominent features emerge from the pattern of impulse responses:

– a positive monetary policy shock results in a temporary contraction of output that reaches a maximum in the second year; it also tends, initially, to affect output more than inflation, which shows the largest reduction three to four years after the shock;

– neither aggregate supply nor aggregate demand disturbances have permanent effects on output and inflation; however, the deviations from equilibrium tend to be remarkably persistent, at least in some cases;

These features are consistent with well-established stylised facts about the timing of the impact of a monetary policy shock on output and inflation. In particular, the general features of the reaction of inflation and the output gap to a monetary policy shock are remarkably similar to those estimated by van Els, Locarno, Morgan and Villetelle (2001), on the basis of the econometric models for the various euro-area countries developed and used by the corresponding NCBs, and the ECB’s Area-Wide Model (see Fagan, Henry and Mestre

models differ from one another, then the welfare gains associated with paying due care to national developments would likely be even more pronounced. In this respect, our experimental set-up may be viewed, if anything, as somewhat biased in favour of the AWIB rule. In the model used to compute the impulse responses and the optimal policy rules, moreover, the rate of change of the bilateral exchange rates is set to zero, given the single currency. Similarly, while in estimation a measure of country-specific short-term interest rates was used, in the experiments below it was imposed that the interest rate be the same for all countries, i.e.: \( i_{t+1} = i_{t+1} \), for all \( j \)'s.

---

Our model thus seems able to reproduce the main features of the monetary policy transmission mechanisms in reasonably satisfactory fashion.

Looking now more closely at the responses of the model to the shocks, a number of interesting features can be related to individual countries:

- monetary policy takes longer to affect inflation in France than in either Italy or Germany; the time-pattern of the effects in the latter two countries is similar, but the effects are markedly more pronounced in Italy;
- the timing of the effects of monetary policy on the output gap are very similar across countries. The German output gap is the most reactive, followed by Italy;
- the effects on area-wide inflation of shocks hitting the Phillips curve in France tend to vanish more slowly than in either Italy or Germany;
- similarly for aggregate demand shocks: in the case of France, their effects are much more persistent, particularly as far as aggregate euro-area inflation is concerned;
- the effects of an aggregate demand shock are smallest and least volatile if the shock originates in Italy;
- by contrast, the effects on the output gap of an aggregate supply shock originating in Italy are largest and most volatile.

4. Design of the experiments

The analytical framework adopted in this paper is borrowed from the time-honored Tinbergen-Theil approach to policy-making, recently revived by a strand of the literature on monetary policy that addresses the issue of whether the performance under simple rules

12 At a first glance, our results would seem to imply that our MCM results in a considerably slower reaction of the economy to the monetary policy shock, particularly for inflation, than estimated by van Els, Locarno, Morgan and Villetelle (2001); even more so since they examine the effects of a sustained shock (for 8 quarters) to the policy interest rate, while our shock is only for one period. However, one should bear in mind that the simulation experiments in van Els, Locarno, Morgan and Villetelle (2001) do not incorporate a monetary policy reaction function. In our experiments, given that the model is augmented with a monetary policy rule, the shock to the policy interest rate is in fact implicitly a sustained one. This goes in the direction of reconciling the two sets of results, though not entirely.

13 While a case-by-case comparison with other empirical evidence is beyond the scope of this paper, it may be worth emphasising that most of those individual country features are in accordance with the recent results in van Els, Locarno, Morgan and Villetelle (2001), which we take as further evidence that our simple MCM may be deemed to provide a reasonably satisfactory description, for our purposes, of the functioning of the euro area economy.

14 See the papers presented at the January 1998 NBER Conference on Monetary policy rules, recently pub-
obtained by imposing some constraint on the functional form of the optimal reaction function is significantly worse than performance under the latter. In this literature, the underperformance of the simple rules is weighted against their simplicity, which can make them easier for the authorities to use and more useful for communication with the public. Furthermore, simple rules may be more robust than model-dependent optimal rules. Thus, there may be a trade-off between performance in the context of a specific model and robustness.

While we share the analytical approach used by this body of literature, our focus conceptually different. We are not interested in the functional form of the policy rules (e.g. number of lags, or forward- vs. backward-looking specification), or in their robustness; rather, for a given functional form, we compare the performance of rules that include national variables among their arguments with that of rules that react only to area-wide variables.

We assume the policymaker’s loss function to be quadratic and time-separable; its arguments include the deviation of inflation from its target value (assumed to be zero), the output gap, and a term accounting for the central bank’s dislike for excessive interest rate volatility:

\[
L = \sum_{t}^{\infty} E_t \delta^\tau \left[ \pi_t^2 + \lambda \cdot y_t^2 + \mu \cdot (\Delta i_t)^2 \right]
\]

(3)

where \(\delta\) is a discount factor and \(\lambda\) and \(\mu\) are parameters that reflect the policymaker’s preferences. Note that no country-specific variables appear in the loss function, implying that the monetary policy authority is interested solely in area-wide developments.

For \(\delta \rightarrow 1\) (a scaled version of) the intertemporal loss function can be interpreted as the unconditional mean of the period loss functions, which in turn is given by the weighted sum

lished in Taylor (1999); in particular, see Rudebusch and Svensson (1999), who apply this approach to the United States.

