

# Fiscal Buffers, Private Debt and Stagnation: The Good, the Bad and the Ugly

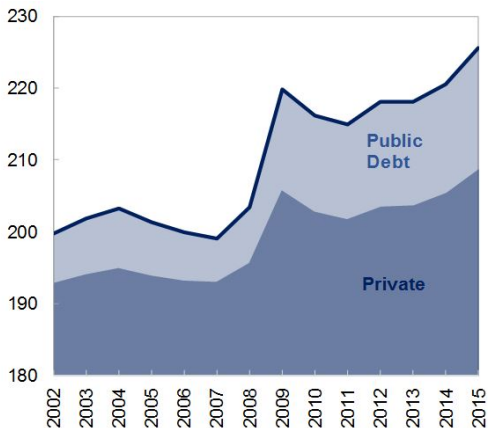
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*The views expressed in this paper are those of the authors and do not necessarily represent those of the Banca d'Italia, the International Monetary Fund or IMF policy.*

# Global Gross Debt (percent of GDP) - Fiscal Monitor 2016



Sources: Abbas and others, 2010; Bank for International Settlements; Dealogic; IMF, *International Financial Statistics*; IMF, *Standardized Reporting Forms*; IMF, *World Economic Outlook*; Organisation for Economic Co-operation and Development; and IMF staff estimates.

# Context

- The Global Financial Crisis followed an extraordinary **upward swing in the leverage cycle** (Geanakoplos et al., 2012, *AER*).
- Bust sparked typical **debt deflation dynamics** (Fisher, 1933, *Econometrica*; Minsky, 1982) that boosted public debt-to-GDP very rapidly:
  - recession-induced **decline in government revenues**;
  - governments **took over** private debt.
- We are left with both **high private and public debt**.

# Research questions

- 1 Do the levels of **private and public debt** amplify swings in economic activity over the leverage cycle?
- 2 Should governments extend **financial assistance** to credit-constrained agents at times of financial stress?

## In this paper:

- We first **empirically** revisit the interaction between private and public debt and economic growth.
- We then build a **DSGE** model that:
  - reproduces leverage cycles;
  - embeds explicit links between private and public debt dynamics;
  - stylizes the empirical relationships between private-public debt and output.
- We use the model to analyze **targeted government interventions** towards financially-constrained agents.

# Empirics

- Similarly to Mian, Sufi and Verner (2017, *QJE*), we estimate

$$\Delta_3 y_{i,t+3} = \alpha_i + \beta_{prd} \Delta_3 \left( \frac{PRD}{Y} \right)_{it-1} + \beta_{pud} \Delta_3 \left( \frac{PUD}{Y} \right)_{it-1} + u_{it}, \quad (1)$$

where  $\Delta_3 y_{it+3}$  is **future output growth** over three years, while  $\Delta_3 \left( \frac{PRD}{Y} \right)_{it-1}$  and  $\Delta_3 \left( \frac{PUD}{Y} \right)_{it-1}$  are the **change in total private/public debt-to-GDP ratio** in the previous three years.

- We seek to capture **partial correlations** between past private and public debt growth and future GDP growth.
- Panel annual dataset of 30 advanced and emerging market countries from 1960 to 2014. [▶ More](#)

# Revisiting the link between private-public debt and output

## Private and Public Debt and Subsequent Real GDP Growth

	Dependent variable: $\Delta_3 y_{it+3}$					
	(1)	(2)	(3)	(4)	(5)	(6)
$\Delta_3 (PRD/Y)_{it-1}$	-0.128*** (0.014)	-0.143*** (0.016)				
$\Delta_3 (PUD/Y)_{it-1}$		-0.014 (0.019)				
$(PRD/Y)_{it-1}$			-0.086*** (0.005)	-0.095*** (-0.006)	-0.087*** (0.006)	-0.212*** (0.030)
$(PUD/Y)_{it-1}$				-0.008 (0.011)	0.057*** (0.015)	-0.119*** (0.032)
$(PUD/Y)_{it-1} \leq 95\%$					✓	
$(PUD/Y)_{it-1} > 95\%$						✓
$R^2$	0.056	0.108	0.131	0.112	0.125	0.034
Country fixed effects	✓	✓	✓	✓	✓	✓
Observations	873	629	898	700	626	74

