# Discussion of: Barigozzi-Lippi-Luciani - Dynamic Factor Models, Cointegration, and Error Correction Mechanisms 

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(9) Few minor points, to be discussed separately with the authors

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- Proposed model:

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x_{t} & =\Lambda F_{t}+\xi_{t} \\
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permanent $v_{2 t}=\eta^{\prime} u_{t}$ (giving rise to common trends) and $d=(q-\tau)$ transitory $v_{1 t}=\eta_{\perp}^{\prime} u_{t}$
(1) $\xi_{t}$ : observable idiosyncratic shocks, allowed to be $\mathrm{I}(0)$ or $\mathrm{I}(1)$, $n \times 1$ possibly autocorrelated, possibly cross correlated

## Model developement 1

- Interpretation of the factors: the structural shocks $v_{1 t}$ and $v_{2 t}$ are interpreted thruogh SVAR-like restrictions, while the factors $F_{t}$ are not. It would be interesting to interpret them, since the observed variables are affected by structural shocks through the factors. An interpretation of the factors would also allow for an interpretation of the cointegration vectors $\beta$, which might therefore be (over)-identified via suitable restrictions, gaining efficiency and insight


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(3) $H_{0 C}(i, j): \lambda_{i j}=0$ (meaning: the $i$-th variable is not affected by the $j$-th factor)


## Model developement 2

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- Measuring the relative relevance of $\xi_{i t}$ and $F_{1 t}, \cdots, F_{r t}$ (or possibly $\left.v_{11 t}, \cdots, v_{1 d t}, v_{21 t}, \cdots, v_{2(q-d) t}\right)$ in determining the dynamics of $x_{i t}$ (something like FEVD): I believe that a major difficulty comes from the fact that the $\xi^{\prime}$ 's are allowed to be I(0) or I(1), autocorrelated or not, cross correlated or not.


## Application

- US macro data, 1960Q3-2012Q4; $n=103$, number of factors $\hat{r}=7$, number of $\hat{q}=3, \hat{\tau}=1, \hat{c}=\hat{r}-\hat{q}+(\hat{q}-\hat{\tau})=6$


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- Are $\hat{r}$ and $\hat{q}$ in the benchmark model in differences based on a statistical analysis or they are fixed at 7 and 3?
- Two different/alternative identification schemes are used (sign restrictions to identify the monetary shock, BQ long-run restrictions for the technology shock): it would be preferable to merge the two schemes by first separating the technology shock a la BQ, and then identify the 2 transitory shocks via sign-restrictions.