15 It has been shown that - unlike optimal rules - certainty equivalence does not hold for simple rules (the rule is not the same as that for the deterministic problem); in addition, the parameters of these rules depend on the covariance matrix of the error terms and on the initial conditions of the system (Currie and Levine, 1985, 1987).

16 To test robustness of the ranking, the comparison is carried out changing one or more elements of the conceptual framework; in particular, different hypotheses are adopted concerning the preferences of the monetary authorities and the possible effects of uncertainty on the structure of the model, the estimation or calibration of the model parameters, and the presence of measurement errors (Rudebusch (1998); Orphanides (1998); Peersman and Smets (1999)). Other authors compare the performance of various rules across different models of the economy (Levine et al. (1999); Taylor (1999)).
of the unconditional variances of the target variables (see Rudebusch and Svensson, (1999)):

\[ L_{t+r} = \text{var}(\pi_{t+r}) + \lambda \cdot \text{var}(y_{t+r}) + \mu \cdot \text{var}(\Delta i_{t+r}) \]  

(4)

We restrict attention to Taylor-type rules augmented with a lagged interest rate term, i.e. rules in which only contemporaneous inflation and output gap appear among the arguments.\(^{17}\) The difference between the AWIB and the MCIB rules is that with the former the policymaker is assumed to react only to area-wide inflation and output gap aggregates (so that the reaction of the policy rate to a change in any country’s inflation and output is given by the average impact, multiplied by the corresponding country weights). Thus, this rule has three arguments (it includes the lagged interest rate):

\[ i_t = \gamma^A_1 \cdot \pi_t + \gamma^A_2 \cdot y_t + \gamma^A_3 \cdot i_{t-1} \]  

(5)

With the MCIB rule, by contrast, the parameters on the individual countries’ inflation and output are not constrained to fulfills any proportionality constraint. This rule includes seven arguments:

\[ i_t = \gamma^M_{1D} \cdot \pi^D_t + \gamma^M_{1F} \cdot \pi^F_t + \gamma^M_{1I} \cdot \pi^I_t + \gamma^M_{2D} \cdot y^D_t + \gamma^M_{2F} \cdot y^F_t + \gamma^M_{2I} \cdot y^I_t + \gamma^M_3 \cdot i_{t-1} \]  

(6)

As a benchmark, we also compute the fully optimal instrument rule that depends on all state variables of the multi-country model (15 in all).

The two competing AWIB and MCIB rules stem from the solution of the following problems:

<table>
<thead>
<tr>
<th>Optimization exercise based on AWIB rule</th>
</tr>
</thead>
</table>
| \[
\min_{\gamma^A_1, \gamma^A_2, \gamma^A_3} E \mathbb{P}_{\tau=0} \sum_{\tau=0}^{\infty} [\pi^2_{t+r} + \lambda \cdot y^2_{t+r} + \mu \cdot (\Delta i_{t+r})^2] \]
| s.t.: • Multi-country model, and |
|       • eq. (5) |

\(^{17}\) As is shown in Rudebusch and Svensson (1999), rules of this kind tend to produce an outcome that comes remarkably close to the one associated with the optimal instrument rule; this will be shown to be also the case for the experiments carried out below.
and:

\[
\begin{align*}
\text{Optimization exercise based on MCIB rule} \\
\min_{\gamma_1^{M}, \gamma_1^{F}, \gamma_1^{I}, \gamma_2^{M}, \gamma_2^{F}, \gamma_2^{I}, \gamma_3^{M}} E_t^P \mathbb{E}_{\tau=0}^{\infty} \left[ \pi_{t+\tau}^2 + \lambda \cdot y_{t+\tau}^2 + \mu \cdot (\Delta i_{t+\tau})^2 \right]
\end{align*}
\]

s.to: 
- Multi-country model, and
- eq. (6)

It is clear from these panels that the performance of an optimal MCIB rule cannot be worse, by construction, than the corresponding AWIB performance, as the former boils down to being an unconstrained version of the latter. The issue then is: Given that the MCIB approach necessarily results in an optimised value of the loss function at least as desirable as the AWIB approach, are the welfare gains at stake large enough to make it worthwhile to exploit all available national information?

The variances of the goal variables are of course a function both of the choice of the parameters in the two rules above and of the variance-covariance matrix of the stochastic terms in the estimated equation. The latter is given in Table 2. The historical variance-covariance matrix is rather sparse. Indeed, the results were not perceptibly modified by introducing the assumption that the off-diagonal block (i.e., the one that includes the covariances between the set of the three aggregate supply equations and the set of the three aggregate demand equations) is identically zero.

In addition to minimising the loss function (3) subject to the variance-covariance matrix of Table 2, following De Grauwe and Piskorski (2001) we repeated the experiments under the alternative assumption that all stochastic processes belonging to the same diagonal block are exactly the same; their (common and identical) variance is obtained as an average of the three corresponding historical variances. This alternative assumption may be viewed as a very crude, perhaps extreme, way of taking into account the possibility that the euro-area economies are now more similar than they were in the estimation period.