Notes: Estimates are obtained via panel regressions of real GDP growth from  $t$  to  $t + 3$  on either the change in private and public debt to GDP from  $t - 4$  to  $t - 1$  or the level of private and public debt in  $t - 1$ . \*, \*\*, \*\*\* denote significance at the 0.1, 0.05, 0.01 level, respectively.

## To sum up

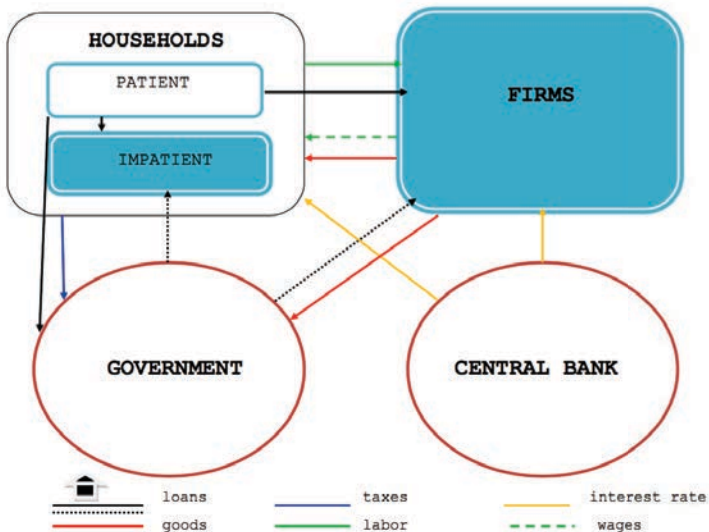
- Surges in **private debt** are unambiguously followed by lower output growth.
- Surges in **public debt** do not generally exacerbate recessions.
- There are **nonlinearities** at play: when the level of public debt is high, further increases in public debt are associated to lower growth *and* the negative effects of excessive private debt on growth are harshened.
- Results are robust to detrended real GDP (consistent with the DSGE model). [▶ More](#)



# Theoretical framework

- Model that produces **leverage cycles** and embeds links between private and public debt dynamics:
  - Basic structure: Iacoviello (2005, *AER*);
  - Government debt and fiscal limits leading to sovereign risk premium (Corsetti et al., 2013, *EJ*; Bi and Traum, 2014, *JAE*);
  - Government financial intervention (in the spirit of Gertler and Karadi, 2011, *JME*).
- Two key **links** between private and public debt:
  - **Financial accelerator**: private deleveraging affects output which depresses government revenues;
  - **Government intervenes** to alleviate borrowing constraints and mitigate private deleveraging.

# The model in a snapshot



## Key model equations - Impatient households

**Impatient households' budget constraint:**

$$\begin{aligned} (1 + \tau_t^C) C_t'' + q_t \Delta h_t'' + \frac{R_{t-1} B_{t-1}''}{\Pi_t} + \frac{R_{t-1} B_{g,t-1}''}{\Pi_t} \leq \\ (1 - \tau_t^W) \frac{W_t''}{P_t} L_t'' + B_t'' + B_{g,t}'' \end{aligned} \quad (2)$$

**Borrowing constraint:**

$$B_t'' \leq m'' E_t \left[ \frac{q_{t+1} h_t'' \Pi_{t+1}}{R_t} \right] \quad (3)$$

## Key model equations - Firms

**Firms' budget constraint:**

$$\begin{aligned} \frac{P_{e,t}}{P_t} Y_{e,t} + B_{e,t} + B_{ge,t} &= (1 + \tau_t^C) C_{e,t} + q_t \Delta h_{e,t} + \frac{R_{t-1} B_{e,t-1}}{\Pi_t} \\ &+ \frac{R_{t-1} B_{ge,t-1}}{\Pi_t} + w_t' L'_{e,t} + w_t'' L''_{e,t} + I_{e,t} + \xi_{K,t} + \xi_{P,t}, \end{aligned} \quad (4)$$