---

18 More precisely, as in De Grauwe and Piskorski (2001), the average variances are calculated as squared weighted sums of the standard deviations of the country specific Phillips curve and aggregate demand shocks.
5. The results

The main results of the exercise are reported in Table 3 and Figures 4 and 5. The table displays the long-run values of the coefficients of the three instrument rules described earlier (the “Fully optimal” (FO), the “Area-wide” (AWIB) and the “Multi-country” (MCIB)), for different choices of the weights $\lambda$ and $\mu$ assigned to output gap and interest rate variability in the loss function.\footnote{Our choices of the values for $\lambda$ and $\mu$ range from the extreme in which the monetary policymaker is interested only in inflation ($\lambda = \mu = 0$) to the opposite extreme, in which the policymaker assigns a very high cost to deviations of the output gap from its equilibrium value (zero) and to the volatility of the policy-controlled interest rate ($\lambda = \mu = 3$). Assuming $\lambda = \mu = 0$ delivers optimal rule parameter values that are not entirely plausible. By contrast, even a very small weight on interest rate volatility suffices to make the results more sensible.} For ease of comparison, the table presents the coefficients assigned both to area-wide and to country-specific inflation and output-gap for each rule.\footnote{The fully optimal rule depends on the complete set of the 15 state variables in the MCM: this set comprises inflation and output gap in the various countries for different lags. The coefficient on inflation reported in Table 4.1 is given, for the fully optimal rule, by the sum of the value of all coefficients that the rule assigns to inflation in all countries and for all lags; similarly for the output gap.} Clearly, depending on the rule, one or the other will be the direct result of the optimisation (in bold) and the complement will only be implicit. For instance, the implicit inflation coefficient for France in the third row (1.33) is obtained by multiplying the optimised area-wide inflation coefficient (4.86) by the relative weight of France out of the total three-country aggregate (0.27), while the implicit area-wide inflation coefficients in the first and second rows are obtained by summing the three national coefficients (respectively, 2.99=1.61+0.90+0.48 and 3.12=1.45+1.18+0.49). The table also shows the standard deviations of inflation, output gap and interest rate change, as well as the loss function obtained for each rule. The top panel of Figure 4 shows the reduction of the loss with the MCIB rule \textit{vis-à-vis} the AWIB, for wider grids of $\lambda$ and $\mu$ than those reported in Table 3; the bottom panel expresses this reduction as a percentage of the difference between the AWIB and the FO losses. Figure 5 presents the optimal inflation/output gap frontiers (in terms of unconditional standard deviations) for both the AWIB and the MCIB rule and for the fully optimal rule; the frontiers have been computed, for given $\mu$, by letting $\lambda$ take a grid of values between 0 (north-west) and 3 (south-east).

A number of insights can be drawn from these results.

Focusing first on the final outcomes of the policies, the key message is that neglecting the information contained in individual country developments substantially worsens of the
overall performance of monetary policy. Relative to the AWIB rule, the MCIB rule reduces loss by between 25 and 50 per cent, except for the case in which both $\lambda$ and $\mu$ are exactly zero (see Figure 4). The reduction varies with the weights in the loss function and increases when the relative weight of inflation and interest rate smoothness are increased; in particular, when inflation variability and interest rate smoothness are the only concerns, the relative loss reduction associated with the MCIB rule is between 40 and 50 per cent. The improvement is statistically significant: using parametric and non parametric tests, equality of the two distributions or of their means was rejected at all significance levels. While the loss reduction would be influenced by an affine transformation of the loss function, the results can be directly appraised in terms of the (unconditional) standard deviation of inflation, output gap and interest rate changes. Table 3 shows that the MCIB rule reduces the standard deviation by 20-30 per cent for inflation and interest rate changes and by 10-20 per cent for the output gap, compared to the AWIB. Figure 5 shows similar results: the optimised combination of inflation and output gap variability (for varying relative weights) under the AWIB rule is well to the north-east of those for the MCIB rule.

A second insight on the overall performance of monetary policy is that the MCIB does a very good job relative to the FO. This can also be gauged from Figure 5, in which the frontiers associated with the two rules lie close together. This result recalls the literature on the performance of simple rules (see, e.g., Rudebusch and Svensson (1999)). Indeed, the MCIB rule loads only 6 variables, compared with 15 for the FO rule, yet delivers quite similar results.

This naturally shifts the attention to the nature of the rules. A number of noteworthy features emerge. First, the MCIB and FO rules are always remarkably similar, with few exceptions for the weights given to German output gap. Second, relative to FO, the AWIB rule is excessively “reactive” to both inflation and output gap, as the implied (area-wide aggregated) coefficients of the former are considerably smaller than those of the latter (between 35 and 45 per cent for the inflation, between 10 and 50 per cent for the output gap). Also, the AWIB rule in general puts too much weight on aggregate inflation. Third, Italian inflation and output gap have too much implicit weight in the AWIB rule compared to the FO and MCIB rules, by 3 to 6 times (see Table 3). As to the variables of the other two countries, although their weights under AWIB differ from those under the FO rule, the order of magnitude of the differences
is much smaller (usually not exceeding 50 per cent). In particular German variables are both over-weighted; French inflation is over-weighted, and French output gap is under-weighted.

It would obviously be most interesting to trace the various features of the rules back to specific features of the individual economies, so as to assess the robustness of the results here reported. In particular, it would be valuable to understand why the optimal monetary policy — as represented by the FO or, almost equivalently, by the MCIB rule — deviates so much from the relative weighting of the countries associated with the statistical procedure of aggregation. For example, why should the optimal monetary policy reaction to Italian inflation and output gap be so much more muted than would be implied by Italy’s GDP or consumption weight?

This issue is complex. In what follows, let us provide some evidence towards a tentative assessment of the various factors at play.

Table 4 provides a qualitative picture of the relationships between the structure of the economies, as captured by our simple model, and the coefficients of the FO rule. Specifically, a small positive shock was given to each of the 14 structural parameters of the model and the derivative of the coefficients of the FO rule was computed; the table indicates the sign of those derivatives (summarising a large set of numerical results obtained by varying the weights in the loss function). A few noteworthy regularities emerge.

First, if the inflation inertia of one country (the autoregressive coefficient of inflation in the inflation equation for that country) increases (maintaining the vertical nature of the Phillips curve\(^{21}\)), the weights that the FO rule assigns to inflation and the output gap in that country increase. Secondly, if the output gap inertia of one country (the autoregressive coefficient of the output gap in the output gap equation for that country) increases, the weights that the FO rule assigns to inflation and the output gap in that country increase. Thirdly, if the interest rate coefficient in the output gap equation for that country increases (in absolute value), the weight that the FO rule assigns to inflation in that country increases, while the weight assigned to inflation in the other two countries tends to decrease (for the output gap the evidence is less clear-cut). Finally, if the output gap effect on inflation in one country increases, the weight that the FO rule assigns to inflation in that country increases (again, the evidence is less clear-cut for the output gap).

---

\(^{21}\) This implies that the coefficient of the cross-country effect (e.g. of French inflation in the German Phillips curve) is lowered by the same amount, to keep the sum of the coefficients on inflation terms equal to 1.
The first two features hew to a common pattern: any change that increases the inertial component of target variables is associated with a stronger reaction of the single monetary policy to the variables in that country. This seems to suggest that a reduction of the monetary policy “leverage” in one country due to the inertia of the target variables is associated with a more aggressive use of monetary policy. However, the latter two results suggest that monetary policy is more reactive to the variables of the country where the transmission of monetary policy impulses is more effective (either because of its direct effect on the output gap or because of the the impact of the output gap on inflation): an increase of the effectiveness of the transmission mechanism in one country induces the central bank to concentrate its reaction on the variables of that country and to reduce the weights assigned to those of the other countries.

On the basis of these remarks, the observed “under-weighting” of Italian variables in the FO and MCIB rules can be rationalised only in part. Relative to other countries, the Italian model features a lower autoregressive term in the aggregate demand equation, a lower coefficient of the interest rate in the aggregate demand equation, and a lower coefficient of the output gap in the Phillips curve, all leading to a smaller weight on Italian inflation and output gap in the FO rule. However, another feature of the Italian model — the higher autoregressive term in the Phillips curve — points to the opposite conclusion. At the present stage we can only observe that the former effects seem to dominate.

The weights assigned to the variables by the FO rule can be expected to depend not only on the structural characteristics of the individual economies, but also on the causal structure of the euro-area economy as a whole. In this respect, let us recall a result on the control of dynamic systems obtained by Ando, Simon and Fisher (1963). They suggest that more effective control of a dynamic system characterised by some form of block-recursiveness is obtained by reacting more strongly to those variables that come earlier in the causal chain, since this gives one the bonus of also affecting those that are “downstream”. In the model estimated, there is a causal structure (by country) that is in fact nearly block-recursive, with Germany at the root of the chain (affecting French and Italian inflation, as well as Italian output gap), then France, which affects German inflation (more weakly) and then Italy. This pattern would seem consistent with the over-weighting of Germany and the under-weighting of Italy. Table 4 confirms that increasing the coefficient of the German output gap in the Italian
aggregate demand equation results in a rule that assigns higher parameter values to German inflation and output gap.

Indeed, if the “cross-country” effects (the coefficient on German output gap and inflation in, respectively, the Italian aggregate demand and aggregate supply equations, the coefficient on German inflation in the French aggregate supply equation and the coefficient on French inflation in the German aggregate supply equation) are put close to zero, the weights assigned by the FO rule to the various countries become very close to those implied by the aggregation weighting scheme.

It may be useful to examine the response of the model to a variety of shocks assuming policy is set on the basis of the FO, AWIB and MCIB rules, alternatively. This is done in Figures 6, 7 and 8. The responses of the model under the MCIB and FO rules do not differ greatly, but the AWIB rule results in visibly more pronounced oscillations.