**Borrowing constraint:**

$$B_{e,t} \leq m E_t \left[ \frac{q_{t+1} h_{e,t} \Pi_{t+1}}{R_t} \right]. \quad (5)$$

## Key model equations - Government

**Rules for government financial intervention:**

$$b''_{g,t} = -\epsilon b''_t \quad (6)$$

$$b_{g,t} = -\epsilon b_t \quad (7)$$

where  $x_t = \frac{x_t - x}{y}$

**Government's budget constraint:**

$$B_t^G = \left(1 - \Delta_t^G\right) \frac{R_{t-1}^G B_{t-1}^G}{\Pi_t} + G_t + \frac{(R_{t-1}^G - R_{t-1}) B_{t-1}^{int}}{\Pi_t} + \kappa B_t^{int} - T_t + \Xi_t \quad (8)$$

where  $B_t^{int} \equiv B''_{g,t} + B_{g,t}$ .

**Total government revenue:**

$$T_t = \tau_t^C (C'_t + C''_t + C_t) + \tau_t^W (w'_t L'_t + w''_t L''_t) + \tau_t^L \quad (9)$$

# Calibration

Parameter		Value
Patient households' discount factor	$\beta$	0.99
Impatient households' discount factor	$\beta''$	0.95
Entrepreneurs' discount factor	$\gamma$	0.98
Labor supply elasticity	$\eta$	1.01
Habits in consumption	$\theta$	0.592
Capital depreciation rate	$\delta$	0.03
Capital share	$\omega$	0.30
Patient households' wage share	$\alpha$	0.64
Capital adjustment costs	$\psi_K$	2.00
Elasticity of substitution in goods	$\chi$	6.00
Price stickiness	$\psi_P$	41.667
Inflation -Taylor rule	$\rho_\pi$	1.5
Output -Taylor rule	$\rho_y$	0.1
SS stock of res. housing over annual $y$	$\bar{q} (\bar{h}' + \bar{h}'') / (4\bar{Y})$	1.34
SS commercial real estate over annual $y$	$\bar{q}\bar{h} / (4\bar{Y})$	0.65
SS share of gov. spending in GDP	$\bar{G} / \bar{Y}$	0.23

# Calibration (cont'd)

SS consumption tax rate	$\bar{\tau}^C$	0.20
SS labor income tax rate	$\bar{\tau}^W$	0.45
Persistence of fiscal instruments	$\rho$	0.90
Fiscal responsiveness to government debt	$\rho_B$	0.01
Responsiveness of the fiscal stance to government debt	$\phi$	1.4
Scaling factor in default probability	$\eta_1$	-8.5527
Slope parameter in default probability	$\eta_2$	1.8261
Government intervention	$\epsilon$	0.10
Efficiency costs	$\kappa$	0.10
SS impatient households loan-to-value ratio	$m''$	0.80
SS entrepreneurs loan-to-value ratio	$m$	0.375
SS debt-to-GDP ratio	$\bar{\Gamma}/4$	0.68
Persistence of housing shock	$\rho_H$	0.9890
Persistence of inflation shock	$\rho_P$	0.8171
Persistence of technology shock	$\rho_A$	0.0421
Standard deviation of housing shock	$\sigma^H$	0.0098
Standard deviation of inflation shock	$\sigma^P$	0.0015
Standard deviation of technology shock	$\sigma^A$	0.0233

## Properties of simulated data

Dynamic Correlations Between Private/Public Debt/GDP Ratios and the Output Gap in Simulated Data