So far, our reading of the basic result of this paper (that neglecting country-specific information in the monetary policy reaction function carries substantial welfare costs) has taken the FO rule as benchmark. Trying to understand why the FO rule weights country variables differently from the statistical aggregation procedure helps to see why the AWIB rule, which is constrained to adopt the latter relative weighting scheme, underperforms the MCIB rule, which can come closer to the fully optimal weighting scheme. A somewhat different tack would be to ask what conditions would attenuate the underperformance of AWIB. Clearly, one would expect the gap to narrow when the single economies become more “similar”, as the advantage of the MCIB rule lies precisely in exploiting differences in the working of the economies. But it is not obvious which yardstick should be used to gauge similarity. One possibility, following De Grauwe and Piskorski (2001), is to assume that the variance-covariance matrix of the disturbances converges to some common pattern, thus reducing the asymmetry of the shocks hitting the various countries. One extreme case of this kind of “similarity” is tantamount to assuming that the shocks hitting the aggregate demand and the aggregate supply equations respectively are exactly the same in all countries. Figure 9 provides a summary of the results obtained under this extreme assumption: the relative loss reduction achieved by the optimal MCIB rule (compared to AWIB) is considerably smaller than in our

---

22 Close, but not exactly equal to zero, since in the latter case the solution algorithm would become unreliable.
benchmark case, and in all cases less than 10 per cent. All rules perform less satisfactorily than in the experiments in which the historical variance-covariance matrix was assumed to hold, the worsening being of course much more pronounced in FO and MCIB cases than in AWIB. A general worsening of the optimised losses should indeed be expected: in this latter experiment the shocks are perfectly correlated, whereas actual shocks in the past have been virtually independent, hence not reciprocally reinforcing.

A more systematic investigation of the consequences of convergence is presented in Siviero and Terlizzese (2002). They find that asymmetry of both economic structures and stochastic shocks is necessary for national information to be of value for monetary policy-making. However, their investigation of the consequences of partial convergence — in which the shocks (and the structures) become increasingly similar and more correlated, but not exactly the same across countries — shows that a rather high degree of convergence must be reached for the MCIB-rule gains to be reduced by a sizeable amount.

Summing up, it seems that all the features of the economies (their internal mechanisms as well as their interrelationships) impinge upon the weights of the FO rule and presumably, though this still remains to be checked, on the weights of the MCIB rule and on the relative performance of the MCIB rule relative to that of the AWIB rule. Moreover, the nature of the correlation structure of shocks to single economies also has a bearing on relative performance. This suggests the importance of thorough empirical inquiry into the properties of the euro-area economy and of the monetary policy transmission mechanism, an inquiry that, fortunately, has recently gained momentum both in academia and in the central banking community.

6. Preliminary conclusions and possible extensions

This paper examines how much the effectiveness of monetary policy in the euro area may be enhanced by paying attention to national information, as opposed to reacting exclusively to aggregate area-wide variables. The starting conjecture is that this distinction should be relevant because of the structural differences between countries. The exercise is based on a simple aggregate demand-aggregate supply multi-country model for the three main economies of the area and a standard quadratic loss function of the central bank. While the objectives in the loss function are expressed exclusively in terms of area-wide aggregates — so that the exercise is fully consistent with the area-wide orientation of the single monetary policy — the
arguments of the Eurosystem reaction function (given by a Taylor-type rule) are assumed to be aggregate values of inflation and the output gap or, alternatively, the corresponding national values.

The main results can be summarised as follows:

– the rule that reacts to individual country information (labelled MCIB) yields results that are very close to those of the fully optimal rule (FO);
– the MCIB rule delivers large welfare gains with respect to the rule based solely on area-wide information (AWIB), with loss reductions varying between 25 and 50 per cent, depending on the preference parameters;
– relative to the FO and MCIB rules, AWIB rule is “over-reactive”, to both inflation and the output gap;
– the general overreaction of the AWIB rule is implicitly far too pronounced for Italy, for both inflation and the output gap, less so for Germany and France.

These results suggest that, from the viewpoint of the optimal monetary policy-making, the assessment of euro-area economic conditions must pay due care to national developments; neglecting them can be very costly.

The paper also provides a tentative assessment of the factors underlying the results, tracing the latter back to the structure of the three economies considered and the causal links among them.

Overall, the results should not be interpreted as providing specific indications on the appropriate reaction of monetary policy to the actual structural asymmetries prevailing in the euro area. At this stage, the preliminary character of the analysis, as well as the simplified conceptual setup, prevent any such interpretation. However, we see our results as making a clear case for exploiting national information in formulating the single monetary policy.

Several robustness checks need to be done. In particular, we plan to check whether the gain deriving from the use of national information is sensitive to the class of rules one is

---

23 For instance, throughout the simulation exercises the model coefficients estimated are taken as given, in particular those capturing the degree of inflation inertia and the slope of the Phillips curve. However, since in reality they are likely to be endogenous, it is not obvious that the policy maker would like to react to heterogeneity in these coefficients without closely monitoring their stability.
considering (for example, forward or backward looking, with richer dynamics, with a larger conditioning set, etc).