Quarters	$corr\left(\frac{B_t^{TOT}}{4Y_t}, Y_{t+i}\right)$		$corr\left(\frac{B_t^G}{4Y_t}, Y_{t+i}\right)$	
	Baseline	High private debt	Baseline	High public debt
$i = 0$	0.5421***	0.5039***	-0.2057***	-0.3363***
$i = 4$	0.3057***	0.2814***	-0.0632	-0.2044***
$i = 6$	0.1329***	0.0832*	0.0006	-0.1318***
$i = 8$	-0.0061	-0.0590	0.0422	-0.0744*
$i = 10$	-0.0714	-0.0986**	0.0588	-0.0383
$i = 12$	-0.1005**	-0.0917**	0.0635	-0.0063

Notes: Correlations are computed on simulated time series of length 500 quarters.  $B_t^{TOT}$  is total private debt.

High private debt refers to LTV ratios in the high range of the distribution in the euro area experience,  $m'' = 0.99$  and  $m = 0.44$ ; high government debt refers to  $\Gamma = 1$ . \*, \*\*, \*\*\* denote significance at the 0.1, 0.05, 0.01 level, respectively.

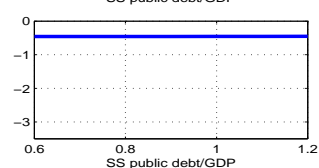
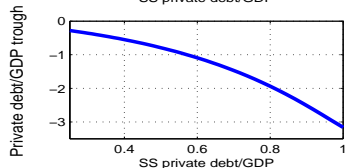
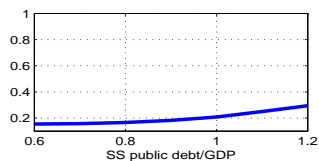
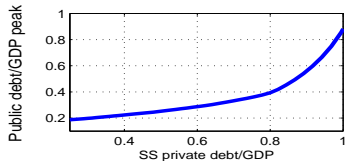
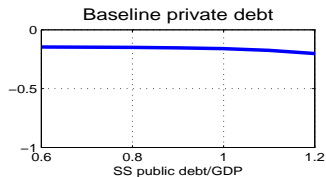
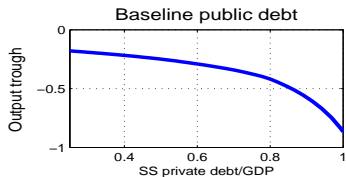


# Impulse responses to a negative 1 % house price shock



Notes: X-axes in quarters; Y-axes are in percent deviations from steady state, except for private and public debt to GDP ratios where deviations are absolute.

# Effects of high private and public debt during deleveraging

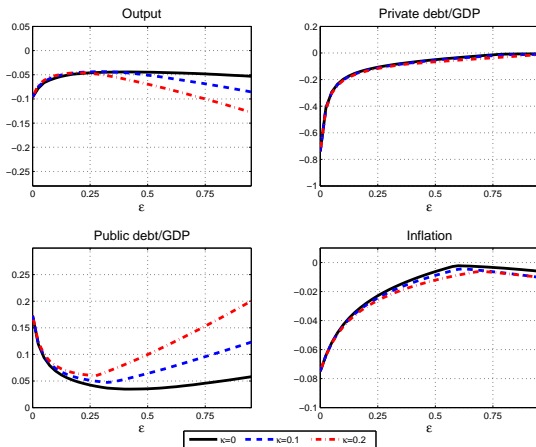


## Should governments extend financial assistance to credit constrained agents in a deleveraging phase?

- Targeted interventions are a form of temporary financial assistance by the government to financially constrained households and firms.
- Since the government is not in the business of funds intermediation, the loan is not perfectly efficient.
- The fiscal cost of targeted intervention is given by: the interest rate differential between the lending and borrowing rate of the government + inefficiency costs.

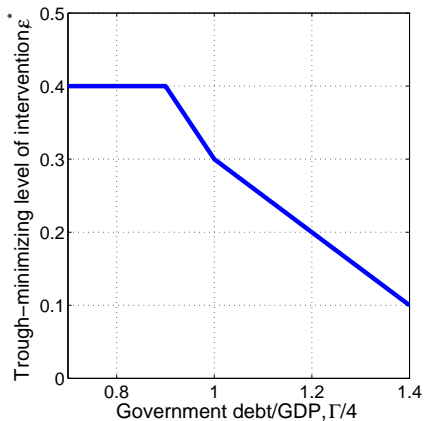
# The effects of targeted interventions

Peak Responses to a Negative One-Per-Cent House Price Shock for Different Degrees of Government Intervention to Private Deleveraging,  $\epsilon$ , and Alternative Levels of Inefficiency Created by Direct Government Intermediation of Funds,  $\kappa$



# “Optimal” level of intervention

## Trough-Minimizing Government Intervention



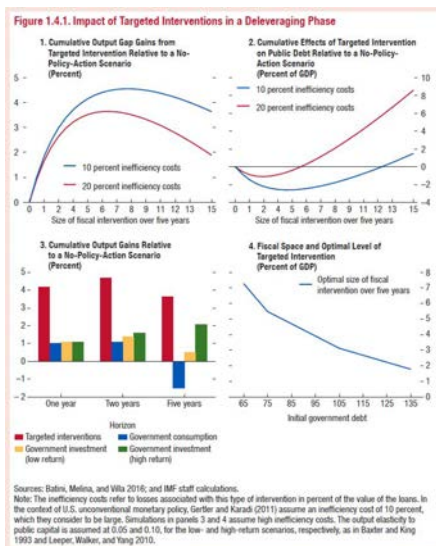
# An application of the model in the IMF Fiscal Monitor 2016 “Debt: Use it Wisely”

Three types of stimuli are considered:

- 1 A targeted intervention in the form of a subsidized government loan to the private sector.
- 2 Government consumption.
- 3 Public investment.

The output benefits of targeted intervention are four times larger than those of more standard stimulus measures.

# Impact of government interventions - FM box 1.4



# Conclusion

- **Private debt booms** raise the **severity** of a recession.
- **Public debt** exacerbates a downturn **only if especially high**.
- There is a **positive “optimal” level of government intervention** targeted at financially constrained agents during a deleveraging phase.
- This is an increasing function of the size of **fiscal buffers**.



## Ground rules and concepts

- What is a **leverage cycle**? An increase (decrease) in private indebtedness caused by an loosening (tightening) of borrowing constraints when collaterals appreciate (depreciate) in value.
- What is **deleveraging**? A reduction in liabilities achieved through cuts to spending.
- What is a **crisis**? A phase of intensified financial stress, which occurs when a drop in the value of the collateral reduces the availability of credit to borrow out of future income.
- What is **public intervention**? It is credit extended to the private sector to alleviate borrowing constraints that originate in swings in the value of private debt collateral.

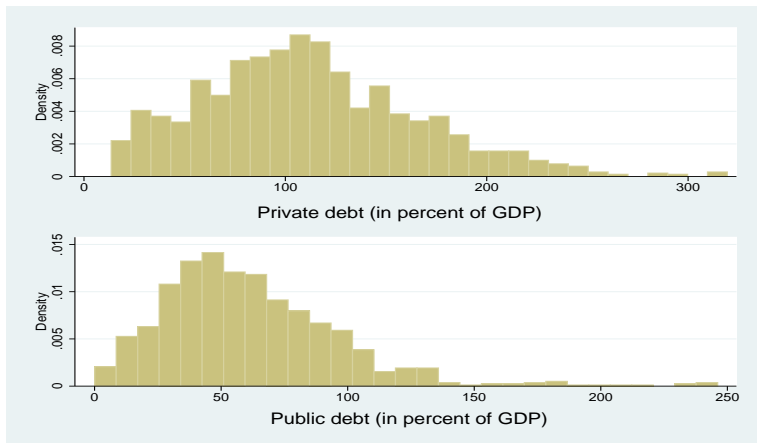
# Countries in panel regressions and descriptive statistics