A line of research that is also worth pursuing concerns the specification of the loss function. In place of the traditional quadratic loss function, with the deviation of inflation from the target and the output gap as arguments, one could use a lexicographic approach, whereby the price stability objective is given the priority that the Statute of the ECB assigns to it (see Terlizzese, 1999). With a more radical departure from the basic tenet of this paper — only area-wide objectives are relevant — we could also consider the case in which the Eurosystem is concerned with variance between countries. Although it is at odds with the Eurosystem’s description of its strategy, such an attitude would not necessarily conflict with the Treaty, which requires it to “support the general economic policies in the Community with a view to contributing to the objectives of the Community laid down in Article 2” without prejudice to the objective of price stability. Among these objectives, one finds: “to promote throughout the Community a harmonious and balanced development of economic activities, a high degree of convergence of economic performance, economic and social cohesion and solidarity among Member States” (italics added). General as they are, these objectives could in principle imply that a cost should be assigned to dispersion of economic developments across the area.
# Table 1

## THE ESTIMATED MULTI-COUNTRY MODEL

<table>
<thead>
<tr>
<th>Input from:</th>
<th>Equations for: Germany</th>
<th>Equations for: France</th>
<th>Equations for: Italy</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>π</td>
<td>y</td>
<td>π</td>
</tr>
<tr>
<td>Germany</td>
<td>0.292 [-1]</td>
<td>0.063 [0] (restr.)</td>
<td>0.036 [0] (restr.)</td>
</tr>
<tr>
<td></td>
<td>0.600 [-4]</td>
<td>(0.069)</td>
<td>(0.069)</td>
</tr>
<tr>
<td></td>
<td>0.095 [-1]</td>
<td>(0.036)</td>
<td>0.785 [-1]</td>
</tr>
<tr>
<td></td>
<td>(0.069)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>r</td>
<td>-0.073 [-2]</td>
<td>(0.038)</td>
</tr>
<tr>
<td>France</td>
<td>0.108 [0] (restr.)</td>
<td></td>
<td>0.937 [-1]</td>
</tr>
<tr>
<td></td>
<td>0.022 [-2]</td>
<td>(0.012)</td>
<td>0.022 [-3]</td>
</tr>
<tr>
<td></td>
<td>(0.036)</td>
<td></td>
<td>0.022 [-4]</td>
</tr>
<tr>
<td></td>
<td>(0.012)</td>
<td></td>
<td>0.022 [-5]</td>
</tr>
<tr>
<td></td>
<td>r</td>
<td>-0.036 [-2]</td>
<td>(0.015)</td>
</tr>
<tr>
<td>Italy</td>
<td>π</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>y</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>r</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>R²</td>
<td>0.514</td>
<td>0.635</td>
</tr>
<tr>
<td></td>
<td>R²</td>
<td>0.483</td>
<td>0.622</td>
</tr>
<tr>
<td></td>
<td>σ</td>
<td>0.411</td>
<td>0.799</td>
</tr>
<tr>
<td></td>
<td>DW</td>
<td>2.160</td>
<td>2.059</td>
</tr>
</tbody>
</table>

In parentheses: standard error of the coefficients.

In brackets: lag with which the variables enter the equations.
## Table 2

**CORRELATION MATRIX OF STOCHASTIC DISTURBANCES**

<table>
<thead>
<tr>
<th></th>
<th>Aggregate supply</th>
<th>Aggregate demand</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Germany</td>
<td>France</td>
</tr>
<tr>
<td>Aggregate supply</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Germany</td>
<td>1</td>
<td>-0.024</td>
</tr>
<tr>
<td>France</td>
<td>1</td>
<td>0.188</td>
</tr>
<tr>
<td>Italy</td>
<td>1</td>
<td>0.182</td>
</tr>
<tr>
<td>Aggregate demand</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Germany</td>
<td></td>
<td></td>
</tr>
<tr>
<td>France</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Italy</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 3

Reaction function coefficients and loss values for the fully optimal, the area-wide, and the multi-country rules

<table>
<thead>
<tr>
<th>Parameter values in the loss function:</th>
<th>Type of rule</th>
<th>Long-run coefficients on:</th>
<th>Standard deviation of:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Inflation</td>
<td>Output gap</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Area</td>
<td>Ger</td>
</tr>
<tr>
<td>$\lambda = 0.1$</td>
<td>FO</td>
<td>2.99</td>
<td>1.61</td>
</tr>
<tr>
<td></td>
<td>MCIB</td>
<td>3.12</td>
<td>1.45</td>
</tr>
<tr>
<td></td>
<td>AWIB</td>
<td>4.86</td>
<td>2.16</td>
</tr>
<tr>
<td>$\mu = 0.1$</td>
<td>FO</td>
<td>2.08</td>
<td>1.16</td>
</tr>
<tr>
<td></td>
<td>MCIB</td>
<td>2.21</td>
<td>1.02</td>
</tr>
<tr>
<td></td>
<td>AWIB</td>
<td>3.73</td>
<td>1.66</td>
</tr>
<tr>
<td>$\mu = 1$</td>
<td>FO</td>
<td>2.27</td>
<td>1.23</td>
</tr>
<tr>
<td></td>
<td>MCIB</td>
<td>2.24</td>
<td>1.07</td>
</tr>
<tr>
<td></td>
<td>AWIB</td>
<td>3.90</td>
<td>1.73</td>
</tr>
<tr>
<td>$\lambda = 1$</td>
<td>FO</td>
<td>1.83</td>
<td>1.02</td>
</tr>
<tr>
<td></td>
<td>MCIB</td>
<td>1.88</td>
<td>0.88</td>
</tr>
<tr>
<td></td>
<td>AWIB</td>
<td>3.21</td>
<td>1.43</td>
</tr>
<tr>
<td>$\mu = 0.1$</td>
<td>FO</td>
<td>2.03</td>
<td>1.10</td>
</tr>
<tr>
<td></td>
<td>MCIB</td>
<td>1.98</td>
<td>0.95</td>
</tr>
<tr>
<td></td>
<td>AWIB</td>
<td>3.55</td>
<td>1.58</td>
</tr>
<tr>
<td>$\lambda = 2$</td>
<td>FO</td>
<td>1.70</td>
<td>0.95</td>
</tr>
<tr>
<td></td>
<td>MCIB</td>
<td>1.73</td>
<td>0.82</td>
</tr>
<tr>
<td></td>
<td>AWIB</td>
<td>2.97</td>
<td>1.32</td>
</tr>
</tbody>
</table>