	Private debt (% of GDP)			Public debt (% of GDP)		
	Years	Average	Std. dev.	Years	Average	Std. dev.
Australia	1960-2014	110.62	47.21	1989-2014	21.75	8.03
Austria	1960-2014	92.29	38.36	1988-2014	68.27	9.28
Belgium	1970-2014	120.52	45.38	1980-2014	111.33	16.01
Canada	1955-2014	126.49	36.49	1980-2014	78.12	14.39
Czech Republic	1993-2014	77.25	10.07	1995-2014	27.92	11.11
Denmark	1966-2014	162.54	48.05	1992-2014	51.00	13.89
Finland	1970-2014	120.34	31.20	1980-2014	36.61	16.67
France	1969-2014	125.86	25.73	1980-2014	54.93	22.21
Germany	1960-2014	100.24	19.14	1991-2014	62.37	11.61
Greece	1970-2014	62.28	33.17	1980-2014	91.52	45.06
Hong Kong	1978-2014	163.28	48.74	2001-2014	1.18	1.00
Hungary	1989-2014	81.49	33.96	1997-2014	66.83	10.04
Indonesia	1976-2014	35.96	15.05	2000-2014	40.31	20.11
Ireland	1971-2014	135.17	85.22	1995-2014	61.43	33.97
Italy	1960-2014	79.55	21.70	1988-2014	109.02	11.61
Japan	1964-2014	169.53	30.98	1980-2014	132.25	66.72
Korea, Rep.	1962-2014	107.75	52.29	1990-2014	21.63	9.58

# Countries in panel regressions and descriptive statistics (cont'd)

	Private debt (% of GDP)			Public debt (% of GDP)		
	Years	Average	Std. dev.	Years	Average	Std. dev.
Mexico	1980-2014	28.30	10.07	1980-2014	34.92	23.07
Netherlands	1961-2014	141.13	70.35	1980-2014	63.21	10.56
Norway	1960-2014	144.30	36.05	1980-2014	36.63	8.53
Poland	1992-2014	50.17	21.06	1995-2014	46.61	5.70
Portugal	1960-2014	124.69	49.46	1990-2014	72.27	28.40
Singapore	1970-2014	98.78	19.75	1963-2014	67.57	25.84
Spain	1970-2014	123.53	44.86	1980-2014	52.09	19.57
Sweden	1961-2014	138.07	44.74	1993-2014	50.70	12.56
Switzerland	1960-2014	156.31	33.05	1983-2014	48.33	11.11
Thailand	1970-2014	86.46	40.24	1996-2014	43.65	9.64
Turkey	1986-2014	31.74	18.82	1987-2014	40.45	12.38
United Kingdom	1963-2014	110.19	46.68	1980-2014	49.87	17.12
United States	1952-2014	110.83	29.93	1947-2014	85.54	15.25

# Distributions of private and public debt/GDP ratios in the sample

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# Detrended GDP as a dependent variable

Private and Public Debt and Subsequent Cyclical Fluctuations of Real GDP

	Dependent variable: $\hat{y}_{it+3}$			
	(1)	(2)	(3)	(4)
$(\frac{PRD}{Y})_{it}$	-0.007*** (0.003)	-0.012*** (0.003)	-0.012*** (0.003)	-0.043*** (0.013)
$(\frac{PUD}{Y})_{it}$		0.006 (0.005)	0.003 (0.008)	-0.029** (0.013)
$(\frac{PUD}{Y})_{it} \leq 95\%$			✓	
$(\frac{PUD}{Y})_{it} > 95\%$				✓
$R^2$	0.003	0.005	0.003	0.003
Country fixed effects	✓	✓	✓	✓
Observations	972	743	659	84

Notes: Estimates are obtained via panel regressions of deviations of real GDP from HP(100) trend in  $t + 3$  on the level of private and public debt in  $t$ . All specifications include country fixed effects. \*, \*\*, \*\*\* denote significance at the 0.1, 0.05, 0.01 level, respectively.

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## Key model equations - Fiscal limit

**Government's fiscal limit (default probability):**

$$p_t^* = P(\Gamma_t^* \leq \Gamma_t) = \frac{\exp(\eta_1 + \eta_2 \Gamma_t)}{1 + \exp(\eta_1 + \eta_2 \Gamma_t)} \quad (10)$$

**Expected haircut rate:**

$$\Delta_t^G = \begin{cases} 0 & \text{with probability } 1 - p_t^* \\ \bar{\Delta}^G & \text{with probability } p_t^* \end{cases} \quad (11)$$

$$\Delta_t^G = p_t^* \bar{\Delta}^G \quad (12)$$

**Sovereign default risk premium:**

$$R_t^G = E_t \left[ (1 - \Delta_{t+1}^G)^{-1} \right] R_t \quad (13)$$

## Calibration of the CDF of the fiscal limit

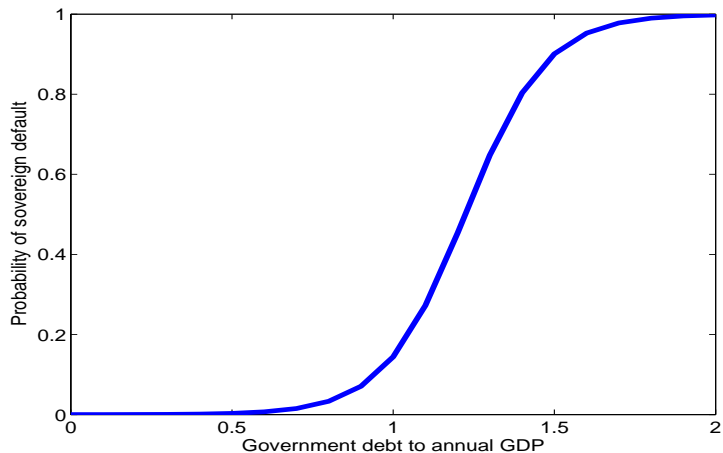
- We fix two points on the function in a way consistent with empirical evidence.
- Given two points  $(\Gamma_1, p_1^*)$  and  $(\Gamma_2, p_2^*)$ , with  $\Gamma_2 > \Gamma_1$ , parameters  $\eta_1$  and  $\eta_2$  are uniquely determined by

$$\eta_2 = \frac{1}{\Gamma_1 - \Gamma_2} \log \left( \frac{p_1^* (1 - p_2^*)}{p_2^* (1 - p_1^*)} \right), \quad (14)$$

$$\eta_1 = \log \left( \frac{p_1^*}{1 - p_1^*} \right) - \eta_2 \Gamma_1. \quad (15)$$

- We assume that at  $\Gamma_2$  the probability of exceeding the fiscal limit is almost unity, i.e.  $p_2^* = 0.99$ .
- We can recover the haircut rate,  $\bar{\Delta}$ , consistent with  $ABP_2$  and  $p_2^*$ .
- At this point, we can recover the probability of default  $p_1^*$ .

# Cumulative density function of the fiscal limit





# Policy rules

## Fiscal rules

$$\log\left(\frac{\tau_t}{\tau}\right) = \rho \log\left(\frac{\tau_{t-1}}{\tau}\right) + (1 - \rho) \left[ e^{\phi \frac{B^G}{Y}} \rho_B \log\left(\frac{B_{t-1}^G}{B^G}\right) \right] \quad (16)$$

$$\log\left(\frac{G_t}{G}\right) = \rho \log\left(\frac{G_{t-1}}{G}\right) - (1 - \rho) \left[ e^{\phi \frac{B^G}{Y}} \rho_B \log\left(\frac{B_{t-1}^G}{B^G}\right) \right] \quad (17)$$

## Monetary policy rule:

$$\log\left(\frac{R_t}{R}\right) = \rho_\pi \log\left(\frac{\pi_t}{\pi}\right) + \rho_y \log\left(\frac{Y_t}{Y}\right) \quad (18)$$

## Fiscal space

In the case of higher and higher public indebtedness, intervention can still mitigate output losses, but the government has **much less room for maneuver**.