Note:
The fully optimal rule depends on the complete set of the 15 state variables in the multi-country model, including inflation and the output gap in the various countries for different lags; the coefficients for both inflation and the output gap reported in the table are given by the sum of the coefficients for all lags and, in the case of area-wide variables, of the coefficients for all lags and countries. For the other two rules, the coefficients reported in bold face are those directly resulting from the optimisation; the other coefficients are implicit.
Derivatives of the reaction function coefficients with respect to the coefficients in the model equations

<table>
<thead>
<tr>
<th>Coefficients in the model equations (2)</th>
<th>Reaction function coefficients</th>
<th>Inflation in:</th>
<th>Output gap in:</th>
<th>Lagged interest rate</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Germany</td>
<td>France</td>
<td>Italy</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aggregate supply equation for Germany</td>
<td>( \pi_g(-1) )</td>
<td>++</td>
<td>--</td>
<td>\sim (\pm)</td>
</tr>
<tr>
<td></td>
<td>( \pi_g(-4) )</td>
<td>++</td>
<td>--</td>
<td>\sim (\pm)</td>
</tr>
<tr>
<td></td>
<td>( y_g(-1) )</td>
<td>++</td>
<td>--</td>
<td>\sim (\pm)</td>
</tr>
<tr>
<td>Aggregate demand equation for Germany</td>
<td>( y_g(-1) )</td>
<td>++</td>
<td>+/-</td>
<td>++</td>
</tr>
<tr>
<td></td>
<td>( r_g(2) )</td>
<td>--</td>
<td>++</td>
<td>++</td>
</tr>
<tr>
<td>Aggregate supply equation for France</td>
<td>( \pi_i(-1) )</td>
<td>--</td>
<td>++</td>
<td>\sim (\pm)</td>
</tr>
<tr>
<td></td>
<td>( y_i )</td>
<td>+/-</td>
<td>--</td>
<td>++</td>
</tr>
<tr>
<td>Aggregate demand equation for France</td>
<td>( y_i(-1) )</td>
<td>\sim (\pm)</td>
<td>\sim (\pm)</td>
<td>++</td>
</tr>
<tr>
<td>Aggregate supply equation for Italy</td>
<td>( \pi_i(-1) )</td>
<td>--</td>
<td>--</td>
<td>++</td>
</tr>
<tr>
<td></td>
<td>( y_i )</td>
<td>+/-</td>
<td>--</td>
<td>++</td>
</tr>
<tr>
<td>Aggregate demand equation for Italy</td>
<td>( y_i )</td>
<td>\sim (\pm)</td>
<td>\sim (\pm)</td>
<td>++</td>
</tr>
<tr>
<td></td>
<td>( r_i(-1) )</td>
<td>++</td>
<td>+/-</td>
<td>++</td>
</tr>
</tbody>
</table>

(1) “++” indicates that the derivative is slightly positive; “+++” indicates that it is positive and comparatively large; similarly for “–” and “––”. “\sim” indicates derivatives consistently close to 0 for all l’s and m’s. “\sim (\pm)” indicates that the sign of derivatives changes depending on l’s and m’s.

(2) Lags are indicated in parentheses.
Fig. 1

Impulse responses to a temporary monetary policy shock (+100 b.p.)

(a) Response of individual country and euro-area inflation rates

(b) Response of individual country and euro-area output gaps

(a) Response of individual country real interest rates

(d) Response of euro-area nominal interest rate
Impulse responses to a temporary Phillips curve shock (individual countries’ stochastic terms: +1)

(a) Response of euro-area inflation rate

(b) Response of euro-area output gap

(c) Response of euro-area real interest rate

(d) Response of euro-area nominal interest rate
Impulse responses to a temporary aggregate demand shock (individual countries’ stochastic terms: +1)

(a) Response of euro-area inflation rate

(b) Response of euro-area output gap

(c) Response of euro-area real interest rate

(d) Response of euro-area nominal interest rate
Fig. 4

Percentage reduction in the optimised loss function, MCIB rule vs. AWIB rule

Percentage reduction in the optimised loss function, MCIB rule vs. AWIB rule as a share of overall reduction, FO rule vs. AWIB rules
Fig. 5

Inflation - output gap optimal frontiers

(a) $\mu=0.1$

(b) $\mu=1$

(c) $\mu=2$

(d) $\mu=3$
Impulse responses to a temporary Phillips curve shock (+1 s.d. of stochastic terms) under FO, AWIB and MCIB rules

(a) Response of euro-area inflation rate

(b) Response of euro-area output gap

(c) Response of euro-area nominal interest rate
Impulse responses to a temporary aggregate demand shock (+1 s.d. of stochastic terms) under FO, AWIB and MCIB rules

(a) Response of euro-area inflation rate

(b) Response of euro-area output gap

(c) Response of euro-area nominal interest rate
Impulse responses to a temporary monetary policy shock (+1 s.d. of stochastic terms) under FO, AWIB and MCIB rules

(a) Response of euro-area inflation rate

(b) Response of euro-area output gap

(c) Response of euro-area nominal interest rate
Fig. 9

Percentage reduction in the optimised loss function, MCIB rule vs. AWIB rule with identical Phillips curve and aggregate demand stochastic processes in all countries.
References


No. 434 — The construction of coincident and leading indicators for the euro area business cycle, by F. ALTISSIMO, A. BASSANETTI, R. CRISTADORO, L. REICHLIN and G. VERONESE (December 2001).

No. 435 — A core inflation index for the euro area, by R. CRISTADORO, M. FORNI, L. REICHLIN and G. VERONESE (December 2001).


No. 437 — The use of preliminary data in econometric forecasting: an application with the Bank of Italy Quarterly Model, by F. BUSSETTI (December 2001).

No. 438 — Financial crises, moral hazard and the “speciality” of the international interbank market; further evidence from the pricing of syndicated bank loans to emerging markets, by F. SPADAFOREA (March 2002).


No. 440 — Bootstrap bias-correction procedure in estimating long-run relationships from dynamic panels, with an application to money demand in the euro area, by D. FOCARELLI (March 2002).

No. 441 — Forecasting the industrial production index for the euro area through forecasts for the main countries, by R. ZIZZA (March 2002).

No. 442 — Introduction to social choice and welfare, by K. SUZUMURA (March 2002).

No. 443 — Rational ignorance and the public choice of redistribution, by V. LARCINESE (July 2002).

No. 444 — On the ‘conquest’ of inflation, by A. GERALI and F. LIPPI (July 2002).


No. 446 — Currency crises and uncertainty about fundamentals, by A. PRATI and M. SBRACIA (July 2002).

No. 447 — The size of the equity premium, by F. FORNARI (July 2002).

No. 448 — Are mergers beneficial to consumers? Evidence from the market for bank deposits, by D. FOCARELLI and F. PANETTA (July 2002).

No. 449 — Contemporaneous aggregation of GARCH processes, by P. ZAFFARONI (July 2002).

No. 450 — Un’analisi critica delle definizioni di disoccupazione e partecipazione in Italia, by E. VIVIANO (July 2002).

No. 451 — Liquidity and announcement effects in the euro area, by P. ANGELINI (October 2002).

No. 452 — Misura e determinanti dell’agglomerazione spaziale nei comparti industriali in Italia, by M. PAGNINI (October 2002).


No. 454 — Italian households’ debt: determinants of demand and supply, by S. MAGRI (October 2002).

No. 455 — Heterogeneity in human capital and economic growth, by S. ZOTTERI (October 2002).

No. 456 — Real-time GDP forecasting in the euro area, by A. BAFFIGI, R. GOLINELLI and G. PARIGI (December 2002).

(*) Requests for copies should be sent to: Banca d’Italia – Servizio Studi – Divisione Biblioteca e pubblicazioni – Via Nazionale, 91 – 00184 Rome (fax 0039 06 47922059). They are available on the Internet at www.bancaditalia.it
1999


2000


2001


2002


FORTHCOMING


F. Schivardi, Reallocation and learning over the business cycle, European Economic Review, TD No. 345 (December 1998).

F. Altissimo, S. Siviero and D. Terlizze, How deep are the deep parameters?, Annales d’Economie et de Statistique, TD No. 354 (June 1999).


M. Sbracia and A. Zaghini, The role of the banking system in the international transmission of shocks, World Economy, TD No. 409 (June 2001).

E. Gaiotti and A. Generale, Does monetary policy have asymmetric effects: A look at the investment decisions of Italian firms, Giornale degli Economisti e Annali di Economia, TD No. 429 (December 2001).

L. Gambacorta, The Italian banking system and monetary policy transmission: Evidence from bank level


D. FOCARELLI, Bootstrap bias-correction procedure in estimating long-run relationships from dynamic panels, with an application to money demand in the euro area, Economic Modelling, **TD No. 440 (March 2002).**

D. FOCARELLI and F. PANETTA, Are mergers beneficial to consumers? Evidence from the market for bank deposits, American Economic Review, **TD No. 448 (July 2002).**